## SECTION 9

## Conservation of Energy: Defy Gravity

## Section Overview

By calculating an athlete's time in air, called "hang time," students find out if the skater or basketball player at any point is able to counter the effect of gravity by hanging in the air. They watch a video of the skater doing a triple-axle jump, both in slow motion and at normal speed, and multiply the number of frames (pictures completed every $1 / 30$ s) by the time the skater remains in air. Students then locate their center of mass to make a better estimate of how high they are able to jump. They jump as high as they can to calculate and record the vertical height through which their center of mass shifts during the jump. They use the concepts of work, spring potential energy (SPE), gravitational potential energy (GPE), and kinetic energy ( $K E$ ) to help them analyze the energy transformations that take place during the jump. The students measure the position of their center of mass at the ready, launch, and peak positions and use these values along with their mass and the acceleration of gravity to calculate the energy forms at the various positions. Using the principle of conservation of energy, the students create a chart to compares value of the energies at the three different positions, as well as the sum of the GPE, SPE, and $K E$ at these positions.

## Background Information

Read the Physics Talk in the student text for this section before proceeding. Energy is simply stored work, and work is transformed into kinetic energy and gravitational potential energy in a vertical jump. Research has shown that the location of the center of mass within the jumper's body varies only slightly for the body positions assumed during the process of the vertical jump. The force that lifts and accelerates the body's center of mass
during a vertical jump is provided by muscles of the leg, ankles, and feet. The method of analysis used for this activity assumes that the muscular force is constant as the body rises from "ready" to "launch" positions. This is not entirely accurate-in a real jump, the force varies-but is a reasonable approximation of reality.

The center of mass of an object is the only idea introduced in this section. The center of mass is the point at which the entire mass of an object may be thought of as being concentrated for purposes of analyzing the translational (along a path) or rotational (spinning) motion of the object. For practical purposes, the location of the center of mass of an object having only one significant dimension-such as a straight stick, loaded teetertotter, twirler's baton, screwdriver, or wrenchcorresponds to the object's balance point. For a two-dimensional object-such as a sheet of plywood cut into any shape-the location of the center of mass corresponds to the balance point located on either of the two large, flat surfaces of the object. To the extent that a two-dimensional object-such as a triangle cut from a sheet of plywood-may have significant thickness and, therefore, actually be three-dimensional, the center of mass would be located within the object, "in line" with the balance point, at the center of the thick dimension. For objects with simple three-dimensional shapes-such as homogeneous or symmetrically layered spheres such as bowling balls, basketballs, cubes, rectangular solids and cylinders-the center of mass is located within the center. An alternative to balancing an object to locate the center of mass is to suspend the object from any point that is not the center of mass. When suspended, gravity serves to orient the object so that its center of mass is located directly below the point of suspension. Earth "views" an object near it as a "point mass" (located at the object's center of
mass) and pulls the point mass as close to Earth as possible. A line extended straight downward from the point of suspension passes through the object's
center of mass. The intersection of two such lines, corresponding to two points of suspension, locates the object's center of mass.

## Crucial Physics

- The center of mass of an object is the point that moves due to forces on the object as if all the mass of the object were located at that point.
- Energy is "stored work" and energy comes in different forms.
- Energy is conserved when there are no outside forces acting on the objects under consideration.

| Learning Outcomes | Location in the Section | Evidence of Understanding |
| :--- | :--- | :--- |
| Measure changes in height of <br> the body's center of mass during <br> a vertical jump. | Investigate <br> Steps 4-6 | Students record the height in meters of their body's <br> distance from its center of mass to the floor at three <br> different positions of their vertical jump. |
| Calculate changes in the <br> gravitational potential energy of <br> the body's center of mass during <br> a vertical jump. | Investigate <br> Step 6 | Students record the distance from the floor to their center <br> of mass at the "peak position." Then they subtract the <br> height at the peak of the jump height from the launch <br> height. |
| Apply the definition of work. | Investigate <br> Steps 3 and 5 <br> Physics Talk | Students' work, which is required to lift themselves from <br> the ready to the launch position, is their weight times the <br> change in height. |
| Recognize how work is related <br> to energy. | Investigate <br> Steps 5 and 6 <br> Physics Talk | Students do work with their leg muscles to provide the <br> energy of the jump that is converted into kinetic energy. |
| Apply the joule as a unit of work <br> and conservation of energy to <br> the analysis of a vertical jump, <br> including weight, force, height, <br> and time of flight. | Investigate <br> Step 7 <br> Physics Talk | Students use the same units for all measures of energy and <br> work in their calculations of the energy transformations <br> between work, SPE, GPE, and KE during the jump. |
| Describe the concepts of work <br> and conservation of energy to <br> the analysis of a vertical jump, <br> including weight, force, height, <br> and time of flight | Physics Talk | Students read the Physics Talk and learn about <br> conservation of energy based on tables providing a <br> breakdown of total energy. |

## Section 9 Materials, Preparation, and Safety

Materials and Equipment

| Materials and Equipment | Group <br> (4 students) | Class |
| :--- | :---: | :---: |
| Meter stick, wood | 2 per group |  |

*Additional items needed not supplied

| Materials and Equipment | Group <br> (4 students) | Class |
| :--- | :--- | :--- |
| Meter stick, wood |  | 2 per class |
| Calculator, basic | 1 per group | 6 per class |
| Tape, masking, 3/4 in. $\times 60$ yds |  | 1 per class |
| MBL or CBL Technology (to record <br> probeware activity* |  | 1 per class |
| Probeware, motion detector* |  | 1 per class |
| Scale, bathroom* |  | 1 per class |
| TV with VCR* |  |  |

*Additional items needed not supplied
Note: Time, Preparation, and Safety requirements are based on Plan A, if using Plan B, please adjust accordingly.

## Time Requirement

This Investigate should take at least one class period or 40 minutes.

## Teacher Preparation

- Obtain a TV and VCR (or DVD player) that has single-frame advance capability to show the students stop-frame video of an athlete jumping. Have a common bathroom scale available for students to determine their mass, but place it in a location in the classroom where students can obtain their mass privately.
- Set up a motion detector, computer, and interface if available. Attach the motion detector to the classroom ceiling so the students can jump underneath it to measure their jump height.


## Safety Requirements

Students who do not wish to jump should not be forced to do so. Check with the school nurse to see if any students might have physical limitations that would preclude their jumping in class.

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## Meeting the Needs of All Students

## Differentiated Instruction: Augmentation and Accommodations

| Learning Issue | Reference | Augmentation and Accommodations |
| :---: | :---: | :---: |
| Understanding vocabulary | What Do You Think? <br> Investigate Steps 1.c) and 2 Physics to Go Step 2 | Augmentation <br> - Explain the meaning of "defy" and provide examples. <br> Accommodation <br> - Show a video clip of a bobsled team in action before students are asked to answer this question because they may have no idea what bobsledding means. |
| Visual perception and attention | Investigate <br> Steps 1.a) and 2.a) | Augmentation <br> - Ask students to count the individual frames in the video for the figure skater and basketball player. <br> - Students with vision issues could be assigned to record the class data on the board and help do the hang time calculations. |
| Scientific measurement | Investigate <br> Step 4 | Augmentation <br> - Students struggle with metric conversions. Tell them to find the vertical distance in centimeters. Then show them how to do the conversion. <br> - Students often leave out decimal points and do not understand the importance of decimals in determining the value of numbers. Teach this concept in the context of money ( $\$ 0.50$ versus $\$ 50.00$ ). |
| Measuring "peak position" | Investigate <br> Step 6 | Augmentation <br> - Teach strategies for marking "peak position" and then measuring it. For example, make one group member responsible for being the height-marker of the "peak position." Then have a pair of students measure the distance from the floor to the peak position. <br> - Students could also jump near the blackboard and mark the peak position with chalk before measuring. |
| Recording data for calculations | Investigate <br> Steps 3-8 | Augmentation <br> - To help students record data accurately, model how to set up a table or record sheet before beginning the Investigate. <br> Accommodation <br> - Provide a blank copy of a data table for students to tape into their logs. |
| Creating a chart to understand an essential concept | Investigate <br> Step 7.d) | Augmentation <br> - Model and ask students to turn their paper to landscape format to create any tables/charts that are larger than four columns. This will accommodate students with large handwriting and fine-motor issues. <br> - Ask students to first draw the template of a table based on the teacher's sample. The table should fill most of the page. <br> - If students are using lined paper, they can use the vertical lines on the paper to space out their columns (about five lines per column). Encourage them to quickly draw the appropriate number of rows. <br> - Make sure students include a column for total energy. <br> Accommodation <br> - Provide a blank chart for students to tape into their logs and record the values. |


| Learning Issue | Reference | Augmentation and Accommodations |
| :--- | :--- | :--- |
| Understanding the <br> conservation of <br> energy principle | Physics Talk | Augmentation <br> - Students struggle to conceptualize energy transfer and conservation because they <br> cannot see the energy changing from one form to another. Also, the most common <br> way for students to understand this principle is to compare the total energy of a <br> system before and after the transfer of energy. Show students that the total energy <br> of a system is always conserved. <br> - Ask pairs of students to make drawings to represent the energy transfers involved <br> when a person jumps. Students could use the values presented in the tables in this <br> section to mathematically support their sketches. <br> Accommodation <br> $\bullet$ Provide a teacher-made worksheet or sketch of a person jumping on which students <br> can add "types of energy" labels or "number of joules" labels. |
| Solving multi-step <br> problems and <br> using more than <br> one formula in an <br> assignment | Physics Talk <br> Physics to Go | Accommodation <br> - Provide opportunities to practice individual formulas for mastery before combining <br> concepts into one multi-step problem that requires the use of a few different <br> formulas and concepts. |
| Solving for velocity <br> using the $K E$ formula | Physics Talk <br> Sample Problem d) | Augmentation <br> -Students struggle to understand the concept of square root and square root <br> functions. Provide direct instruction in how to solve for velocity using the $K E$ <br> formula. Make sure that students understand that $v^{2}$ means $v$ multiplied by $v$. |
| Accommodation |  |  |
| - Some students may not be developmentally or academically prepared at this time to |  |  |
| solve for velocity using the $K E$ formula. |  |  |

## Strategies for Students with Limited English-Language Proficiency

| Learning Issue | Reference |  |
| :--- | :--- | :--- |
| Vocabulary <br> comprehension | What Do You <br> Think? | Given the "Defy Gravity" focus of this section, it is essential that all students <br> understand the concept of hang time. Hang time is how long an athlete stays in <br> the air after jumping. Some athletes stay in the air so long they appear to defy, or <br> overcome, gravity. |
| Understanding <br> scientific concepts | Physics Essential <br> Questions | Students likely think of a theory as a guess or an assumption based on little <br> understanding or information. But the word "theory" has a different meaning in <br> science. A theory, in science, is an organized body of knowledge known to accurately <br> predict and explain a specific set of phenomena in the natural world. The law of <br> conservation of energy is a scientific theory that has stood the test of time. Remind <br> students of the definition of "model" from Section 5: A model is anything that <br> accurately represents what we know about how the natural world behaves. A theory <br> is just as much a model as a mathematical model or a physical model. |

Two important aspects of learning a new language are speaking and writing in that language. Some ELL students will be self-conscious and shy about speaking in front of their peers, while others will be less reluctant to try. Be sure to encourage all ELL students to speak in class, and give them
opportunities to write on the board from time to time. Experience will broaden their comfort level. Over time, the shy students will get increasingly less self-conscious about speaking in front of their classmates.

## SECTION 9 Teaching Suggestions and Sample Answers

## What Do You See?

There are many points of interest that your students are most likely to bring up when they are asked to discuss the illustration. Each image provides a focus that relates to the main topic. Consider various aspects of students' responses and encourage them to articulate their thoughts without hesitation. The What Do You See? stage provides the centerpiece on which you can build the rest of your students' understanding.


## Students' Prior Conceptions

The concepts of force, motion of the center of mass of an object, free fall, weight, work, energy, and conservation of energy culminate to perplex students as they master the concepts building throughout the activities in this chapter. It is essential for students to explain the concepts in their own words and for teachers to listen to and probe student understanding so that the preconceptions listed in Sections $1-8$ are not overlooked. Explaining work, identifying the forces involved, examining weight and the center of mass, and considering the height of the vertical jump along with the time of the flight all act to perplex students in their
analysis of the conservation of energy during a vertical jump. It is vital for the teacher to recognize students' preconceptions that continue to hinder understanding in order to help compare prior conceptions with observable behavior in order to prevent many misconceptions.

## What Do You Think?

While recording their ideas, some students might ask you what hang time means. Instead of being locked down in a question and answer session, gently remind them that their task for the What Do You Think? questions is to record their answers in their Active Physics logs. Ask them to ponder what they already know and how they can respond to these questions. You might want to emphasize that the main purpose of this task is to stimulate their scientific thinking to prepare them for the inquiry-driven approach followed in Active Physics.

## What Do You Think?

## A Physicist's Response

No, the hang time does not defy the pull of gravity. Hang time is mere illusion. The pull of gravity continues to act, but this cannot be detected because the people's eyes cannot detect the rapid movement that happens in the flash of a second.

The world-class figure skater cannot defy gravity long enough to do a triple-axle. Each turn brings him very slightly toward the ground.

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## Investigate

## 1.a)

The skater is in the air for 15 frames.

## 1.b)

Time in air $(s)=$ Number of Frames $(15)(1 / 30 \mathrm{~s})=\frac{1}{2} \mathrm{~s}$

## 1.c)

During the time frame viewed on the video, the skater's position is constantly changing. Although there is no hang time, the vertical change in position at the peak is at its slowest, giving the impression of a hang time. If students continue to say they
observe hang time, ask them for a suitable definition of hang time. If they come up with a useable definition, they should not be able to observe it in the video.
2.a)

The basketball player is in the air for 31 frames.


Time in air $(\mathrm{s})=$ Number of Frames
$(31)(1 / 30 \mathrm{~s})=31 / 30 \mathrm{~s}=$
$1 \frac{1}{30} \mathrm{~s}=1.03 \mathrm{~s}$

## 2.b)

During the time frame viewed on the video, the basketball player's position is constantly changing. There is no hang time but due to the slow vertical change of position it may appear that way. (As the ball is moving upward before the player leaves the
ground, on the way down his arms are extended and lift the ball into the net, giving the illusion of hanging in the air.)

## 3.a)

Students' answers will vary according to their weight in pounds. Be aware that some students may be sensitive about their weight and be reluctant to write it down. To avoid this problem, you may choose to only have one student in the group, or
class, do the jumping and everyone in the class use this weight and height in their calculations. Expect to help students when applying their own data to replicate the calculations presented as an example in Physics Talk. Ask the students about the forces acting on them between the "ready" and "launch" positions and between the "launch" and "peak" positions.

## 4.a)

Students record the distance from the floor to their center of mass in the crouched or "ready" position.

## Teaching Tip

If the student is going to jump near the wall, the group can just place pieces of masking tape on the wall to correspond to the "ready" and "launch" positions, and then measure the distance between them.

## 5.a)

Students record the distance from the floor to their center of mass in the launch position.

## 5.b)

The students calculate the difference between the ready and launch heights.

## 6.a)

Students measure the height of the center of mass from the floor at the peak of the jump. One student should indicate the position with their finger, and hold that position while another measures the height after the student has landed.

## 6.b)

The students calculate vertical jump height by subtracting the height at the peak of the jump height from the launch height.

## Teaching Tip

A motion detector can easily be attached to the ceiling of the classroom for the students to check the height of their jump. This quickly becomes a competitive exercise for many students, so you may want to limit its use to only serve as an additional check on the height reached by the jumpers in each group. To determine the height of the jump, have the students stand underneath the motion detector. Start the detector, and then have the students crouch down and jump directly upward toward the detector. The height of their jump is the difference between their distance from the detector when standing, and the minimum distance from the detector reached while jumping.


## 7.a)

Answers will vary. The GPE will equal $m g h$ where $b$ is the difference in height measure in Step 6.b).

## 7.b)

The students copy their answer from Step 7.a) here.


## 7.d)

The students create a chart that shows the $S P E=K E+G P E$ for the top of the jump.

## 8.

The students may try to jump under a motion detector. The height of the jump and the height during the ready position may be easily measured with this device.

## 2-9a Blackline Master

## Physics Talk

As students read the Physics Talk, have them revise their definitions of gravitational potential energy, spring potential energy, and kinetic energy. Ask them to write a brief explanation of how energy conversions took place during the Investigate, how work done brought about a change in energy, and what happened to the total energy of a system. Once students have written their explanation, divide them into groups and have them share their responses, then invite them to discuss their responses with the whole class. Suggest to students that they can illustrate their explanation with diagrams showing an athlete in different positions. Have them label each diagram. A useful visual would be the use of bar graphs to indicate the amount of energy in the form of GPE, $S P E$, and $K E$ in the various positions, as well as the total energy of the system. The students should realize that the total energy remains constant for the system, and should have a total energy graph that indicates this in all positions.

Choose the results of one member of the class (or yourself if you did the jump) as an example of how to calculate the energy in the various positions, as it is shown in the Physics Talk. Have them work out the values of gravitational potential energy and kinetic energy at their launch position. The height of jump of a second class member may be chosen, or perhaps that of an Olympic athlete as a comparison for additional practice. A person jumping on a trampoline provides another opportunity for students to examine energy conversion. A discussion of why jumping on a trampoline yields ever-increasing heights (up to a point), while successive jumps on a hard floor do not, should convince the students that the SPE stored in the deformed trampoline is restored to the jumper, while the hard floor does not respond in a similar manner. They should know how jumping from a hard surface produces a difference in the kinetic energy of rebound as compared to jumping from a soft surface like a trampoline.

When students are introduced to other forms of energy like light energy, chemical energy, heat energy, and sound energy, reemphasize that each type of energy can be measured and the total energy of a closed system is always conserved when this energy is transformed from one form into another. Write one of the sample problems in the Physics Talk on the board and discuss each step of the strategy. Be sure to emphasize the connection between work and energy, and how doing work

on a system will change the system's total energy, while energy transformations within the system do not.

A similar example to jumping from a hard floor into the air is jumping on a trampoline (or your bed, when you were younger). If you were to jump on the trampoline, the potential energy from the height you are jumping would provide kinetic energy when you landed on the trampoline. As you continued down, you would continue to have kinetic energy because you would still be losing gravitational potential energy. However, the trampoline bends and/or the springs holding the trampoline stretch. Either way, the trampoline or springs gain elastic potential energy at the expense of your kinetic energy and changes into gravitational potential energy.

| Energy $\rightarrow$ <br> Position $\downarrow$ | Elastic potential <br> energy | Gravitational <br> potential energy $=m g h$ | Kinetic energy <br> $=\frac{1}{2} m v^{2}$ |
| :---: | :---: | :---: | :---: |
| High in the air position | 0 | 2300 J | 0 |
| Landing on the <br> trampoline position | 0 | 500 J | 1800 J |
| Lowest point on the <br> trampoline position | 2300 J | 0 | 0 |

The conservation of energy is one of the great discoveries of science. You can describe the type of energy in words (elastic potential energy, gravitational potential energy, and kinetic energy). There is also sound energy, light energy, chemical energy, electrical energy, nuclear energy, and the internal energy that reveals itself through temperature. These words, however, do not give the complete picture. Each type of energy can be measured and calculated. In a system not exchanging energy with objects external to it, the total of all the energies at any one time must equal the total of all the energies at any other time. That is what is meant by the conservation of energy.
If you choose to look at one object in the system, that one object can gain energy. For example, in the collision between a player's foot and a soccer ball, the soccer ball can gain kinetic energy and move faster. Whatever energy the ball gained, you can be sure that the foot lost an equal amount of energy. The ball gained energy, the foot lost energy, and the "ball and foot" total energy remained the same. The ball gained energy because work (force on the ball over a distance in the same direction) was done on it. The foot lost energy because negative work (force on the foot over a distance in opposite directions) was done on it. The total system of "ball and foot" neither gained nor lost energy.
Physics provides you with the means to calculate energies. You may wish to practice some of these calculations now. Never lose sight of the fact that you can calculate the energies because the sum of all of the energies remains the same.

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\begin{aligned}
& \text { Sample Problem } \\
& \text { A trainer lifts a } 5.0-\mathrm{kg} \text { equipment bag from the floor to the shelf } \\
& \text { of a locker. The locker shelf is } 1.6 \mathrm{~m} \text { off the floor. } \\
& \text { a) How much force will be required to lift the bag off the floor? } \\
& \text { b) How much work will be done in lifting the bag to the shelf? } \\
& \text { c) How much potential energy does the bag have as it sits on the shelf? } \\
& \text { d) If the bag falls off the shelf, how fast will it be going when } \\
& \text { it hits the floor? } \\
& \text { Strategy: This problem has several parts. It may look complicated, } \\
& \text { but if you follow it step-by-step, it should not be difficult to solve. } \\
& \text { Given: } \\
& m=5.0 \mathrm{~kg} \\
& h=1.6 \mathrm{~m} \\
& a=9.8 \mathrm{~m} / \mathrm{s}^{2} \\
& \text { Strategy: } \\
& \text { a) Why does it take a force to lift the bag? It takes a force because the } \\
& \text { trainer must act against the pull of the gravitational field of Earth. } \\
& \text { This force is called weight, and you can solve for it using Newton's } \\
& \text { second law. } \\
& F=m a=w \\
& =(5.0 \mathrm{~kg})\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right) \\
& =49 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}^{2} \text { or } 49 \mathrm{~N} \\
& \text { A force of } 49 \mathrm{~N} \text { is required to lift the bag. } \\
& \text { b) The information you need to find the work done on an object is the } \\
& \text { force exerted on it and the distance it travels. The distance was given } \\
& \text { and you calculated the force needed. Use the equation for work. } \\
& \text { Solution: } \\
& W=F \cdot d \\
& =(49 \mathrm{~N})(1.6 \mathrm{~m}) \\
& =78.4 \mathrm{~N} \cdot \mathrm{~m} \text { or } 78 \mathrm{~J} \\
& \text { The work done lifting the bag is } 78 \mathrm{~J} \text {. } \\
& \text { c) The amount of potential energy depends on the mass of the object, } \\
& \text { the acceleration due to gravity, and the height of the object above } \\
& \text { what is designated as zero height (in this case, the floor). You have all } \\
& \text { the needed pieces of information, so you can apply the equation for } \\
& \text { potential energy. }
\end{aligned}
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## Active Physics



## Checking Up

## 1.

The energy is provided by the student's muscles.

## 2.

In the launch position, the students will have gravitational potential energy and kinetic energy. At the peak of the jump, the students will have gravitational potential energy.

## 3.

Other forms of energy include sound, electrical, chemical, nuclear, and internal energy or heat. However, all these energies may be classified as either kinetic or potential when observed on an atomic level.

## Active Physics Plus

While students are solving problems, ask them how they could explain that kinetic energy is a scalar quantity. One justification for kinetic energy being a scalar can be seen from the formula
$K E=\frac{1}{2} m v^{2}$
Because the energy is proportional to velocity squared, it would make no difference if the velocity were in the positive or negative direction. The square of either would be positive and the previous direction would be lost. On a simpler level, there simply is no direction associated with kinetic energy because the work necessary to cancel the energy would be independent of the direction in which the object moves.

Point out that each answer should highlight the transformation of energy and how the law of conservation of energy is helpful in finding the value of a quantity. Ask students to share their answers with their classmates, then have a whole-class discussion on each problem.

## 1.a)

$\frac{1}{2} m v^{2}=m g \Delta h$. Solving for $v$ we have $v=\sqrt{2 g \Delta h}=20 \mathrm{~m} / \mathrm{s}$.

## 1.b)

Velocity is the same regardless of the number of people in the roller coaster. If the ride were people dependent, numerous problems might arise. If the cart went faster with more people, increasing the number of people would increase the chances of a collision between

carts. Also, the "thrill" of the ride would depend upon how many people were in the car. Finally, the stresses created on the rollercoaster structure would depend upon the cart's speed, which would vary greatly if the speed was mass dependent.

## 2.

The spring potential energy is
$\frac{1}{2} k x^{2}=\frac{1}{2}(60 \mathrm{~N} / \mathrm{m})(0.4 \mathrm{~m})^{2}=4.8 \mathrm{~J}$

The kinetic energy of the launched balloon equals the spring potential energy. Setting these two equal and solving for $v$ we have
$\frac{1}{2} m v^{2}=4.8 \mathrm{~J}$
$v=\sqrt{\frac{2(4.8 \mathrm{~J})}{m}}=5.7 \mathrm{~m} / \mathrm{s}$
The vertical fall distance determines the time in the air for an object launched horizontally or
$d=\frac{1}{2} a t^{2}$
$t=\sqrt{\frac{2 d}{a}}=\sqrt{\frac{2(2 \mathrm{~m})}{\left(10 \mathrm{~m} / \mathrm{s}^{2}\right)}}=0.63 \mathrm{~s}$
The horizontal distance traveled is the horizontal speed multiplied by the time in the air or
$d=v t$, which gives $d=$
$(5.7 \mathrm{~m} / \mathrm{s})(0.63 \mathrm{~s})=3.6 \mathrm{~m}$
3.

At the start, the energy of the motorcycle is all gravitational potential energy:
$P E=m g h=$
$(200 \mathrm{~kg})\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)(20 \mathrm{~m})=$ 39, 000 J .

The motorcycle gains 200,000 J of energy and loses $50,000 \mathrm{~J}$ of energy while on the ramp, so its
total energy when airborne equals the net energy gained, which is
$200,000 \mathrm{~J}$ (from the motor) + 39,000 J(from PE) -
$50,000 \mathrm{~J}($ due to friction $)=$ 189, 000 J .

At the highest point while airborne, the motorcycle has a kinetic energy of $K E=\frac{1}{2} m v^{2}=$ $\frac{1}{2}(200 \mathrm{~kg})(40 \mathrm{~m} / \mathrm{s})^{2}=160,000 \mathrm{~J}$. Therefore, the rest of the energy, $189,000 \mathrm{~J}-160,000 \mathrm{~J}=29,000 \mathrm{~J}$ must be gravitational potential energy. So, the height can be found using
$P E=m g h$ or $h=\frac{P E}{m g}=$
$\frac{29,000 \mathrm{~J}}{(200 \mathrm{~kg})\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)}=15 \mathrm{~m}$.

## What Do You Think Now?

The What Do You Think Now? questions give students the opportunity to bring up any questions that they might have, revisit their responses, and modify them where necessary. You might want to return to the What Do You See? illustration and ask students if they now understand which concept the artist was trying to capture. Encourage them to discuss their ideas. Consider sharing A Physicist's Response with them. At this stage, students should show confidence in their answers.

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## Reflecting on the Section and the Challenge

After students have read Reflecting on the Section and the Challenge in their Active Physics textbooks, focus attention on the important aspects of this section by highlighting key physics concepts. Discuss how work is related to energy transformations. Ask students to reflect on a specific event in a sports video that illustrates the work done by an athlete, as well as the energy transformations that took place during the sporting event. Emphasize that concepts learned in this section could be applied to their Chapter Challenge.

## Physics Essential Questions

## What does it mean?

The energy of the muscles provides the body with kinetic energy which propels the body in the air where it gains gravitational potential energy. The sum of $E P E, K E$, and GPE is constant for any point in the jump.

How do you know?
$K E=\frac{1}{2} m v^{2}$
$G P E=m g h$
$E P E=\frac{1}{2} k x^{2}$

Why do you believe?
The energy came from the work done by your arm. Chemical energy in your muscles provided the kinetic energy of the ball.

## Why should you care?

The conservation of energy can explain how a high jumper uses the muscles in her legs to give her body kinetic energy. This kinetic energy and more chemical energy from the legs propels her into the air, where she gains gravitational potential energy and clears the bar.

## Physics to Go

1. 

Work $=F d=(m g) d=$
$(50 \mathrm{~kg})\left(10 \mathrm{~m} / \mathrm{s}^{2}\right)(1 \mathrm{~m})=500 \mathrm{~J}$.
2.

Before jumping on the sled, team members do work while running and pushing the sled to give the sled and their bodies kinetic energy; therefore, $F d=\frac{1}{2} m v^{2}$. After the team has jumped on the sled, the total energy of the team and sled is equal to the kinetic energy gained during the pushing phase plus the gravitational potential energy $=$ $m g h$, where $b$ is the vertical distance from the top to the bottom of the hill. At the bottom of the hill, the kinetic energy of the sled should be equal to the kinetic energy gained during the pushing phase plus the loss in potential energy due to coming down the hill, $\frac{1}{2} m v^{2}+m g h$. The brake must do enough work to cause the sled to lose all of its kinetic energy by exerting a force in the direction opposite the sled's motion.

## 3.

It is apparent that the person wants to believe that the player can defy gravity and is attempting to justify that belief by rejecting scientific evidence. It could be said that the person is not reflecting open-mindedness, a desirable attribute in scientific pursuits. To address the situation, you may offer to video tape in slow motion the player, as many times as necessary, to ascertain if in any of the cases the player is able to "hang." After several attempts,

even this person may agree he was mistaken.
4.

The burden of proof rests with the person making the claim.
5.

One way is to increase the force the athlete is able to exert using muscles, and the other way is to lose weight without decreasing muscular force.
6.a)
$1.0 \mathrm{~N} \times 1.0 \mathrm{~m}=1 \mathrm{~J}$
6.b)
$1.0 \mathrm{~N} \times 10 \mathrm{~m}=10 \mathrm{~J}$
6.c)
$10 \mathrm{~N} \times 1.0 \mathrm{~m}=10 \mathrm{~J}$
6.d)
$0.10 \mathrm{~N} \times 100 \mathrm{~m}=10 \mathrm{~J}$
6.e)
$100 \mathrm{~N} \times 0.10 \mathrm{~m}=10 \mathrm{~J}$
7.

All answers are the same as for Question 6 on the previous page.

## 8.

All answers are the same as for Question 6 on the previous page.
9.
$W=F d=(50.0 \mathrm{~N})(43 \mathrm{~m})=$
$2150 \mathrm{~J}(2200 \mathrm{~J})$
10.
$K E=\frac{1}{2} m v^{2}=\frac{1}{2}(62 \mathrm{~kg})(8.2 \mathrm{~m} / \mathrm{s})^{2}$
$=2084 \mathrm{~J}(2100 \mathrm{~J})$
11.a)
$F=m a \quad a=F / m=$
$30.0 \mathrm{~N} / 5.0 \mathrm{~kg}=6 \mathrm{~m} / \mathrm{s}^{2}$
11.b)
$W=F d=(30.0 \mathrm{~N})(18.75 \mathrm{~m})=$ 563 J

## NOTES

NOTES

| 12.a) | 13. | $K E=\frac{1}{2} m v^{2}=$ |
| :---: | :---: | :---: |
| $\begin{aligned} & W=F d \quad d=W / F= \\ & (40,000 \mathrm{~J}) /(3200 \mathrm{~N})= \end{aligned}$ | The work done is equal to the change in $K E$. The final $K E$ is 0 . | $\frac{1}{2}(64.0 \mathrm{~kg})(15.0 \mathrm{~m} / \mathrm{s})^{2}=7200 \mathrm{~J}$ |
|  | The initial $K E$ can be found. | $W=F d$ |
| $12.5 \mathrm{~m}(12 \mathrm{~m})$ | $K E=\frac{1}{2} m v^{2}=$ | $d=W / F=$ |
| $F=m a \quad a=F / m=$ | $\frac{1}{2}(0.150 \mathrm{~kg})(40 \mathrm{~m} / \mathrm{s})^{2}=120 \mathrm{~J}$ | $(7200 \mathrm{~J}) /(417 \mathrm{~N})=17 \mathrm{~m}$ |
| $(3200 \mathrm{~N}) /(1200 \mathrm{~kg})=2.7 \mathrm{~m} / \mathrm{s}^{2}$ | 14. |  |
|  | The change in $K E$ is equal to the work done. Calculate the change in $K E$ and then calculate the distance. |  |

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$d=W / F=$
$(7200 \mathrm{~J}) /(417 \mathrm{~N})=17 \mathrm{~m}$
14.

The change in $K E$ is equal to the work done. Calculate the change in $K E$ and then calculate the distance.
$\frac{1}{2}(64.0 \mathrm{~kg})(15.0 \mathrm{~m} / \mathrm{s})^{2}=7200 \mathrm{~J}$
$W=F d$
$K E=\frac{1}{2} m v^{2}=$


## 15.

A sample table might look like the one below.

|  | KE | GPE EPE | Sum of <br> energies |  |
| :--- | :---: | :---: | :---: | :---: |
| Running | 1000 | 0 | 0 | 1000 |
| Pole <br> bent | 100 | 0 | 900 | 1000 |
| At peak | 150 | 850 | 0 | 1000 |
| Landing | 1000 | 0 | 0 | 1000 |
| On <br> cushion | 0 | 0 | 0 | 0 |

16. 

|  | $K E$ | GPE | EPE | Sum of <br> energies |
| :--- | :---: | :---: | :---: | :---: |
| Peak <br> height | 0 | 1000 | 0 | 1000 |
| Landing | 900 | 100 | 0 | 1000 |
| Lowest <br> point | 0 | 0 | 1000 | 1000 |

17. 

|  | $K E$ | GPE | SPE | Sum of <br> energies |
| :--- | :---: | :---: | :---: | :---: |
| Top of <br> Mt | 0 | 1000 | 0 | 1000 |
| Middle | 500 | 500 | 0 | 1000 |
| Bottom | 1000 | 0 | 0 | 1000 |

## 18.

## Preparing for the Chapter Challenge

The students should choose a sports event that includes elastic potential energy and a thorough description of what is happening during the energy transformations. Many sports that include rackets, bats, or other objects striking a ball, puck, etc., will have stored energy. A baseball transition might go as follows: work is done by the pitcher to give the ball $K E$, the loss of $K E$ into spring $P E$ when the ball strikes the bat, the change from elastic $P E$ to $K E$ as the ball leaves the bat, the transformation of some of the $K E$ to Gravitational PE as the ball rises, then returning to $K E$ as the ball falls, and finally the work done by the fielder who catches and stops the ball. Additional discussion might include the energy lost to heat in the bat, and the air due to frictional forces.

## SECTION 9 QUIZ

## 2-9b Blackline Master

1. A baseball bat strikes a baseball of mass that is at rest, and as a result the baseball flies away from the bat. The kinetic energy gained by the baseball as it leaves the bat is due to the
a) loss of potential energy of the ball as it falls back to the ground.
b) work done by the bat on the ball.
c) gain in potential energy as the ball rises to the peak of its trajectory.
d) loss of mass after the ball is hit.
2. A catapult with a spring constant of $10,000 \mathrm{~N} / \mathrm{m}$ is used to launch a target from the deck of a ship. The spring is compressed a distance of 0.5 m before the $1.56-\mathrm{kg}$ target launched. What is the target's velocity as it leaves the spring?
a) $10 \mathrm{~m} / \mathrm{s}$
b) $20 \mathrm{~m} / \mathrm{s}$
c) $30 \mathrm{~m} / \mathrm{s}$
d) $40 \mathrm{~m} / \mathrm{s}$
3. A ball is thrown vertically upward. As the ball rises, the ball's total energy
a) decreases.
b) increases.
c) remains the same.
4. A $10-\mathrm{kg}$ mass at rest on a horizontal frictionless table is accelerated by a force of 20 N . How much work is needed to accelerate the ball to a velocity of $10 \mathrm{~m} / \mathrm{s}$ ?
a) 5 J
b) 200 J
c) 500 J
d) 2000 J
5. An object is lifted upward at a constant speed. The gain in potential energy of the object is due to the
a) work done on the object.
b) total force applied to the object.
c) change in kinetic energy of the object.
d) weight of the object.

## SECTION 9 QUIZ ANSWERS

(1) b) work done by the bat on the ball. This work will not be equal to the loss of GPE when the ball falls down, since it will still be moving forward when it lands, and will maintain some $K E$.
(2) d) $S P E=K E$ or $\frac{1}{2} k x^{2}=\frac{1}{2} m v^{2}$. Canceling the $\frac{1}{2}$ 's on each side gives $(10,000 \mathrm{~N} / \mathrm{m})(0.5 \mathrm{~m})^{2}=(1.56 \mathrm{~kg}) v^{2}$, and $v=40 \mathrm{~m} / \mathrm{s}$.
(3) c) by conservation of energy
(4) c) The work needed is equal to the increase in $K E=\frac{1}{2} m v^{2}=500 \mathrm{~J}$.
(5) a) Because the object is lifted with constant speed, there is no change in $K E$, so all the work goes into increasing GPE.

## NOTES

