## 4

## Organic Compounds: Cycloalkanes and Their Stereochemistry

## Organic Knowledge tools

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Online homework for this chapter may be assigned in Organic OWL.

We've discussed only open-chain compounds up to this point, but most organic compounds contain rings of carbon atoms. Chrysanthemic acid, for instance, whose esters occur naturally as the active insecticidal constituents of chrysanthemum flowers, contains a three-membered (cyclopropane) ring.


Chrysanthemic acid

Prostaglandins, potent hormones that control an extraordinary variety of physiological functions in humans, contain a five-membered (cyclopentane) ring.


Prostaglandin $\mathrm{E}_{1}$

Steroids, such as cortisone, contain four rings joined together-3 sixmembered (cyclohexane) and 1 five-membered. We'll discuss steroids and their properties in more detail in Sections 27.6 and 27.7.


Cortisone

## WHY THIS CHAPTER?

We'll see numerous instances in future chapters where the chemistry of a given functional group is strongly affected by being in a ring rather than an open chain. Because cyclic molecules are so commonly encountered in all classes of biomolecules, including proteins, lipids, carbohydrates, and nucleic acids, it's important that the effects of their cyclic structures be understood.

### 4.1 Naming Cycloalkanes

Saturated cyclic hydrocarbons are called cycloalkanes, or alicyclic compounds (aliphatic cyclic). Because cycloalkanes consist of rings of $-\mathrm{CH}_{2}-$ units, they have the general formula $\left(\mathrm{CH}_{2}\right)_{n}$, or $\mathrm{C}_{n} \mathrm{H}_{2 n}$, and can be represented by polygons in skeletal drawings.


Cyclopropane



Cyclobutane



Cyclopentane


Cyclohexane

Substituted cycloalkanes are named by rules similar to those we saw in the previous chapter for open-chain alkanes (Section 3.4). For most compounds, there are only two steps.

Rule 1 Find the parent.
Count the number of carbon atoms in the ring and the number in the largest substituent chain. If the number of carbon atoms in the ring is equal to or greater than the number in the substituent, the compound is named as an alkylsubstituted cycloalkane. If the number of carbon atoms in the largest substituent is greater than the number in the ring, the compound is named as a cycloalkyl-substituted alkane. For example:


Methylcyclopentane


1-Cyclopropylbutane

Rule 2 Number the substituents, and write the name.
For an alkyl- or halo-substituted cycloalkane, choose a point of attachment as carbon 1 and number the substituents on the ring so that the second substituent
has as low a number as possible. If ambiguity still exists, number so that the third or fourth substituent has as low a number as possible, until a point of difference is found.


Lower
1,3-Dimethylcyclohexane


Lower Lower

NOT


Higher


1-Ethyl-2,6-dimethylcycloheptane

Higher


3-Ethyl-1,4-dimethylcycloheptane


Higher
(a) When two or more different alkyl groups that could potentially receive the same numbers are present, number them by alphabetical priority.

(b) If halogens are present, treat them just like alkyl groups.


1-Bromo-2-methylcyclobutane


2-Bromo-1-methylcyclobutane

Some additional examples follow:


1-Bromo-3-ethyl-5-methylcyclohexane

(1-Methylpropyl)cyclobutane or sec-butylcyclobutane


1-Chloro-3-ethyl-2-methylcyclopentane

Problem 4.1 Give IUPAC names for the following cycloalkanes:
(a)

(b)

(c)

(d)

(e)

(f)


Problem 4.2 Draw structures corresponding to the following IUPAC names:
(a) 1,1-Dimethylcyclooctane
(b) 3-Cyclobutylhexane
(c) 1,2-Dichlorocyclopentane
(d) 1,3-Dibromo-5-methylcyclohexane

Problem 4.3 Name the following cycloalkane:


### 4.2 Cis-Trans Isomerism in Cycloalkanes

In many respects, the chemistry of cycloalkanes is like that of open-chain alkanes: both are nonpolar and fairly inert. There are, however, some important differences. One difference is that cycloalkanes are less flexible than open-chain alkanes. In contrast with the relatively free rotation around single bonds in openchain alkanes (Sections 3.6 and 3.7), there is much less freedom in cycloalkanes.

Cyclopropane, for example, must be a rigid, planar molecule because three points (the carbon atoms) define a plane. No bond rotation can take place around a cyclopropane carbon-carbon bond without breaking open the ring (Figure 4.1).
(a)


(a)

Figure 4.1 (a) Rotation occurs around the carbon-carbon bond in ethane, but (b) no rotation is possible around the carbon-carbon bonds in cyclopropane without breaking open the ring.

Larger cycloalkanes have increasing rotational freedom, and the very large rings ( $\mathrm{C}_{25}$ and up) are so floppy that they are nearly indistinguishable from open-chain alkanes. The common ring sizes $\left(C_{3}-C_{7}\right)$, however, are severely restricted in their molecular motions.

Because of their cyclic structures, cycloalkanes have two faces as viewed edge-on, a "top" face and a "bottom" face. As a result, isomerism is possible in substituted cycloalkanes. For example, there are two different 1,2-dimethylcyclopropane isomers, one with the two methyl groups on the same face of the ring and one with the methyls on opposite faces (Figure 4.2). Both isomers are stable compounds, and neither can be converted into the other without breaking and reforming chemical bonds. Make molecular models to prove this to yourself.

cis-1,2-Dimethylcyclopropane


trans-1,2-Dimethylcyclopropane

Figure 4.2 There are two different 1,2-dimethylcyclopropane isomers, one with the methyl groups on the same face of the ring (cis) and the other with the methyl groups on opposite faces of the ring (trans). The two isomers do not interconvert.

Unlike the constitutional isomers butane and isobutane (Section 3.2), which have their atoms connected in a different order, the two 1,2-dimethylcyclopropanes have the same order of connections but differ in the spatial orientation of the atoms. Such compounds, which have their atoms connected in the same order but differ in three-dimensional orientation, are called stereochemical isomers, or stereoisomers.

Constitutional isomers (different connections between atoms)

Stereoisomers (same connections but different threedimensional geometry)


and


The 1,2-dimethylcyclopropanes are members of a subclass of stereoisomers called cis-trans isomers. The prefixes cis- (Latin "on the same side") and trans(Latin "across") are used to distinguish between them. Cis-trans isomerism is a common occurrence in substituted cycloalkanes.

cis-1,3-Dimethylcyclobutane

trans-1-Bromo-3-ethylcyclopentane

## WORKED EXAMPLE 4.1 Naming Cycloalkanes

ThomsonNOW Click Organic Interactive to learn to write IUPAC names for simple cycloalkanes.
ThomsonNOW Click Organic Interactive to use an online palette to draw cycloalkane structures from their IUPAC names.

Name the following substances, including the cis- or trans- prefix:
(a)

(b)


Strategy In these views, the ring is roughly in the plane of the page, a wedged bond protrudes out of the page, and a dashed bond recedes into the page. Two substituents are cis if they are both out of or both into the page, and they are trans if one is out of and one is into.

Solution
(a) trans-1,3-Dimethylcyclopentane
(b) cis-1,2-Dichlorocyclohexane

Problem 4.4 $\quad$ Name the following substances, including the cis- or trans- prefix:
(a)

(b)


Problem 4.5 Draw the structures of the following molecules:
(a) trans-1-Bromo-3-methylcyclohexane
(b) cis-1,2-Dimethylcyclobutane
(c) trans-1-tert-Butyl-2-ethylcyclohexane

Problem 4.6
Prostaglandin $\mathrm{F}_{2 \alpha}$, a hormone that causes uterine contraction during childbirth, has the following structure. Are the two hydroxyl groups $(-\mathrm{OH})$ on the cyclopentane ring cis or trans to each other? What about the two carbon chains attached to the ring?


Prostaglandin $\mathrm{F}_{2 \alpha}$

Problem 4.7 Name the following substances, including the cis- or trans- prefix (red-brown $=\mathrm{Br}$ ):


### 4.3 Stability of Cycloalkanes: Ring Strain

## Adolf von Baeyer

Adolf von Baeyer (1835-1917) was born in Berlin, Germany, and received his Ph.D. at the University of Berlin in 1858, working with Robert Bunsen and August Kekulé. After holding positions at Berlin and Strasbourg, he was a professor at Munich from 1875 to 1917. He was the first to synthesize the blue dye indigo and was also discoverer of the first barbiturate sedative, which he named after his friend Barbara. Baeyer was awarded the Nobel Prize in chemistry in 1905.

Chemists in the late 1800s knew that cyclic molecules existed, but the limitations on ring size were unclear. Although numerous compounds containing five- and six-membered rings were known, smaller and larger ring sizes had not been prepared, despite many efforts.

A theoretical interpretation of this observation was proposed in 1885 by Adolf von Baeyer, who suggested that small and large rings might be unstable due to angle strain-the strain induced in a molecule when bond angles are forced to deviate from the ideal $109^{\circ}$ tetrahedral value. Baeyer based his suggestion on the simple geometric notion that a three-membered ring (cyclopropane) should be an equilateral triangle with bond angles of $60^{\circ}$ rather than $109^{\circ}$, a four-membered ring (cyclobutane) should be a square with bond angles of $90^{\circ}$, a five-membered ring should be a regular pentagon with bond angles of $108^{\circ}$, and so on. Continuing this argument, large rings should be strained by having bond angles that are much greater than $109^{\circ}$.


Cyclopropane


Cyclobutane


Cyclopentane


Cyclohexane

What are the facts? To measure the amount of strain in a compound, we have to measure the total energy of the compound and then subtract the energy of a strain-free reference compound. The difference between the two values should represent the amount of extra energy in the molecule due to strain. The simplest way to do this for a cycloalkane is to measure its heat of combustion, the amount of heat released when the compound burns completely with oxygen. The more energy (strain) the compound contains, the more energy (heat) is released on combustion.

$$
\left(\mathrm{CH}_{2}\right)_{n}+3 n / 2 \mathrm{O}_{2} \longrightarrow n \mathrm{CO}_{2}+n \mathrm{H}_{2} \mathrm{O}+\text { Heat }
$$

Figure 4.3 Cycloalkane strain energies, calculated by taking the difference between cycloalkane heat of combustion per $\mathrm{CH}_{2}$ and acyclic alkane heat of combustion per $\mathrm{CH}_{2}$, and multiplying by the number of $\mathrm{CH}_{2}$ units in a ring. Small and medium rings are strained, but cyclohexane rings are strain-free.

Because the heat of combustion of a cycloalkane depends on size, we need to look at heats of combustion per $\mathrm{CH}_{2}$ unit. Subtracting a reference value derived from a strain-free acyclic alkane and then multiplying by the number of $\mathrm{CH}_{2}$ units in the ring gives the overall strain energy. Figure 4.3 shows the results.


The data in Figure 4.3 show that Baeyer's theory is only partially correct. Cyclopropane and cyclobutane are indeed strained, just as predicted, but cyclopentane is more strained than predicted, and cyclohexane is strain-free. Cycloalkanes of intermediate size have only modest strain, and rings of 14 carbons or more are strain-free. Why is Baeyer's theory wrong?

Baeyer's theory is wrong for the simple reason that he assumed all cycloalkanes to be flat. In fact, as we'll see shortly, most cycloalkanes are not flat; they adopt puckered three-dimensional conformations that allow bond angles to be nearly tetrahedral. As a result, angle strain occurs only in three- and fourmembered rings that have little flexibility. For most ring sizes, particularly the medium-ring $\left(\mathrm{C}_{7}-\mathrm{C}_{11}\right)$ cycloalkanes, torsional strain caused by $\mathrm{H} \leftrightarrow \mathrm{H}$ eclipsing interactions on adjacent carbons (Section 3.6) and steric strain caused by the repulsion between nonbonded atoms that approach too closely (Section 3.7) are the most important factors. Thus, three kinds of strain contribute to the overall energy of a cycloalkane.

- Angle strain-the strain due to expansion or compression of bond angles
- Torsional strain-the strain due to eclipsing of bonds on neighboring atoms
- Steric strain-the strain due to repulsive interactions when atoms approach each other too closely

Problem 4.8 Each $\mathrm{H} \leftrightarrow$ H eclipsing interaction in ethane costs about $4.0 \mathrm{~kJ} / \mathrm{mol}$. How many such interactions are present in cyclopropane? What fraction of the overall $115 \mathrm{~kJ} / \mathrm{mol}$ ( $27.5 \mathrm{kcal} / \mathrm{mol}$ ) strain energy of cyclopropane is due to torsional strain?

Problem 4.9 cis-1,2-Dimethylcyclopropane has more strain than trans-1,2-dimethylcyclopropane. How can you account for this difference? Which of the two compounds is more stable?

### 4.4 Conformations of Cycloalkanes

## Cyclopropane

Cyclopropane is the most strained of all rings, primarily because of the angle strain caused by its $60^{\circ} \mathrm{C}-\mathrm{C}-\mathrm{C}$ bond angles. In addition, cyclopropane also has considerable torsional strain because the $\mathrm{C}-\mathrm{H}$ bonds on neighboring carbon atoms are eclipsed (Figure 4.4).

Figure 4.4 The structure of cyclopropane, showing the eclipsing of neighboring $\mathrm{C}-\mathrm{H}$ bonds that gives rise to torsional strain. Part (b) is a Newman projection along a $\mathrm{C}-\mathrm{C}$ bond.


How can the hybrid-orbital model of bonding account for the large distortion of bond angles from the normal $109^{\circ}$ tetrahedral value to $60^{\circ}$ in cyclopropane? The answer is that cyclopropane has bent bonds. In an unstrained alkane, maximum bonding is achieved when two atoms have their overlapping orbitals pointing directly toward each other. In cyclopropane, though, the orbitals can't point directly toward each other; rather, they overlap at an angle. The result is that cyclopropane bonds are weaker and more reactive than typical alkane bonds-255 kJ/mol ( $61 \mathrm{kcal} / \mathrm{mol}$ ) for a $\mathrm{C}-\mathrm{C}$ bond in cyclopropane versus $355 \mathrm{~kJ} / \mathrm{mol}(85 \mathrm{kcal} / \mathrm{mol})$ for a $\mathrm{C}-\mathrm{C}$ bond in open-chain propane.


Typical alkane C-C bonds


Typical bent cyclopropane C-C bonds

## Cyclobutane

Cyclobutane has less angle strain than cyclopropane but has more torsional strain because of its larger number of ring hydrogens. As a result, the total strain for the two compounds is nearly the same- $110 \mathrm{~kJ} / \mathrm{mol}$ ( $26.4 \mathrm{kcal} / \mathrm{mol}$ ) for cyclobutane versus $115 \mathrm{~kJ} / \mathrm{mol}$ ( $27.5 \mathrm{kcal} / \mathrm{mol}$ ) for cyclopropane. Experiments show that cyclobutane is not quite flat but is slightly bent so that one carbon atom lies about $25^{\circ}$ above the plane of the other three (Figure 4.5). The effect of
this slight bend is to increase angle strain but to decrease torsional strain, until a minimum-energy balance between the two opposing effects is achieved.


Figure 4.5 The conformation of cyclobutane. Part (c) is a Newman projection along the $\mathrm{C} 1-\mathrm{C} 2$ bond, showing that neighboring $\mathrm{C}-\mathrm{H}$ bonds are not quite eclipsed.

## Cyclopentane

Cyclopentane was predicted by Baeyer to be nearly strain-free but in fact has a total strain energy of $26 \mathrm{~kJ} / \mathrm{mol}(6.2 \mathrm{kcal} / \mathrm{mol})$. Although planar cyclopentane has practically no angle strain, it has a large amount of torsional strain. Cyclopentane therefore twists to adopt a puckered, nonplanar conformation that strikes a balance between increased angle strain and decreased torsional strain. Four of the cyclopentane carbon atoms are in approximately the same plane, with the fifth carbon atom bent out of the plane. Most of the hydrogens are nearly staggered with respect to their neighbors (Figure 4.6).
(a)

(b)

(c)


Figure 4.6 The conformation of cyclopentane. Carbons $1,2,3$, and 4 are nearly planar, but carbon 5 is out of the plane. Part (c) is a Newman projection along the C1-C2 bond, showing that neighboring $\mathrm{C}-\mathrm{H}$ bonds are nearly staggered.

Problem 4.10 How many $\mathrm{H} \longleftrightarrow$ H eclipsing interactions would be present if cyclopentane were planar? Assuming an energy cost of $4.0 \mathrm{~kJ} / \mathrm{mol}$ for each eclipsing interaction, how much torsional strain would planar cyclopentane have? Since the measured total strain of cyclopentane is $26 \mathrm{~kJ} / \mathrm{mol}$, how much of the torsional strain is relieved by puckering?

Problem 4.11 Two conformations of cis-1,3-dimethylcyclobutane are shown. What is the difference between them, and which do you think is likely to be more stable?
(a)

(b)


### 4.5 Conformations of Cyclohexane

Substituted cyclohexanes are the most common cycloalkanes and occur widely in nature. A large number of compounds, including steroids and many pharmaceutical agents, have cyclohexane rings. The flavoring agent menthol, for instance, has three substituents on a six-membered ring.


Menthol

Cyclohexane adopts a strain-free, three-dimensional shape, called a chair conformation because of its similarity to a lounge chair, with a back, a seat, and a footrest (Figure 4.7). Chair cyclohexane has neither angle strain nor torsional strain-all $\mathrm{C}-\mathrm{C}-\mathrm{C}$ bond angles are near $109^{\circ}$, and all neighboring $\mathrm{C}-\mathrm{H}$ bonds are staggered.
(a)

(b)


Observer
(c)


Figure 4.7 The strain-free chair conformation of cyclohexane. All $\mathrm{C}-\mathrm{C}-\mathrm{C}$ bond angles are $111.5^{\circ}$, close to the ideal $109.5^{\circ}$ tetrahedral angle, and all neighboring $\mathrm{C}-\mathrm{H}$ bonds are staggered.

The easiest way to visualize chair cyclohexane is to build a molecular model. (In fact, do it now.) Two-dimensional drawings like that in Figure 4.7 are useful, but there's no substitute for holding, twisting, and turning a three-dimensional model in your own hands. The chair conformation of cyclohexane can be drawn in three steps.

Step 1 Draw two parallel lines, slanted downward and slightly offset from each other. This means that four of the cyclohexane carbons lie in a plane.

Step 2 Place the topmost carbon atom above and to the right of the plane of the other four, and connect the bonds.

Step 3 Place the bottommost carbon atom below and to the left of the plane of the middle four, and connect the bonds. Note that the bonds to the bottommost carbon atom are parallel to the bonds to the topmost carbon.

|||


When viewing cyclohexane, it's helpful to remember that the lower bond is in front and the upper bond is in back. If this convention is not defined, an optical illusion can make it appear that the reverse is true. For clarity, all cyclohexane rings drawn in this book will have the front (lower) bond heavily shaded to indicate nearness to the viewer.


In addition to the chair conformation of cyclohexane, a second arrangement called the twist-boat conformation is also nearly free of angle strain. It does, however, have both steric strain and torsional strain and is about $23 \mathrm{~kJ} / \mathrm{mol}(5.5 \mathrm{kcal} / \mathrm{mol})$ higher in energy than the chair conformation. As a result, molecules adopt the twist-boat geometry only under special circumstances.



Twist-boat cyclohexane ( $23 \mathrm{~kJ} / \mathrm{mol}$ strain)

### 4.6 Axial and Equatorial Bonds in Cyclohexane

The chair conformation of cyclohexane has many consequences. We'll see in Section 11.9, for instance, that the chemical behavior of many substituted cyclohexanes is influenced by their conformation. In addition, we'll see in Section 25.5 that simple carbohydrates such as glucose adopt a conformation based on the cyclohexane chair and that their chemistry is directly affected as a result.



Cyclohexane (chair conformation)


Glucose
(chair conformation)

Another consequence of the chair conformation is that there are two kinds of positions for substituents on the cyclohexane ring: axial positions and equatorial positions (Figure 4.8). The six axial positions are perpendicular to the ring, parallel to the ring axis, and the six equatorial positions are in the rough plane of the ring, around the ring equator.

Figure 4.8 Axial (red) and equatorial (blue) positions in chair cyclohexane. The six axial hydrogens are parallel to the ring axis, and the six equatorial hydrogens are in a band around the ring equator.



As shown in Figure 4.8, each carbon atom in cyclohexane has one axial and one equatorial hydrogen. Furthermore, each face of the ring has three axial and three equatorial hydrogens in an alternating arrangement. For example, if the top face of the ring has axial hydrogens on carbons 1,3 , and 5 , then it has equatorial hydrogens on carbons 2,4 , and 6 . Exactly the reverse is true for the bottom face: carbons 1,3 , and 5 have equatorial hydrogens, but carbons 2,4 , and 6 have axial hydrogens (Figure 4.9).

Note that we haven't used the words cis and trans in this discussion of cyclohexane conformation. Two hydrogens on the same face of the ring are always cis, regardless of whether they're axial or equatorial and regardless of whether they're adjacent. Similarly, two hydrogens on opposite faces of the ring are always trans.

Figure 4.9 Alternating axial and equatorial positions in chair cyclohexane, as shown in a view looking directly down the ring axis. Each carbon atom has one axial and one equatorial position, and each face has alternating axial and equatorial positions.


Axial and equatorial bonds can be drawn following the procedure in Figure 4.10. Look at a molecular model as you practice.

Axial bonds: The six axial bonds, one on each carbon, are parallel and alternate up-down.


Equatorial bonds: The six equatorial bonds, one on each carbon, come in three sets of two parallel lines. Each set is also parallel to two ring bonds. Equatorial bonds alternate between sides around the


 ring.

## Completed cyclohexane



Figure 4.10 A procedure for drawing axial and equatorial bonds in chair cyclohexane.

Because chair cyclohexane has two kinds of positions, axial and equatorial, we might expect to find two isomeric forms of a monosubstituted cyclohexane. In fact, we don't. There is only one methylcyclohexane, one bromocyclohexane, one cyclohexanol (hydroxycyclohexane), and so on, because cyclohexane rings are conformationally mobile at room temperature. Different chair conformations readily interconvert, exchanging axial and equatorial positions. This interconversion, usually called a ring-flip, is shown in Figure 4.11.

As shown in Figure 4.11, a chair cyclohexane can be ring-flipped by keeping the middle four carbon atoms in place while folding the two end carbons in opposite directions. In so doing, an axial substituent in one chair form becomes an equatorial substituent in the ring-flipped chair form and vice versa. For example, axial bromocyclohexane becomes equatorial bromocyclohexane after ring-flip. Since the energy barrier to chair-chair interconversion is only

Figure 4.11 A ring-flip in chair cyclohexane interconverts axial and equatorial positions. What is axial (red) in the starting structure becomes equatorial in the ring-flipped structure, and what is equatorial (blue) in the starting structure is axial after ring-flip.

about $45 \mathrm{~kJ} / \mathrm{mol}(10.8 \mathrm{kcal} / \mathrm{mol})$, the process is rapid at room temperature and we see what appears to be a single structure rather than distinct axial and equatorial isomers.


WORKED EXAMPLE 4.2
Drawing the Chair Conformation of a Substituted Cyclohexane
Draw 1,1-dimethylcyclohexane in a chair conformation, indicating which methyl group in your drawing is axial and which is equatorial.

Strategy Draw a chair cyclohexane ring using the procedure in Figure 4.9, and then put two methyl groups on the same carbon. The methyl group in the rough plane of the ring is equatorial, and the other (directly above or below the ring) is axial.

## Solution



Problem 4.12

Problem 4.13

Problem 4.14

## 4.7

## Key IDEAS

Test your knowledge of Key Ideas by using resources in ThomsonNOW or by answering end-of-chapter problems marked with $A$.

Figure 4.12 A plot of the percentages of two isomers at equilibrium versus the energy difference between them. The curves are calculated using the equation $\Delta E=-R T \ln K$.

Draw two different chair conformations of cyclohexanol (hydroxycyclohexane), showing all hydrogen atoms. Identify each position as axial or equatorial.

Draw two different chair conformations of trans-1,4-dimethylcyclohexane, and label all positions as axial or equatorial.

Identify each of the colored positions-red, blue, and green-as axial or equatorial. Then carry out a ring-flip, and show the new positions occupied by each color.


## Conformations of Monosubstituted Cyclohexanes

Even though cyclohexane rings rapidly flip between chair conformations at room temperature, the two conformations of a monosubstituted cyclohexane aren't equally stable. In methylcyclohexane, for instance, the equatorial conformation is more stable than the axial conformation by $7.6 \mathrm{~kJ} / \mathrm{mol}(1.8 \mathrm{kcal} / \mathrm{mol})$. The same is true of other monosubstituted cyclohexanes: a substituent is almost always more stable in an equatorial position than in an axial position.

You might recall from your general chemistry course that it's possible to calculate the percentages of two isomers at equilibrium using the equation $\Delta E=-R T$ In $K$, where $\Delta E$ is the energy difference between isomers, $R$ is the gas constant [8.315 J/(K $\cdot \mathrm{mol})], T$ is the Kelvin temperature, and $K$ is the equilibrium constant between isomers. For example, an energy difference of $7.6 \mathrm{~kJ} / \mathrm{mol}$ means that about $95 \%$ of methylcyclohexane molecules have the methyl group equatorial at any given instant and only 5\% have the methyl group axial. Figure 4.12 plots the relationship between energy and isomer percentages.


The energy difference between axial and equatorial conformations is due to steric strain caused by 1,3-diaxial interactions. The axial methyl group on C1 is too close to the axial hydrogens three carbons away on C3 and C5, resulting in $7.6 \mathrm{~kJ} / \mathrm{mol}$ of steric strain (Figure 4.13).


Figure 4.13 Interconversion of axial and equatorial methylcyclohexane, as represented in several formats. The equatorial conformation is more stable than the axial conformation by $7.6 \mathrm{~kJ} / \mathrm{mol}$.

Figure 4.14 The origin of 1,3-diaxial interactions in methylcyclohexane. The steric strain between an axial methyl group and an axial hydrogen atom three carbons away is identical to the steric strain in gauche butane. Note that the $-\mathrm{CH}_{3}$ group in methylcyclohexane moves slightly away from a true axial position to minimize the strain.


Gauche butane ( $3.8 \mathrm{~kJ} / \mathrm{mol}$ strain)



Axial methylcyclohexane ( $7.6 \mathrm{~kJ} / \mathrm{mol}$ strain)

What is true for methylcyclohexane is also true for other monosubstituted cyclohexanes: a substituent is almost always more stable in an equatorial position than in an axial position. The exact amount of 1,3-diaxial steric strain in a given substituted cyclohexane depends on the nature and size of the substituent, as indicated in Table 4.1. Not surprisingly, the amount of steric strain increases through the series $\mathrm{H}_{3} \mathrm{C}-<\mathrm{CH}_{3} \mathrm{CH}_{2}-<\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}-\ll\left(\mathrm{CH}_{3}\right)_{3} \mathrm{C}-$, paralleling the increasing bulk of the alkyl groups. Note that the values in Table 4.1 refer to 1,3-diaxial interactions of the substituent with a single hydrogen atom. These values must be doubled to arrive at the amount of strain in a monosubstituted cyclohexane.

Table 4.1 Steric Strain in Monosubstituted Cyclohexanes


Problem 4.15 What is the energy difference between the axial and equatorial conformations of cyclohexanol (hydroxycyclohexane)?

Problem 4.16 Why do you suppose an axial cyano ( -CN ) substituent causes practically no 1,3-diaxial steric strain $(0.4 \mathrm{~kJ} / \mathrm{mol})$ ? Use molecular models to help with your answer.

Problem 4.17 Look at Figure 4.12, and estimate the percentages of axial and equatorial conformers present at equilibrium in bromocyclohexane.

### 4.8 Conformations of Disubstituted Cyclohexanes

Monosubstituted cyclohexanes are more stable with their substituent in an equatorial position, but the situation in disubstituted cyclohexanes is more complex because the steric effects of both substituents must be taken into account. All steric interactions in both possible chair conformations must be analyzed before deciding which conformation is favored.

Let's look at 1,2-dimethylcyclohexane as an example. There are two isomers, cis-1,2-dimethylcyclohexane and trans-1,2-dimethylcyclohexane, which
must be considered separately. In the cis isomer, both methyl groups are on the same face of the ring, and the compound can exist in either of the two chair conformations shown in Figure 4.15. (It may be easier for you to see whether a compound is cis- or trans-disubstituted by first drawing the ring as a flat representation and then converting to a chair conformation.) Both chair conformations have one axial methyl group and one equatorial methyl group. The top conformation in Figure 4.15 has an axial methyl group at C2, which has 1,3-diaxial interactions with hydrogens on C4 and C6. The ring-flipped conformation has an axial methyl group at C1, which has 1,3-diaxial interactions with hydrogens on C3 and C5. In addition, both conformations have gauche butane interactions between the two methyl groups. The two conformations are equal in energy, with a total steric strain of $3 \times 3.8 \mathrm{~kJ} / \mathrm{mol}=11.4 \mathrm{~kJ} / \mathrm{mol}(2.7 \mathrm{kcal} / \mathrm{mol})$.

## cis-1,2-Dimethylcyclohexane

One gauche interaction ( $3.8 \mathrm{~kJ} / \mathrm{mol}$ ) Two $\mathrm{CH}_{3} \leftrightarrow \mathrm{H}$ diaxial interactions $(7.6 \mathrm{~kJ} / \mathrm{mol})$
Total strain: $3.8+7.6=11.4 \mathrm{~kJ} / \mathrm{mol}$

One gauche interaction ( $3.8 \mathrm{~kJ} / \mathrm{mol}$ ) Two $\mathrm{CH}_{3} \leftrightarrow \mathrm{H}$ diaxial interactions $(7.6 \mathrm{~kJ} / \mathrm{mol})$
Total strain: $3.8+7.6=11.4 \mathrm{~kJ} / \mathrm{mol}$

$\|$ Ring-flip


Active Figure 4.15 Conformations of cis-1,2-dimethylcyclohexane. The two chair conformations are equal in energy because each has one axial methyl group and one equatorial methyl group. Sign in at www.thomsonedu.com to see a simulation based on this figure and to take a short quiz.

In trans-1,2-dimethylcyclohexane, the two methyl groups are on opposite faces of the ring and the compound can exist in either of the two chair conformations shown in Figure 4.16. The situation here is quite different from that of the cis isomer. The top trans conformation in Figure 4.16 has both methyl groups equatorial and therefore has only a gauche butane interaction between methyls ( $3.8 \mathrm{~kJ} / \mathrm{mol}$ ) but no 1,3-diaxial interactions. The ring-flipped conformation, however, has both methyl groups axial. The axial methyl group at C1 interacts with axial hydrogens at C3 and C5, and the axial methyl group at C2 interacts with axial hydrogens at C4 and C6. These four 1,3-diaxial interactions produce a steric strain of $4 \times 3.8 \mathrm{~kJ} / \mathrm{mol}=15.2 \mathrm{~kJ} / \mathrm{mol}$ and make the diaxial conformation $15.2-3.8=11.4 \mathrm{~kJ} / \mathrm{mol}$ less favorable than the diequatorial conformation. We therefore predict that trans-1,2-dimethylcyclohexane will exist almost exclusively in the diequatorial conformation.

ThomsonNOW Click Organic Interactive to learn to draw and assess the stability of substituted cyclohexanes.

The same kind of conformational analysis just carried out for cis- and trans-1,2-dimethylcyclohexane can be done for any substituted cyclohexane, such as cis-1-tert-butyl-4-chlorocyclohexane (see Worked Example 4.3). As you might imagine, though, the situation becomes more complex as the number of

## trans-1,2-Dimethylcyclohexane

One gauche interaction ( $3.8 \mathrm{~kJ} / \mathrm{mol}$ )

$\downarrow$ Ring-flip


Four $\mathrm{CH}_{3} \leftrightarrow \mathrm{H}$ diaxial interactions ( $15.2 \mathrm{~kJ} / \mathrm{mol}$ )

Figure 4.16 Conformations of trans-1,2-dimethylcyclohexane. The conformation with both methyl groups equatorial is favored by $11.4 \mathrm{~kJ} / \mathrm{mol}(2.7 \mathrm{kcal} / \mathrm{mol})$ over the conformation with both methyl groups axial.

ThomsonNOW Click Organic Interactive to learn to recognize the most stable conformations of cyclohexanes following ring-flips.
substituents increases. For instance, compare glucose with mannose, a carbohydrate present in seaweed. Which do you think is more strained? In glucose, all substituents on the six-membered ring are equatorial, while in mannose, one of the -OH groups is axial, making mannose more strained.
 ,
$\qquad$

Glucose



## WORKED EXAMPLE 4.3

Drawing the Most Stable Conformation of a Substituted Cyclohexane
Draw the most stable conformation of cis-1-tert-butyl-4-chlorocyclohexane. By how much is it favored?

Strategy Draw the possible conformations, and calculate the strain energy in each. Remember that equatorial substituents cause less strain than axial substituents.

Solution First draw the two chair conformations of the molecule:


In the left-hand conformation, the tert-butyl group is equatorial and the chlorine is axial. In the right-hand conformation, the tert-butyl group is axial and the chlorine is equatorial. These conformations aren't of equal energy because an axial tert-butyl substituent and an axial chloro substituent produce different amounts of steric strain. Table 4.1 shows that the 1,3-diaxial interaction between a hydrogen and a tert-butyl group costs $11.4 \mathrm{~kJ} / \mathrm{mol}(2.7 \mathrm{kcal} / \mathrm{mol})$, whereas the interaction between a hydrogen and a chlorine costs only $1.0 \mathrm{~kJ} / \mathrm{mol}$ ( $0.25 \mathrm{kcal} / \mathrm{mol}$ ). An axial tert-butyl group therefore produces $(2 \times 11.4 \mathrm{~kJ} / \mathrm{mol})-$ $(2 \times 1.0 \mathrm{~kJ} / \mathrm{mol})=20.8 \mathrm{~kJ} / \mathrm{mol}(4.9 \mathrm{kcal} / \mathrm{mol})$ more steric strain than does an axial chlorine, and the compound preferentially adopts the conformation with the chlorine axial and the tert-butyl equatorial.

Problem 4.18

Problem 4.19

Draw the most stable chair conformation of the following molecules, and estimate the amount of strain in each:
(a) trans-1-Chloro-3-methylcyclohexane
(b) cis-1-Ethyl-2-methylcyclohexane
(c) cis-1-Bromo-4-ethylcyclohexane
(d) cis-1-tert-Butyl-4-ethylcyclohexane

Identify each substituent in the following compound as axial or equatorial, and tell whether the conformation shown is the more stable or less stable chair form (yellowgreen $=\mathrm{Cl}$ ):


### 4.9 Conformations of Polycyclic Molecules

The last point we'll consider about cycloalkane stereochemistry is to see what happens when two or more cycloalkane rings are fused together along a common bond to construct a polycyclic molecule-for example, decalin.


Decalin consists of two cyclohexane rings joined to share two carbon atoms (the bridgehead carbons, C1 and C6) and a common bond. Decalin can exist in either of two isomeric forms, depending on whether the rings are trans fused or cis fused. In cis-decalin, the hydrogen atoms at the bridgehead carbons are on the same face of the rings; in trans-decalin, the bridgehead hydrogens are on opposite faces. Figure 4.17 shows how both compounds can be represented using chair cyclohexane conformations. Note that cis- and trans-decalin are not interconvertible by ring-flips or other rotations. They are cis-trans stereoisomers and have the same relationship to each other that cis- and trans-1,2-dimethylcyclohexane have.

Figure 4.17 Representations of cis- and trans-decalin. The red hydrogen atoms at the bridgehead carbons are on the same face of the rings in the cis isomer but on opposite faces in the trans isomer.


Polycyclic compounds are common in nature, and many valuable substances have fused-ring structures. For example, steroids, such as the male hormone testosterone, have 3 six-membered rings and 1 five-membered ring fused together. Although steroids look complicated compared with cyclohexane or decalin, the same principles that apply to the conformational analysis of simple cyclohexane rings apply equally well (and often better) to steroids.





Testosterone (a steroid)

Another common ring system is the norbornane, or bicyclo[2.2.1]heptane, structure. Like decalin, norbornane is a bicycloalkane, so called because two rings would have to be broken open to generate an acyclic structure. Its systematic name, bicyclo[2.2.1]heptane, reflects the fact that the molecule has seven carbons, is bicyclic, and has three "bridges" of 2,2 , and 1 carbon atoms connecting the two bridgehead carbons.


Norbornane
(bicyclo[2.2.1]heptane)


## Molecular Mechanics



All the structural models in this book are computer-drawn. To make sure they accurately portray bond angles, bond lengths, torsional interactions, and steric interactions, the most stable geometry of each molecule has been calculated on a desktop computer using a commercially available molecular mechanics program based on work by N. L. Allinger of the University of Georgia.

The idea behind molecular mechanics is to begin with a rough geometry for a molecule and then calculate a total strain energy for that starting geometry, using mathematical equations that assign values to specific kinds of molecular interactions. Bond angles that are too large or too small cause angle

Computer programs make it possible to portray accurate representations of molecular geometry. strain; bond lengths that are too short or too long cause stretching or compressing strain; unfavorable eclipsing interactions around single bonds cause torsional strain; and nonbonded atoms that approach each other too closely cause steric, or van der Waals, strain.

$$
E_{\text {total }}=E_{\text {bond stretching }}+E_{\text {angle strain }}+E_{\text {torsional strain }}+E_{\text {van der Waals }}
$$

After calculating a total strain energy for the starting geometry, the program automatically changes the geometry slightly in an attempt to lower strain-perhaps by lengthening a bond that is too short or decreasing an angle that is too large. Strain is recalculated for the new geometry, more changes are made, and more calculations are done. After dozens or hundreds of iterations, the calculation ultimately converges on a minimum energy that corresponds to the most favorable, least strained conformation of the molecule.

Molecular mechanics calculations have proved to be enormously useful in pharmaceutical research, where the complementary fit between a drug molecule and a receptor molecule in the body is often a key to designing new pharmaceutical agents (Figure 4.18).

Figure 4.18 The structure of Tamiflu (oseltamivir phosphate), an antiviral agent active against type A influenza, and a molecular model of its minimum-energy conformation, as calculated by molecular mechanics.

alicyclic, 108
angle strain, 113
axial position, 119
chair conformation, 117
cis-trans isomers, 112
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1,3-diaxial interaction, 123
equatorial position, 119
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ring-flip (cyclohexane), 120
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twist-boat conformation, 118

## SUMMMARY AND KEY WORDS

A cycloalkane is a saturated cyclic hydrocarbon with the general formula $\mathrm{C}_{n} \mathrm{H}_{2 n}$. In contrast to open-chain alkanes, where nearly free rotation occurs around $\mathrm{C}-\mathrm{C}$ bonds, rotation is greatly reduced in cycloalkanes. Disubstituted cycloalkanes can therefore exist as cis-trans isomers. The cis isomer has both substituents on the same face of the ring; the trans isomer has substituents on opposite faces. Cis-trans isomers are just one kind of stereoisomers-isomers that have the same connections between atoms but different three-dimensional arrangements.

Not all cycloalkanes are equally stable. Three kinds of strain contribute to the overall energy of a cycloalkane: (1) angle strain is the resistance of a bond angle to compression or expansion from the normal $109^{\circ}$ tetrahedral value, (2) torsional strain is the energy cost of having neighboring $\mathrm{C}-\mathrm{H}$ bonds eclipsed rather than staggered, and (3) steric strain is the repulsive interaction that arises when two groups attempt to occupy the same space.

Cyclopropane ( $115 \mathrm{~kJ} / \mathrm{mol}$ strain) and cyclobutane ( $110.4 \mathrm{~kJ} / \mathrm{mol}$ strain) have both angle strain and torsional strain. Cyclopentane is free of angle strain but has a substantial torsional strain due to its large number of eclipsing interactions. Both cyclobutane and cyclopentane pucker slightly away from planarity to relieve torsional strain.

Cyclohexane is strain-free because it adopts a puckered chair conformation, in which all bond angles are near $109^{\circ}$ and all neighboring $\mathrm{C}-\mathrm{H}$ bonds are staggered. Chair cyclohexane has two kinds of positions: axial and equatorial. Axial positions are oriented up and down, parallel to the ring axis, whereas equatorial positions lie in a belt around the equator of the ring. Each carbon atom has one axial and one equatorial position.

Chair cyclohexanes are conformationally mobile and can undergo a ring-flip, which interconverts axial and equatorial positions. Substituents on the ring are more stable in the equatorial position because axial substituents cause 1,3-diaxial interactions. The amount of 1,3-diaxial steric strain caused by an axial substituent depends on its bulk.

## EXERCISES

## $\overline{\text { Organic }}$ KNOWLEDGE TOOLS

ThomsonNow Sign in at www.thomsonedu.com to assess your knowledge of this chapter's topics by taking a pre-test. The pre-test will link you to interactive organic chemistry resources based on your score in each concept area.
On Online homework for this chapter may be assigned in Organic OWL.

- indicates problems assignable in Organic OWL.

A denotes problems linked to Key Ideas of this chapter and testable in ThomsonNOW.

## VISUALIZING CHEMISTRY

(Problems 4.1-4.20 appear within the chapter.)
4.21 Name the following cycloalkanes:

4.22 Name the following compound, identify each substituent as axial or equatorial, and tell whether the conformation shown is the more stable or less stable chair form (yellow-green $=\mathrm{Cl}$ ):

$4.23 \Delta$ A trisubstituted cyclohexane with three substituents-red, yellow, and blue-undergoes a ring-flip to its alternative chair conformation. Identify each substituent as axial or equatorial, and show the positions occupied by the three substituents in the ring-flipped form.

4.24 Glucose exists in two forms having a 36:64 ratio at equilibrium. Draw a skeletal structure of each, describe the difference between them, and tell which of the two you think is more stable (red $=0$ ):

$\alpha$-Glucose

$\beta$-Glucose

## ADDITIONAL PROBLEMS

4.25 Draw the five cycloalkanes with the formula $\mathrm{C}_{5} \mathrm{H}_{10}$.
4.26 Draw two constitutional isomers of cis-1,2-dibromocyclopentane.
4.27 Draw a stereoisomer of trans-1,3-dimethylcyclobutane.
4.28 Hydrocortisone, a naturally occurring hormone produced in the adrenal glands, is often used to treat inflammation, severe allergies, and numerous other conditions. Is the indicated -OH group in the molecule axial or equatorial?


Hydrocortisone
4.29 A 1,2-cis disubstituted cyclohexane, such as cis-1,2-dichlorocyclohexane, must have one group axial and one group equatorial. Explain.
4.30 A 1,2-trans disubstituted cyclohexane must have either both groups axial or both groups equatorial. Explain.
4.31 Why is a 1,3 -cis disubstituted cyclohexane more stable than its trans isomer?
4.32 Which is more stable, a 1,4-trans disubstituted cyclohexane or its cis isomer?
4.33 cis-1,2-Dimethylcyclobutane is less stable than its trans isomer, but cis-1,3dimethylcyclobutane is more stable than its trans isomer. Draw the most stable conformations of both, and explain.
4.34 Draw the two chair conformations of cis-1-chloro-2-methylcyclohexane. Which is more stable, and by how much?
4.35 Draw the two chair conformations of trans-1-chloro-2-methylcyclohexane. Which is more stable?
4.36 흔 Galactose, a sugar related to glucose, contains a six-membered ring in which all the substituents except the -OH group indicated below in red are equatorial. Draw galactose in its more stable chair conformation.


Galactose
4.37 Draw the two chair conformations of menthol, and tell which is more stable.


Menthol
4.38 There are four cis-trans isomers of menthol (Problem 4.37), including the one shown. Draw the other three.
4.39 Identify each pair of relationships among the - OH groups in glucose (red-blue, red-green, red-black, blue-green, blue-black, green-black) as cis or trans.


Glucose
$4.40 \Delta$ Draw 1,3,5-trimethylcyclohexane using a hexagon to represent the ring. How many cis-trans stereoisomers are possible?
4.41 From the data in Figure 4.12 and Table 4.1, estimate the percentages of molecules that have their substituents in an axial orientation for the following compounds:
(a) Isopropylcyclohexane
(b) Fluorocyclohexane
(c) Cyclohexanecarbonitrile, $\mathrm{C}_{6} \mathrm{H}_{11} \mathrm{CN}$
4.42 Assume that you have a variety of cyclohexanes substituted in the positions indicated. Identify the substituents as either axial or equatorial. For example, a 1,2-cis relationship means that one substituent must be axial and one equatorial, whereas a 1,2-trans relationship means that both substituents are axial or both are equatorial.
(a) 1,3-Trans disubstituted
(b) 1,4-Cis disubstituted
(c) 1,3-Cis disubstituted
(d) 1,5-Trans disubstituted
(e) 1,5-Cis disubstituted
(f) 1,6-Trans disubstituted
4.43 A The diaxial conformation of cis-1,3-dimethylcyclohexane is approximately $23 \mathrm{~kJ} / \mathrm{mol}(5.4 \mathrm{kcal} / \mathrm{mol})$ less stable than the diequatorial conformation. Draw the two possible chair conformations, and suggest a reason for the large energy difference.
4.44 Approximately how much steric strain does the 1,3-diaxial interaction between the two methyl groups introduce into the diaxial conformation of cis-1,3-dimethylcyclohexane? (See Problem 4.43.)
4.45 In light of your answer to Problem 4.44, draw the two chair conformations of 1,1,3-trimethylcyclohexane, and estimate the amount of strain energy in each. Which conformation is favored?
4.46 We saw in Problem 4.20 that cis-decalin is less stable than trans-decalin. Assume that the 1,3-diaxial interactions in trans-decalin are similar to those in axial methylcyclohexane [that is, one $\mathrm{CH}_{2} \longleftrightarrow \mathrm{H}$ interaction costs $3.8 \mathrm{~kJ} / \mathrm{mol}$ $(0.9 \mathrm{kcal} / \mathrm{mol})]$, and calculate the magnitude of the energy difference between cis- and trans-decalin.
4.47 Using molecular models as well as structural drawings, explain why transdecalin is rigid and cannot ring-flip, whereas cis-decalin can easily ring-flip.
4.48 trans-Decalin is more stable than its cis isomer, but cis-bicyclo[4.1.0]heptane is more stable than its trans isomer. Explain.

trans-Decalin

cis-Bicyclo[4.1.0]heptane
$4.49 \Delta$ myo-Inositol, one of the isomers of 1,2,3,4,5,6-hexahydroxycyclohexane, acts as a growth factor in both animals and microorganisms. Draw the most stable chair conformation of myo-inositol.

myo-Inositol
4.50 How many cis-trans stereoisomers of myo-inositol (Problem 4.49) are there? Draw the structure of the most stable isomer.
4.51 One of the two chair structures of cis-1-chloro-3-methylcyclohexane is more stable than the other by $15.5 \mathrm{~kJ} / \mathrm{mol}(3.7 \mathrm{kcal} / \mathrm{mol})$. Which is it? What is the energy cost of a 1,3-diaxial interaction between a chlorine and a methyl group?
4.52 The German chemist J. Bredt proposed in 1935 that bicycloalkenes such as 1 -norbornene, which have a double bond to the bridgehead carbon, are too strained to exist. Make a molecular model of 1-norbornene, and explain Bredt's proposal.


## 1-Norbornene

4.53 Tell whether each of the following substituents on a steroid is axial or equatorial. (A substituent that is "up" is on the top face of the molecule as drawn, and a substituent that is "down" is on the bottom face.)
(a) Substituent up at C3
(b) Substituent down at C 7
(c) Substituent down at C11

4.54 Amantadine is an antiviral agent that is active against influenza A infection and against some strains of H5N1 avian flu. Draw a three-dimensional representation of amantadine showing the chair cyclohexane rings.


Amantadine
4.55 Ketones react with alcohols to yield products called acetals. Why does the allcis isomer of 4-tert-butyl-1,3-cyclohexanediol react readily with acetone and an acid catalyst to form an acetal while other stereoisomers do not react? In formulating your answer, draw the more stable chair conformations of all four stereoisomers and the product acetal. Use molecular models for help.




An acetal
4.56 Alcohols undergo an oxidation reaction to yield carbonyl compounds on treatment with $\mathrm{CrO}_{3}$. For example, 2-tert-butylcyclohexanol gives 2-tert-butylcyclohexanone. If axial -OH groups are generally more reactive than their equatorial isomers, which do you think would react faster, the cis isomer of 2-tert-butylcyclohexanol or the trans isomer? Explain.


2-tert-Butylcyclohexanol
2-tert-Butylcyclohexanone

