## SECTION 3

## Newton's Second Law: Push or Pull

## Section Overview

Students observe how acceleration is directly proportional to the force applied and inversely proportional to an object's mass. By applying a variable force to small and large masses, they obtain a kinesthetic feel for Newton's second law. The Physics Talk explains and defines Newton's second law. The use of the newton as a derived unit is emphasized by analyzing the equation for Newton's second law of motion. Students read about the importance of units and significant figures in measurements. Students explore applications of Newton's second law, particularly the force of gravity as a special case. Additionally, they explore scalar and vector quantities, and add forces acting in different directions to measure the resulting unbalanced force. Particular attention is given to the theory and application of significant figures when making experimental calculations.

## Background Information

The unit of mass, or quantity of matter, in the International System of Units is the kilogram. One of seven base units from which all other units are derived, the kilogram originally was conceived as the quantity of matter represented by 1 L of water at the temperature of maximum density, $4^{\circ} \mathrm{C}$. Today, the kilogram is defined by a carefully protected metal standard called the International Prototype Kilogram. When a balance which employs the force of gravity is used to measure the mass of an object by comparison to prototype masses, the resulting measurement is known as the "gravitational mass" of the object. Mass is also internationally recognized as a measure of the inertial resistance of an object to acceleration. When a standard force is used to compare an object's acceleration to the acceleration of a prototype mass as a means of measuring the
mass of the object, the resulting measurement is known as the "inertial mass" of the object.

Extremely accurate measurements indicate that 1 kg of gravitationally determined mass is equivalent to 1 kg of inertial mass. A derived unit of force, the newton, is defined in terms of base units of mass, length, and time using Newton's second law of motion, $F=m a$. One newton is the force which will cause one kilogram to accelerate at one meter per second squared, or $1 \mathrm{~N}=1 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}$. The word "weight" denotes a force; the weight of an object is the product of its mass and a proportionality constant for objects on the surface of the Earth, $9.81 \mathrm{~N} / \mathrm{kg}$. Because weight is the force due to gravity, weight is measured in newtons. 1 N is roughly $1 / 4 \mathrm{lb}$, prompting the identification of the familiar $1 / 4 \mathrm{lb}$-burger as a "newton burger."

In summary, matter seems to have two distinct properties: it exhibits a resistance to acceleration (a property called "inertia") and it has the property of gravitation, which means that matter is attracted to other matter. All objects, no matter what their mass, have the same free-fall acceleration at a given location. The more mass, the more gravitational force; but the more mass, the more difficult it is to accelerate the object. These two factors exactly compensate to produce the same acceleration for every freely falling object at a given location. This acceleration is equal to the proportionality constant, $9.81 \mathrm{~N} / \mathrm{kg}$ or $9.81 \mathrm{~m} / \mathrm{s}^{2}$, which is why this constant is often called "the acceleration due to gravity." By emphasizing that weight is equal to the mass times the proper proportionality constant, it will be easier for students to understand that the value of the proportionality constant depends on, for example, whether you are on Earth or the Moon. The acceleration of free-falling objects therefore also depends on whether you are on Earth or the Moon. Students who simply think of $9.81 \mathrm{~m} / \mathrm{s}^{2}$ as
the acceleration due to gravity have little basis for understanding why this number is different on Earth
and the Moon, because in their minds gravity is involved in both cases.

## Crucial Physics

- Forces are "pushes" or "pulls" on an object. Forces on an object add as vectors and it is the total force or net force that determines the acceleration of the object.
- The total or net force on an object is related to its mass and acceleration by Newton's second law, $F=m a$.
- Weight is the force due to gravity on an object and is proportional to the object's mass. On the surface of Earth, the proportionality constant $g=9.81 \mathrm{~N} / \mathrm{kg}$, so $W=m g$.
- By Newton's second law, the acceleration of an object when the only force acting on it is gravity is $g=9.81 \mathrm{~N} / \mathrm{kg}=9.81 \mathrm{~m} / \mathrm{s}^{2}$.
- Active Physics Plus: Forces add as vectors.

| Learning Outcomes | Location in the Section | Evidence of Understanding |
| :--- | :--- | :--- |
| Identify the forces on an object. | Investigate, Physics Talk <br> Steps 6-9 | Students analyze the Investigate to identify forces on an <br> object and learn the definition of a force. |
| Determine when the forces on <br> an object are either balanced or <br> unbalanced. | Investigate, Physics Talk <br> Steps 7-9 | Students keep adding coins to the end of a ruler and learn <br> how an unbalanced force causes the ruler to bend and the <br> coins to drop. |
| Compare amounts of <br> acceleration semi-quantitatively. | Physics Talk, Physics to Go | Students solve problems to compare how the amount of <br> force applied affects acceleration. |
| Apply the definition of the <br> newton as a unit of force. | Physics Talk, Physics to Go <br> Questions 3, 4, and 10-17 | Students write the equivalent form of a newton and solve <br> problems of acceleration and force using the newton as a <br> unit of force. |
| Describe weight as the force due <br> to gravity on an object. | Physics Talk | Students recall the experiment of the ruler and coins in the <br> Investigate to describe weight. |

## Section 3 Materials, Preparation, and Safety

Materials and Equipment

| Materials and Equipment | Group <br> (4 students) | Class |
| :--- | ---: | :--- |
| Ruler, plastic, flexible, 30 cm | 1 per group |  |
| Cart, dynamics | 1 per group |  |
| Weights, slotted, set | 1 per group |  |
| C-clamp, steel, 3 in. | 1 per group |  |
| Tape, masking, 3/4 in. x 60 yds |  | 6 per class |
| Access to a flat surface (such as a <br> table, floor or other open space)* | 1 per group |  |
| Can or bottle (with less mass then <br> the dynamics cart)* | 1 per group |  |
| Coins (pennies, nickels)* | 5 per group |  |

*Additional items needed not supplied

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| :--- | ---: | :--- |
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| Coins (pennies, nickels)* | 5 per group |  |

*Additional items needed not supplied
Note: Time, Preparation, and Safety requirements are based on Plan A, if using Plan B, please adjust accordingly.

## Time Requirement

To complete this requirement, one class period or 40 minutes are required.

## Teacher Preparation

For best results, this Investigate should be done on a clear area of open floor.

Try to push the cart or can yourself with the ruler to maintain a constant force (bend of the ruler) to get a feel for how difficult this will be for the students. The students will often just give the cart a push to get it going over a short distance rather than chasing after the cart to maintain the force.

The students should discover that they must run faster and faster to keep up with the cart and maintain the same bend of the ruler. The chase is very important because it best demonstrates the acceleration that is taking place. If a large frictional force is present that causes the carts to travel with constant speed with the ruler bent, have the students use the bend of a large ruler until the cart or can accelerates.

If you are using carts, it is helpful if the cart has some additional mass on it for the first trial. When a "smaller" mass is required, mass may be removed from the cart, and later may be added to increase the cart's mass.

## Safety Requirements

Make certain that the area where the students will be pushing the carts is free from any obstructions.

Lab partners should watch for any potential problems where the students are pushing the carts so that the students my concentrate on keeping the ruler bent as they chase the cart.

Students should pick up the carts or cans from the floor and place them in a safe location immediately after finishing pushing to prevent anyone from slipping on them.

## Meeting the Needs of All Students Differentiated Instruction: Augmentation and Accommodations

| Learning Issue | Reference | Augmentation and Accommodations |
| :---: | :---: | :---: |
| Describing motion qualitatively | Investigate <br> Steps 2-5 | Augmentation <br> - Assist students in brainstorming a list of words that could be used to describe motion (fast, slow, moderate speed, speeding up, slowing down, forward, etc.). |
| Creating a data table | Investigate <br> Step 5 | Augmentation <br> - Some students may struggle to create a table that includes all of the required information without seeing a sample. Tell students to decide in groups what kind of information needs to be recorded (object's name, relative mass, and motion). Then ask them how many columns and rows are needed. <br> - Tell students to draw two vertical lines to divide their page into three equal sections. Remind them to record descriptions in the appropriate mass and motion columns, and ask them to make each row a few lines in height. <br> - Pair the oral directions with a visual model of the data table. <br> Accommodation <br> - Give students a blank table to tape into their logs and complete. |
| Understanding qualitative vs. quantitative data | Investigate | Augmentation <br> - Ask students if they know the meaning of quantity. Make an explicit connection between the words quantity and quantitative. Then ask students to help you create a list of quantities students can measure. Repeat this activity with quality and qualitative. |
| Understanding concepts of direct and inverse proportion | Physics Talk <br> Physics Essential Questions | Augmentation <br> - Students with reading-comprehension issues may not understand the written explanation. Show the students the relationship in a visual model while explaining the concept orally. Give clear and explicit explanations as in the examples below. <br> - As force increases ( $F \Uparrow$ ), what happens to the acceleration? <br> Acceleration increases ( $a \Uparrow$ ). This is a direct proportion. <br> - This relationship can also be represented visually by increasing the font size of the variables. $(F \Rightarrow F) \text { causes }(a \Rightarrow a)$ <br> - As mass increases ( $m \Uparrow$ ), what happens to acceleration? Acceleration decreases ( $a \Downarrow$ ). This is an inverse proportion. <br> - Provide direct instruction to draw the connection between these relationships to explain $a=F / m$. |
| Using the helpful circle | Physics Talk | Augmentation <br> - Students may have forgotten how to use the helpful circle introduced in Chapter 1. Provide direct instruction and opportunities for guided practice to use/review the helpful circle. |
| Understanding key concepts | Physics Talk | Augmentation <br> - Students with reading-comprehension issues may pass over the key concepts in this section. Students need to know that there are many kinds of forces and that unbalanced forces cause acceleration. <br> - Ask students to brainstorm a list of forces with a partner. Then combine these lists into a class list. This Investigate will activate prior knowledge and also show the teacher if there are any misconceptions about kinds of forces. <br> - Ask students if they can think of an example in which unbalanced forces cause acceleration. |


| Learning Issue | Reference | Augmentation and Accommodations |
| :--- | :--- | :--- |
| $\begin{array}{l}\text { Understanding the } \\ \text { difference between } \\ \text { mass and weight }\end{array}$ | $\begin{array}{l}\text { Physics Talk } \\ \text { Inquiring Further }\end{array}$ | $\begin{array}{l}\text { Augmentation } \\ \text { - The average person in society uses mass and weight interchangeably. These } \\ \text { concepts can be very confusing. Ask students if they know the difference between } \\ \text { mass and weight. Use adequate wait time to give everyone time to think about } \\ \text { the answer. } \\ \text { - Provide direct instruction to explain the difference. Give an example of the weight } \\ \text { of a 1-kg mass on Earth versus the weight of a 1-kg mass on the Moon. }\end{array}$ |
| $\begin{array}{l}\text { Solving word } \\ \text { problems }\end{array}$ | $\begin{array}{l}\text { Physics to Go } \\ \text { Questions 3-7, 15 }\end{array}$ | $\begin{array}{l}\text { Augmentation } \\ \text { - Students with reading-comprehension, sequential, and executive-function issues } \\ \text { may struggle to extract information from a word problem and follow the steps } \\ \text { necessary to solve the problem. }\end{array}$ |
| - Provide direct instruction to teach key words found in word problems, such as what |  |  |
| is, how much, calculate, solve for, etc. |  |  |
| - Model a think-aloud to make explicit the mental steps a good problem-solver takes |  |  |
| to solve a problem. Pair the think-aloud with visual cues that show each step. |  |  |$\}$| Accommodation |
| :--- |
| - Provide students with a sheet of blank problem-solving boxes. |

## Strategies for Students with Limited English-Language Proficiency

| Learning Issue | Reference |  |
| :--- | :--- | :--- |
| Following complex <br> procedures | Investigate | Break down the Investigate into smaller chunks that allow students to comprehend <br> each portion of the experiment before moving on to the next one. This approach <br> will allow students to get comfortable following the procedures outlined within each <br> step, and also to internalize the new concepts that are introduced. Lead a brief class <br> discussion after each step to allow students the opportunity to demonstrate acquired <br> knowledge and understanding. |
| Understanding <br> concepts | Investigate <br> Qualitative and <br> Quantitative <br> Observations | It is vital in science that students understand the difference between the similar words <br> "qualitative" and "quantitative." Tell students that qualitative observations discuss <br> the quality of an object by using adjectives to describe the object: green, rough, loud. <br> Quantitative observations involve quantities, or amounts, and often (but not always) <br> are represented with numbers: 89 kg, 47"C, 5.3 m/s. |
| Vocabulary <br> comprehension | Physics Talk | To help all students, especially kinesthetic learners, understand that a force is a <br> push or a pull, and to help ELL students learn the meanings of "push" and "pull," <br> demonstrate the movements of push and pull with your hands and then have |
| students make the movements with you. |  |  |

# SECTION 3 <br> Teaching Suggestions and Sample Answers 

## What Do You See?

Here is yet another skilled representation of how the net force on an object is directly proportional to its acceleration. The three contrasting visuals of the girl pushing the ball with a stick are meant to evoke a response to the different predicaments faced by the girl. Consider asking your students why the girl appears to be so relaxed at first, then puzzled, and eventually so exhausted. Write down responses on the board and highlight key words and phrases that will be used later in the section to develop concepts. Ask questions that initiate a discussion on force and acceleration. This
is the time that students might reveal prior misconceptions. Each idea that students present is significant. Keep encouraging them as they discuss the illustration. Emphasize that they will be returning to the What Do You See? illustration to discuss how earlier responses get altered with a better understanding of the artist's purpose in relating the physics of a section.

## What Do You Think?

## The What Do You Think?

 questions are designed to stimulate thinking about the section. Have students share their answers and accept all answers without correction. Encourage them to think of a time when they went bowling or played tennis. Prompt them to think of how a tennis ball is different from a bowling ball in terms of weight. Consider asking them if they can think of how weight and applied force are related. Remind them that they will be returning to these questions later in the sectionafter they have explored the concepts of force and acceleration in relation to weight.

## What Do You Think?

A Physicist's Response
In simple terms, a force is a push or a pull. Some forces, such as gravitational and magnetic forces, can act on objects without having to be in contact with them. Many other forces, called mechanical forces, act when particles or objects touch each other. Forces are very important in physics because they determine how matter interacts with other matter.

The same force could be used to move both a bowling ball and a soccer ball, or even a table-tennis ball, as long as there is not much friction or other counteracting forces to interfere. The difference would be the amount by which each is accelerated by the force. The greater the mass, the lesser the acceleration experienced by an object when the same force is applied to it. Mass affects acceleration.

## Students' Prior Conceptions

Students recognize that a force is a push or a pull. Forces have both magnitude and direction. When the forces acting on an object are unbalanced in one direction the object moves, either with acceleration or with steady motion, if the force applied equals the force of static friction. Students should grasp the meaning of Newton's second law to establish their foundation for the application of the laws of motion to all subsequent sections in the chapter. Some preconceptions are listed below:

1. If an object is at rest, no forces are acting on the object. It is necessary for students to identify all forces acting on an object so that they recognize balanced and unbalanced forces. Often, students overlook the forces acting in the vertical direction, for example, gravity pulling down on an object while the floor, chair, or
table push up on the same object. Students might only consider the forces acting in the horizontal direction to affect motion in that direction.
2. Only animate objects can exert a force. Students have difficulty recognizing that all interactions involve equal forces acting in opposite directions on the separate interacting bodies. Thus, if an object is at rest on a table, students often say that there are no forces acting upon the object. Students need to identify all of the forces acting on an object, name the forces, discuss their directions, and identify their magnitudes, even if only relative to each other. Recognizing the nature of balanced and unbalanced forces acting on objects is paramount to learning how to apply Newton's second law to the interactions and motions of objects.


## Investigate

## 1.

Explain to the students that the ruler is behaving much like a spring. The bend of the ruler is indicative of the amount of force being applied in the same manner as the stretch of a spring indicates the amount of force. Although this force meter is not calibrated, the students will only be using it to obtain qualitative data on acceleration under an applied force.
3. Force is a property of an object rather than a relation between objects. Students may believe that an object has force and when the force runs out the object stops moving. Focus student attention on the concept of inertial mass to recognize that matter moves or stays at rest depending upon the nature of the balanced or unbalanced forces acting upon the object with that amount of matter. More matter requires a larger force to give the same type of motion.
4. Large objects exert a greater force than small objects. Students need to understand that force is defined as the product of a mass with its acceleration. A large mass can have a small acceleration and a small force whereas a small mass can have a large acceleration and therefore a large force. The equal nature of pairs of forces in interactions is considered in subsequent activities.
5. Gravity is a property of an object rather than a force experienced by the object; weight is not a force-rather, the air exerts the force; gravity requires a medium to act through; weight is something that can be "felt"; if an object has no weight then it cannot be "felt"; and mass may not be differentiated from weight. It is important for students to explore the relationship between mass and weight to recognize that weight is the product of the mass of an object and the acceleration due to the pull of Earth or another larger object or celestial body on an object.

These prior conceptions emerge in subsequent activities, too, as students apply the laws of motion to falling objects.
2.

The students will have to accelerate as they chase the accelerating cart to maintain a constant bend in the ruler (a constant accelerating force).

## 2.a)

The students should indicate that the cart continually increases in speed as the force is applied. To make the acceleration more obvious to the students, have them apply the force to the cart while it is on the floor, so that the force can be maintained for a longer distance than a lab table, and the students will have to chase after the cart.

## Teaching Tip

Try out the acceleration yourself first to determine if the students will have difficulty keeping up with the accelerating cart. If you determine that your carts accelerate too quickly for the students to effectively maintain a constant force, add mass to the cart to slow down the acceleration in these initial steps. Mass will also be added later to show the effect of increasing mass. If masses are added, they can be removed for Step 4 to simplify that step.

The students should find they have difficulty keeping up with the cart, trying to maintain the constant larger bend in the ruler, as it accelerates at a greater rate.

## 3.a)

The cart accelerated in both trials.

## 3.b)

The students should note that the cart accelerates at a greater rate with a larger bend in the ruler (as it produces a larger force) than

a smaller bend that produces a smaller force.

## 3.c)

The acceleration was greater in the second trial.

## 3.d)

"The greater the constant force pushing on an object, the greater the object's acceleration."

If the students used carts with masses for Step 2, they could remove
the masses for this step. Otherwise use a smaller mass cart or object.

## 4.a)

The students should note that the large force on the smaller mass will give an acceleration greater than the previous trial with a large force.

## 5.a)

The students will see that as the mass becomes larger using the same force, the acceleration of the object will decrease.


## 5.b)

"When equal amounts of a constant force are used to push objects having different masses, the more massive object the less the acceleration of that object."

## 6.

The results of the student's experiments are the essence of Newton's second law.

## 6.a)

Pushing on a large object with a small force would have produced a small acceleration, and pushing on a small object with a large force would have produced a very large acceleration. The results of these two experiments might have led the students to the correct conclusion about the relationship between force and acceleration. However, they might equally conclude that large forces always
mean large accelerations, and small forces always mean small accelerations, regardless of mass. If the experiment had been a large force on a large mass and a small force on a small mass, the conclusion would have been that all masses accelerate at the same rate!

## 7.

The ruler should be clamped with most of the ruler hanging over the edge of the table.

The coin may need a small piece of tape on the side touching the ruler to keep it from sliding off the ruler.

## 8.a)

The ruler bends under the weight of the coin.

## 9.a)

As more coins are added, the bend of the ruler increases.

## 9.b)

One or two coins would represent a small force, while four coins represent a large force.

## 9.c)

In this case it is the weight of the coins causing the bend, rather than the force applied by the hand. You might want to point out to the students that equal bends in the ruler imply that equal forces are needed.

## Physics Talk

This Physics Talk explores Newton's second law of motion qualitatively as well as quantitatively. It would be useful to the students to make connections with the different steps in their Investigate and see how each step can be explained through their reading of the Pbysics Talk. To check for student understanding, have students summarize the findings of their Investigate as evidence for Newton's second law. Emphasize that an unbalanced force is needed for an object to accelerate, and that although a force may be acting, if it is not unbalanced, the object will not accelerate. In addition, point out that the force of gravity or weight is really only a special case of Newton's second law, where it is the ratio of force to mass that gives the constant acceleration we call " $g$." As students learn about force, make sure they also understand the meaning of derived units. You might want to ask them where they have used these before. You could also ask them to write and discuss the units of force and weight and illustrate Newton's second law with diagrams. While students are working through the sample problems, have them discuss the solution of each problem with their peers. To verify whether students are comfortable determining significant figures in a measurement, ask them to give a few examples of significant figures in their logs. Doing several sample calculations using measurements with different numbers of

significant figures will improve their understanding of the role of significant figures in science.

## An Equation for Newton's Second Law of Motion

Newton's second law can be written as an equation:

$$
\begin{aligned}
\text { Acceleration } & =\frac{\text { force }}{\text { mass }} \\
a & =\frac{F}{m}
\end{aligned}
$$

where $a$ is acceleration expressed in meters per second squared $\left(\mathrm{m} / \mathrm{s}^{2}\right)$,
$F$ is force expressed in newtons ( N ), and $m$ is mass expressed in kilograms (kg).
With a bit of algebra, Newton's second law can be arranged so that it is easier to find the unknown quantity of $F, m$, or $a$.

$$
a=\frac{F}{m} \quad F=m a \quad m=\frac{F}{a}
$$

Some students like to use a helpful circle:


If you want to find:

- force, $F$, cover it up and you see $m$ next to $a$ (or $F=m \times a$ ).
- acceleration, a, cover it up and you see $F$ over $m$ (or $a=F \div m$ ).
- mass, $m$, cover it up and you see $F$ over $a$ (or $m=F \div a$ ).

Newton: A Derived SI Unit with a Special Name
When you measured speed and acceleration, you used derived units with compound names. You measured speed in meters per second with compound names. You measured speed in meters per second
(symbol, $\mathrm{m} / \mathrm{s}$ ) and acceleration in meters per second per second, (symbol, $\mathrm{m} / \mathrm{s}$ ) and acceleration in meters per second per second,
or meters per second squared (symbol, ( $\mathrm{m} / \mathrm{s} / \mathrm{s}$ or $\mathrm{m} / \mathrm{s}^{2}$ ). These are or meters per second squared ( $\mathrm{symbol},\left(\mathrm{m} / \mathrm{s}\right.$ )/s or $\mathrm{m} / \mathrm{s}^{2}$ ). These are
derived units. They are made up of one or more base SI units.
In the equation for Newton's second law, force is expressed
in newtons (symbol, N). What is a newton? A newton is a derived SI unit with a special name. A newton is the force required to make one kilogram of mass accelerate at one meter per second squared.

With this definition, the unit newton can be written in its equivalent form: $1 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}$.

$$
1 \mathrm{~N}=1 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}
$$

Knowing the equivalent form for a newton will be important when using Newton's second law to do calculations to find mass and acceleration. Mathematically, the dot represents multiplication.

$$
1 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2} \text { means } 1 \mathrm{~kg} \times \frac{\mathrm{m}}{\mathrm{~s}^{2}} \text { or } 1 \mathrm{~kg} \times \frac{\mathrm{m}}{\mathrm{~s} \times \mathrm{s}}
$$

Where There's Acceleration, There Must Be an Unbalanced Force
There are lots of different everyday forces. There is the force of the bent ruler in this investigation. There is also the force of a spring, the force of a rubber band, the force of a magnet, the force of your hand, the force of a bat hitting a ball, the force of friction, the buoyant force of water, and many more. Newton's second law tells you that accelerations are caused by
unbalanced forces. It does not matter what kind of force it is or how it originates. If you observe an acceleration (a change in velocity), then originates. If you observe an acceleration (a change in velocity), then there must be an unbalanced force causing the acceleration. When you
apply a force to an object that has a small mass, the acceleration may be apply a force to an object that has a small mass, the acceleration may be
quite large. If the object has a large mass, the acceleration will be smaller quite large. If the object has a large mass, the acceleration will be smal measure the acceleration because it is so small.
If you push on a small cart with the largest force you can, the cart will accelerate a great deal. If you push on a car with that same force, the acceleration will be much smaller. If you were to push on a truck, the acceleration would be too small to measure. Can you convince someone acceleration would be too small to measure. Can you convince someo
that a push on a truck accelerates the truck? Why should you believe that a push on a truck accelerates the truck? Why should you believe
something that you cannot measure? If you were to assume that the something that you cannot measure? If you were to assume that the
truck does not accelerate when you push on it, then you would have truck does not accelerate when you push on it, then you would have
to believe that Newton's second law stops working when the mass gets to believe that Newton's second law stops working when the mass gets
too big. If that were so, you would want to determine how big is "too too big. If that were so, you would want to determine how big is "too
big." When you conduct such experiments, you find that the acceleration gets less and less as the mass gets larger and larger. Eventually, the acceleration gets so small that it is difficult to measure. Your inability to measure it does not mean that it is zero. It just means that it is smaller than your best measurement. In this way, you can assume that Newton's second law is always valid.

Calculations Using Newton's Second Law of Motion
Since Newton's second law relates force, mass, and acceleration, you can use the equations for Newton's second law to solve a variety of problems.
Sample Problem I
As the result of a serve, a tennis ball ( $m_{\mathrm{t}}=58 \mathrm{~g}$ ) accelerates at $430 \mathrm{~m} / \mathrm{s}^{2}$ for the very brief time it is in contact with the racket.
a) What force is responsible for this acceleration?
b) Could an identical force accelerate a 5.0 -kg bowling ball at the same rate?

Strategy: Newton's second law states that the acceleration of an object is directly proportional to the applied force and inversely proportional to the mass $(F=m a)$.

Given:
$a=430 \mathrm{~m} / \mathrm{s}^{2}$
$m_{\mathrm{t}}=58 \mathrm{~g}=0.058 \mathrm{~kg}$
$m_{\mathrm{b}}=5.0 \mathrm{~kg}$

## Solution:

a) $F=m_{t} a$
$=(0.058 \mathrm{~kg})\left(430 \mathrm{~m} / \mathrm{s}^{2}\right)$
$=24.94 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}$ or $25 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}$
$=25 \mathrm{~N}$
Recall that $1 \mathrm{~N}=1 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}$
b) Since the mass of the bowling ball has a much greater mass than the tennis ball, an identical force will result in a smaller acceleration. (You can calculate the acceleration.)

$$
\begin{aligned}
a & =\frac{F}{m_{b}} \\
& =\frac{25 \mathrm{~N}}{5.0 \mathrm{~kg}} \\
& =\frac{25 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2}}{5.0 \mathrm{~kg}}
\end{aligned}
$$

$$
=0.5 \mathrm{~m} / \mathrm{s}^{2}
$$

This is much smaller than the acceleration of the tennis ball.
Calculations and Units

In physics, when you do calculations, it is very important to pay close attention to the units in your answer. Notice how in the calculation above you can write the unit N as $\mathrm{kg} \cdot \mathrm{m} / \mathrm{s}^{2}$. Then the units kg in the top and bottom of the equation cancel out, leaving $\mathrm{m} / \mathrm{s}^{2}$, the unit for acceleration that you need for your answer.


## Determining the Number of Significant Figures in a Measurement

There are guidelines that you can use to determine the number of significant figures in a measurement.

All nonzero numbers are considered to be significant figures. In the measurement 152.5 m , all the digits are significant. The measurement has four significant figures.
Zeros may or may not be significant, depending on their place in a number.

- A zero between nonzero digits is a significant figure. In the measurement 308 g , the zero is significant. The measurement has three significant figures.
- A zero at the end of a decimal number is considered significant. In the measurement 1.50 N , the zero is significant. The measurement has three significant figures.
- A zero at the beginning of a decimal number is not significant. In the measurement 0.023 kg , the zeros are not significant. The measurement has two significant figures.
- In a large number without a decimal point, the zeros are not significant. In the measurement 2000 kg , the zeros are not significant. The measurement has one significant figure.


## Significant Figures in Calculations

There are also guidelines that you can use when making your calculations.
Adding and Subtracting
When adding or subtracting, the final result should have the same number of decimal places as the measurement with the fewest decimal places.
Multiplying and Dividing
When multiplying or dividing, the result should have no more significant digits than the factor having the fewest number of significant digits.



## Checking Up

## 1.

When an unbalanced force acts on an object, the acceleration of the object is directly proportional to the magnitude of the force and occurs in the same direction that force was applied.

## 2.

For a constant force, increasing the mass of an object will reduce its acceleration.

## 3.

The statement means that there will be a force of 30 N acting downward on the mass due to force of Earth's gravity.

## 4.

Your weight would increase while your mass would remain the same.

## Active Physics Plus

Encourage your students to draw vectors showing the direction of unbalanced forces. Having them define scalar and vector quantities in their logs will help reinforce their learning. To provide a visual focus, drawing examples of vectors on the board will help students to see how two forces create a net resultant force.

Chapter 2 Physics in Action

| +Math | +Depth | +Concepts | +Exploration | Active Physics |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $* *$ | $\bullet$ |  |  |  |  |

## Adding Vectors

Many of the numbers you use every day are scalars. Scalars are numbers defining quantities that do not have any specific direction associated with them. They only have sizes or magnitudes. Some example of scalars include temperature, prices, time, mass, lengths, and widths.
Unlike a scalar quantity, a vector is a quantity that has both magnitude and direction. The velocity of an object is a vector. Its magnitude is the speed of the object and its direction is the direction the object is moving.
Force is also a vector because you can measure how big it is (its magnitude) and its direction. Acceleration is also a vector. Newton's second law reminds you that the force and the acceleration must be in the same direction. Mass is not a vector - it has no direction associated with it, so it is a scalar. Weight, however, is a force and does have direction associated with it. All forces are vectors. The direction of the weight vector is down (toward the center of Earth).
Often, more than one force acts on an object. If the two forces are in the same direction, the sum of the forces is simply the algebraic addition of the two forces. A $30-\mathrm{N}$ force by one person and a force of 40 N by a second person (pushing in the same direction) on the same desk provide a $70-\mathrm{N}$ force on the same desk provide a $70-\mathrm{N}$ force on the
desk. If the two forces are in opposite desk. If the two forces are in opposite
directions, then you give one of the forces directions, then you give one of the forces
a negative value and one a positive value a negative value and one a positive value
to show that they act opposite to each other. Then you add them algebraically.

If one student pushes on a desk to the right with a force of 30 N and a second student pushes on the same desk to the left with a force of 40 N , the net force on the desk (also called the total force or the unbalanced force) will be 10 N to the left. Mathematically, you would state that $30 \mathrm{~N}+(-40 \mathrm{~N})=-10 \mathrm{~N}$ where the negative sign denotes "to the left." Choosing left as the negative direction is an arbitrary choice.
Occasionally, the two forces acting on an object are at right angles. For instance, one student may be kicking a soccer ball with a force of 30 N ahead toward the goal, while the second student kicks the same soccer ball with a force of 40 N toward the sideline. To find the net force on the ball and the direction the ball accelerates, you must use vector addition. You can do this by using a vector diagram or the Pythagorean theorem.
In the actual situation shown on the next page, the two force vectors are shown as arrows acting on the soccer ball. The magnitudes of the vectors are drawn to scale. If you were to draw this using the scale that $10 \mathrm{~N}=1.0 \mathrm{~cm}$, then the $30-\mathrm{N}$ force would be 3.0 cm long and the $40-\mathrm{N}$ force would be 4.0 cm long. To add the vectors, slide them so that the tip of the $30-\mathrm{N}$ vector can be placed next to the tail of the $40-\mathrm{N}$ vector (tip to tail method).

## Active Physics

## 168

The sum of the two vectors is then drawn from the tail of the $30-\mathrm{N}$ vector to the tip of the $40-\mathrm{N}$ vector as shown in the vector diagram below. This resultant vector is measured and is found to be 5.0 cm , which is equivalent to 50 N . The angle is measured with a protractor and is found to be $53^{\circ}$.

A second method of finding the resultant vector is to recognize that the $30-\mathrm{N}$ and $40-\mathrm{N}$ force vectors form a right triangle. The resultant is the hypotenuse of this triangle. Its length can be found using the Pythagorean theorem.

$$
a^{2}+b^{2}=c^{2}
$$

$(30 \mathrm{~N})^{2}+(40 \mathrm{~N})^{2}=c^{2}$
$900 \mathrm{~N}^{2}+1600 \mathrm{~N}^{2}=c^{2}$
$2500 \mathrm{~N}^{2}=c^{2}$

$$
c=\sqrt{2500 \mathrm{~N}^{2}}
$$

$$
c=50 \mathrm{~N}
$$

The angle can be found by using the tangent function.
$\begin{aligned} \tan \theta & =\frac{\text { opposite }}{\text { adjacent }}=\frac{40 \mathrm{~N}}{30 \mathrm{~N}}=1.33 \\ \theta & =53^{\circ}\end{aligned}$
Adding vector forces that are not perpendicular is a bit more difficult mathematically, but you can use scale drawings to make vector diagrams. Two other players are kicking a soccer ball in the directions shown in the top right diagram. The resultant vector force can be determined using the tip-to-tail approach.


The two arrows in the left diagram correspond to the actual situation in which two players kick the ball at different angles. The vector diagram at the right shows the two vectors being added "tip to tail." The resultant vector (shown as a dotted line) represents the net force and is the direction of the acceleration of the soccer ball.

1. One player applies a force of 125 N north on a soccer ball. Another player pushes with a force of 125 N west on the ball. What is the magnitude and direction of the resultant force?
2. Three hockey players are fighting for a loose puck. Hockey player A exerts a force of 40 N due north on the puck while player B exerts a force of 70 N due south. Player C exerts a force of 40 N due west. The forces are shown in the diagram below.

a) What is the resultant force exerted by players A and B on the hockey puck?
b) What is the resultant force of all three players on the hockey puck? c) What is the direction of the net force on the puck?

## 1.

Given:
$a=b=125 \mathrm{~N}$

## Solution:

Using the Pythagorean theorem, the resultant would be determined by the formula
$a^{2}+b^{2}=c^{2}$
$(125 \mathrm{~N})^{2}+(125 \mathrm{~N})^{2}=c^{2}$
$c=\sqrt{(125 \mathrm{~N})^{2}+(125 \mathrm{~N})^{2}}=177 \mathrm{~N}$
To find the direction use tan
$\theta=$ opposite $/$ adjacent $=$
$(125 \mathrm{~N}) /(125 \mathrm{~N})=1^{\circ}$
$\theta=45^{\circ}$ North of West

## 2.a)

Adding the two opposite vertical forces
$40 \mathrm{~N}+(-70 \mathrm{~N})=-30 \mathrm{~N}$

## 30 N downward or South

## 2.b)

$F_{\text {vertical }}=-30 \mathrm{~N}$
$F_{\text {horizontal }}=-40 \mathrm{~N}$
Using the Pythagorean theorem, the resultant force would be determined by the formula
$F_{\text {resultant }}=\sqrt{\left(F_{\text {vertical }}\right)^{2}+\left(F_{\text {horizontal }}\right)^{2}}=$ $\sqrt{(-30 \mathrm{~N})^{2}+(-40 \mathrm{~N})^{2}}=50 \mathrm{~N}$

## 2.c)

To find the direction use $\tan$
$\theta=\left(\frac{F_{\text {vertical }}}{F_{\text {horizontal }}}\right)=\tan ^{-1}\left(\frac{-30 \mathrm{~N}}{-40 \mathrm{~N}}\right)=37^{\circ}$
$37^{\circ}$ South of West

## What Do You Think Now?

Most students will by now have an understanding of Newton's second law and should be well equipped to answer the What Do You Think Now? questions with ease. As you discuss their responses, make sure that they have a good understanding of Newton's second law. You might want to touch on certain aspects of the Investigate and Physics Talk. Recalling previous learning should help them see why it essential for them to revisit questions asked in What Do You See?

Chapter 2 Physics in Action

What Do You Think Now?
At the beginning of this section, you were asked the following:

- What is a force?
- How will the same amount of force affect a tennis ball and a bowling ball differently?
In the Investigate, you changed the force with which you pushed a mass, and the size of the mass you pushed. How would you answer these questions now?


## Physics <br> Essential Questions

What does it mean?
What does it mean when Newton's second law states that acceleration and mass are inversely proportional?
How do you know?
What part of your investigation shows you that stronger forces cause larger accelerations?
Why do you believe?

| Connects with Other Physics Content | Fits with Big Ideass in Science | Meets Physics Requirements |
| :--- | :--- | :--- |
| Force and motion | * Change and constancy | Good, cleas explanation, no more complex <br> than necessay |

* Newton's second law is used to describe and explain motion of large objects and small objects. It helps you better understand the motion of people in sports, cells in the body, colliding atoms, and planets in the Solar System. Entire physics courses in college are based on Newton's second law. Why do you believe that if you push on a truck, the truck has a tiny acceleration?
Why should you care?
All sports involve motion. All accelerated motion involves unbalanced forces. If you identify an acceleration of a person or an object in your sports video, you can discuss the forces that cause that acceleration. What is one way that this idea will come up in your voice-over challenge?


## Physics Essential Questions

## What does it mean?

If the same force pushed a series of masses, the larger masses would have the smallest accelerations. This is an inverse proportion.

## How do you know?

By applying a larger force (more bend in the ruler), you can observe a greater change in speed in a given time interval.

## Why do you believe?

Newton's second law states that if the push is the only force acting on the truck, then the truck would have a very tiny acceleration. To assume that there would be no acceleration would require us to then find out why Newton's second law does not apply for either small forces or large masses. It makes more sense to conclude the acceleration is too small to see.

## Why should you care?

A baseball leaving the bat has acceleration. Newton's second law states that if there is acceleration, there must be a force. The force is the bat on the ball.


| Newton's second law | F $\quad$ m | a |  |
| :--- | :--- | :--- | :---: |
| sprinter beginning 100-meter dash | 350 N | 70 kg | $5 \mathrm{~m} / \mathrm{s}^{2}$ |
| long jumper in flight | 800 N | 80 kg | $10 \mathrm{~m} / \mathrm{s}$ |
| shot-put ball in flight | 70 N | 7 kg | $10 \mathrm{~m} / \mathrm{s}^{2}$ |
| ski jumper going down hill before jumping | 400 N | 80 kg | $5 \mathrm{~m} / \mathrm{s}^{2}$ |
| hockey player "shaving ice" while stopping | -1500 N | 100 kg | $-15 \mathrm{~m} / \mathrm{s}^{2}$ |
| running back being tackled | -3000 N | 100 kg | $-30 \mathrm{~m} / \mathrm{s}^{2}$ |

## Reflecting on the Section and the Challenge

Students should read this section so that they can begin to form specific connections with the Chapter Challenge. A discussion of different sports, especially the ones mentioned in the Reflecting on the Section and the Challenge, will help students to see how Newton's second law affects the decisions that are made by players. You might want to provide some time for your students to read this section aloud.

## Physics to Go

## 1.

See chart below.

## 2.a)

The long jump and the shot put are both cases of free fall; therefore the acceleration is $g$, the acceleration due to gravity.

## 2.b)

The negative sign is used to denote that the force and acceleration are in a direction opposite the motion.

## 2.c)

Because acceleration occurs in the direction of the causal force, yes, the force should be shown as negative.
3.
$42 \mathrm{~N} / 0.30 \mathrm{~kg}=140 \mathrm{~m} / \mathrm{s}^{2}$
4.
$0.040 \mathrm{~kg} \times 20 \mathrm{~m} / \mathrm{s}^{2}=0.8 \mathrm{~N}$

## 5.a)

A bowling ball has greater inertia (mass) than a baseball; therefore, a bowling ball has a greater tendency to either remain at rest or remain in motion than does a baseball.

## 5.b)

More force is required to cause a bowling ball to accelerate than a baseball; therefore, throwing (accelerating) or catching (decelerating) a bowling ball involves much greater forces than throwing or catching a baseball when equal speeds are involved.

## 6.

The sandwich would weigh $0.1 \mathrm{~kg} \times 10 \mathrm{~m} / \mathrm{s}^{2}=1 \mathrm{~N}$. Names such as "newtonburger" might work.

## 7.a)

Example:
Weight $=150 \mathrm{lb} \times 4.38 \mathrm{~N} / \mathrm{lb}=$ 657 N

## 7.b)

Mass $=657 \mathrm{~N} / 10 \mathrm{~m} / \mathrm{s}^{2}=65.7 \mathrm{~kg}$
8.

Students provide voice-over for tug of war.

## 9.

No. The force of your hand stops acting on the ball the moment the two are no longer in contact.
3. What is the acceleration of a $0.30-\mathrm{kg}$ volleyball when a player uses a force of 42 N to spike the ball?
4. What force would be needed to accelerate a $0.040-\mathrm{kg}$ golf ball at $20.0 \mathrm{~m} / \mathrm{s}^{2}$ ?
5. Most people can throw a baseball farther than a bowling ball, and most people would find it less painful to catch a flying baseball than a bowling ball flying at the same speed as the baseball. Explain these two situations in terms of a) Newton's first law of motion. b) Newton's second law of motion.
6. Calculate the weight of a new fast-food sandwich that has a mass of 0.1 kg (approximately the mass of a quarter pound). Think of a clever name for the sandwich that would incorporate its weight in newtons.
7. In the United States, people measure body weight in pounds. Imagine a person weighs 150 lb .
a) Convert the person's weight in pounds to the international unit of force, newtons. To do so, use the following conversion equation:
Weight in newtons $=$ (weight in pounds) ( 4.38 newtons per pound)
b) Use the person's body weight, in newtons, and the equation

Weight $=m g$
to calculate the person's body mass ( $m$ ), in kilograms.
8. If you were doing the voice-over for a tug-of-war competition, how would you explain what was happening? Write a few sentences as if you were the science narrator of that athletic event.
9. You throw a ball. When the ball is many meters away from you, is the force of your hand still acting on the ball? When does the force of your hand stop acting on the ball?
10. Carlo and Sara push on a desk in the same direction. Sara pushes with a force of 50 N , and Carlo pushes with a force of 40 N . What is the unbalanced force acting on the desk? The unbalanced force on an object is sometimes called the total force, or net force, on an object.
11. A vehicle is stuck in the mud. Four adults each push on the back of the vehicle with a force of 200 N . What is the combined force, due to all four adults, on the vehicle?
12. A baseball player throws a ball. While the $700.0-\mathrm{g}$ ball is in the pitcher's hand, there is a force of 125 N on it. What is the acceleration of the ball?
13. During a football game, two players try to tackle another player. One player applies a force of 50.0 N to the east. A second player applies a force of 120.0 N to the north. What is the resultant force applied to the player being tackled? (Since force is a vector, you must give both the magnitude and direction of the force.)

## 72

## 10. <br> 0.

The resultant is
$40 \mathrm{~N}+50 \mathrm{~N}=90 \mathrm{~N}$.
11.

The total or combined force is $4 \times 200 \mathrm{~N}=800 \mathrm{~N}$. But there may also be forces due to the mud, acting in the opposite direction.
12.
$F=m a$
$a=F / m=(125 \mathrm{~N}) /(0.7 \mathrm{~kg})=$
$179 \mathrm{~m} / \mathrm{s}^{2}$
13.

Application of the Pythagorean theorem yields:
$(50 \mathrm{~N})^{2}+(120 \mathrm{~N})^{2}=F^{2}$
$F=130 \mathrm{~N}$
Using the tangent button on the calculator or a vector diagram, the angle is $23^{\circ}$ East of North.


## 14.

Application of the Pythagorean theorem yields:
$(4000 \mathrm{~N})^{2}+(5000 \mathrm{~N})^{2}=F^{2}$
$F=6403 \mathrm{~N}$
Using the tangent button on the calculator or a vector diagram, the angle is $39^{\circ}$.
15.
$F=m a=(12.8 \mathrm{~kg})\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)=$ 125 N
16.b)
$a=F / m=50 \mathrm{~N} / 5.6 \mathrm{~kg}=8.9 \mathrm{~m} / \mathrm{s}^{2}$

## 17.a)

Application of the Pythagorean theorem yields:
$(30 \mathrm{~N})^{2}+(20 \mathrm{~N})^{2}=F^{2}$
$F=\sqrt{(30 \mathrm{~N})^{2}+(20 \mathrm{~N})^{2}}=36 \mathrm{~N}$
Using the tangent button on the calculator or a vector diagram, the angle is $34^{\circ}$.

## 17.b)

$a=F / m=36 \mathrm{~N} / 100 \mathrm{~kg}=$
$0.36 \mathrm{~N} / \mathrm{kg}=0.36 \mathrm{~m} / \mathrm{s}^{2}$

## 17.c)

If both boxes were pushed toward the right, the new force would be 50 N .
(30 N + $20 \mathrm{~N}=50 \mathrm{~N}$ )
The acceleration can then be calculated:
$a=F / m=50 \mathrm{~N} / 100 \mathrm{~kg}=$
$0.5 \mathrm{~N} / \mathrm{kg}=0.5 \mathrm{~m} / \mathrm{s}^{2}$

## 18.

## Preparing for the Chapter Challenge

Student responses will vary, but should include a description of how Newton's second law will determine the acceleration of an object that is acted upon by one or more forces. The forces should be appropriate for the sports example being illustrated.

## Inquiring Further

Because your weight depends upon your mass times the acceleration of gravity, the best place to go to "lose weight" would be the planet with the lowest gravity. Unfortunately, although you would weigh less, your mass would still be the same so you would not look appreciably different.

The acceleration of gravity on the Moon is approximately $1.6 \mathrm{~m} / \mathrm{s}^{2}$ or about one-sixth that of Earth. If you went to the Moon, your new weight
would be one-sixth your weight on Earth. A person who weighed 150 lbs on Earth would only weigh 25 lbs on the Moon!

The acceleration of gravity varies greatly from planet to planet, with a high of about $26 \mathrm{~m} / \mathrm{s}^{2}$ for Jupiter, and a low of $0.6 \mathrm{~m} / \mathrm{s}^{2}$ for Pluto. The weight of a $60-\mathrm{kg}$ person would vary from

1560 N (about 350 lbs ) on Jupiter to 36 N (about 8 lbs ) on Pluto.

## NOTES

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## SECTION 3 QUIZ

## 2-3b Blackline Master

1. The force required to accelerate a $2-\mathrm{kg}$ mass at $4 \mathrm{~m} / \mathrm{s}^{2}$ is
a) 6 N .
b) 2 N .
c) 8 N .
d) 16 N .
2. A force of $F$ newtons will give an object with a mass of $M$ an acceleration of $A$. The same force will give a mass of 2 M an acceleration of
a) $\mathrm{A} / 2$.
b) 2 A .
c) A.
d) $\mathrm{A} / 4$.
3. On the planet Gamma a $4.0-\mathrm{kg}$ mass experiences a gravitational force of 24 N . What is the acceleration due to gravity on Gamma?
a) $0.17 \mathrm{~m} / \mathrm{s}^{2}$
b) $6 \mathrm{~m} / \mathrm{s}^{2}$
c) $9.8 \mathrm{~m} / \mathrm{s}^{2}$
d) $96 \mathrm{~m} / \mathrm{s}^{2}$
4. A cart is uniformly accelerating from rest. The force on the cart must be
a) decreasing.
b) zero.
c) constant.
d) increasing.
5. In the graph below, the acceleration of an object is plotted against the unbalanced force applied. What is the mass of the object?

a) 0.5 kg
b) 2 kg
c) 4 kg
d) 0.2 kg

## SECTION 3 QUIZ ANSWERS

(1) b) Using $F=m a=(2 \mathrm{~kg})\left(4 \mathrm{~m} / \mathrm{s}^{2}\right)=8 \mathrm{~N}$.
(2) a) $a=F / M$, then $F / 2 M=\frac{1}{2} A$
(3) b) Using $W=m g$ gives $24 \mathrm{~N}=(4 \mathrm{~kg})(g)$ Solving for $g=6 \mathrm{~m} / \mathrm{s}^{2}$.
(4) c) A constant acceleration requires a constant net force.
(5) a) Using values from the graph, when the force is 4 N , the acceleration is $8 \mathrm{~m} / \mathrm{s}^{2}$. Substituting these values in the equation $F=m a$ yields $4 \mathrm{~N}=m\left(8 \mathrm{~m} / \mathrm{s}^{2}\right)$, or $m=0.5 \mathrm{~kg}$.
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