## SECTION II

## Velocity and Acceleration: The Big Thrill

## Section Overview

Students begin investigating roller coasters by drawing a roller coaster of their own design and then consider the Terminator Express roller coaster, which they will modify for the Chapter Challenge. To understand what makes roller coasters such fun, students start by blindfolding a person in a chair with wheels and pushing the chair around by varying the direction and speed. The rider rates each type of move according to the level of "thrill" that he or she experiences on a 1 -to- 5 scale. Students then decide whether it is displacement, velocity, or acceleration during the ride that provides the excitement, and investigate which part of a blindfolded chair ride caused the rider's greatest reactions. Students also measure and analyze relationships between speed and acceleration for a ball on a track. Their observations support the concepts of displacement, speed, velocity, and acceleration. Finally, students apply what they know to solve problems on the concepts they have investigated.

## Background Information

Velocity is defined as the change of position (displacement) divided by the time elapsed. This definition can be written as an equation:

$$
v=\Delta d / \Delta t
$$

where $\Delta d$ is the displacement and $\Delta t$ is the time elapsed. The units for displacement are meters and the units for time are seconds; hence the units for velocity are $\mathrm{m} / \mathrm{s}$ (meters per second). Velocity is a vector quantity. It has both a magnitude and a direction. The direction of the displacement is the direction of the velocity.

Although you recognize speed and velocity as you move about in cars, trains, planes or walking, there are misconceptions that you are well aware of and
you must listen intently to your students to catch these misconceptions and help them confront them. For example, students may confuse position with velocity. When one car passes another, students may think that at the instant one car passes another, their speeds are identical.

Acceleration is defined as a change in velocity divided by the time elapsed. This definition can be written as an equation:

$$
a=\Delta v / \Delta t
$$

The units for velocity are $\mathrm{m} / \mathrm{s}$ and the units for time are seconds; the units for acceleration are $(\mathrm{m} / \mathrm{s}) / \mathrm{s}$ (meters per second every second). It is often abbreviated as the equivalent $\mathrm{m} / \mathrm{s}^{2}$ (meters per second squared) but student understanding will be increased if the units are stated as $\mathrm{m} / \mathrm{s}$ every second. This will continue to reinforce the definition of acceleration as a change in velocity divided by the time elapsed. Acceleration is a vector quantity. It has both a magnitude and a direction. The direction of the change in velocity is the direction of the acceleration. Acceleration is a change of velocity with respect to time, while velocity is, in itself, a change of position (displacement) with respect to time. It's very difficult for students to grasp a change of a change. In calculus, you recognize a change of a change as the second derivative of the function.

Strictly speaking, the velocity and acceleration as defined above are quantities averaged over the time elapsed. More sophisticated treatments would let the elapsed time become very short, so we could talk about the velocity or acceleration at a particular instant of time. Although the distinction between average velocity and instantaneous velocity is important in some circumstances, the difference is not crucial for the sections discussed in this chapter.

## Crucial Physics

- A vector quantity has magnitude (how much) and direction (which way). A scalar quantity has only magnitude (how much). There is no direction associated with it. Both quantities require units for a complete description.
- Speed is calculated by dividing the distance (the path length) traveled by the elapsed time. Both speed and distance are scalar quantities, having no direction. Speed is measured in meters/second.
- The average velocity is given by the displacement (change in position) over the time elapsed. Both displacement and velocity are vector quantities. The average velocity is in the same direction as the displacement. Velocity is measured in meters/second.
- The acceleration of an object is defined as the change in velocity divided by the time elapsed. Whenever an object's velocity changes (either its magnitude, direction, or both) the object accelerates. Acceleration is measured in meters/second/second.
- You can "feel" your acceleration because of the forces on you that must be exerted to accelerate you and your internal organs.

| Learning Outcomes | Location in the Section | Evidence of Understanding |
| :--- | :--- | :--- |
| Sketch and interpret a top view <br> and a side view of a roller- <br> coaster ride. | Investigate <br> Steps 1 and 2 | Students sketch diagrams and interpret the advantages and <br> disadvantages of having two sketches. |
| Identify whether thrills in roller- <br> coaster rides come from speeds, <br> accelerations, or changes in each. | Investigate <br> Steps 3-7 | A student pushes a blindfolded student around in a chair <br> at different speeds and directions, and from the reaction <br> of the blindfolded person determines the extent of the <br> blindfolded person's reaction. |
| Define accelerations as a change <br> in velocity with respect to time <br> and recognize the units of <br> acceleration. | Investigate <br> Steps 4-8 <br> Physics Talk | Students note the change in velocity while pushing <br> a blindfolded rider, and arrive at the definition of <br> acceleration. |
| Calculate and measure velocity <br> and acceleration. | Investigate <br> Part C: <br> Steps 1-7 | Students correctly calculate the velocity and acceleration of <br> the ball on the track. |

## NOTES

## Section 1 Materials, Preparation, and Safety

## Materials and Equipment

| Materials and Equipment | Group <br> (4 students) | Class |
| :--- | ---: | :--- |
| Beespi | 1 per group |  |
| Ball, steel sphere, 3/4 in. | 1 per group |  |
| Track (plastic piece for roller coaster) | 1 per group |  |
| Track, wood, base pack <br> (to include hardware) | 1 per group |  |
| Holder, right angle, cast iron | 1 per group |  |
| Rod, aluminum, 3/8 in. x 12 in. <br> (to act as crossarm) | 1 per group |  |
| Ring stand, large | 1 per group |  |
| Meter stick | 1 per group |  |
| Stopwatch | 1 per group |  |
| C-clamp, 3 in. | 1 per group |  |
| Ruler, metric, in./cm | 1 per group |  |
| Battery, alkaline, AAA | 2 per group |  |
| Blindfold* | 1 per group |  |
| Chair (w/ wheels)* | 1 per class |  |
| Access to a flat surface* |  |  |

*Additional items needed not supplied

## Time Requirements

- Allow one and a half 45 -minute class periods or 65 minutes for this investigation.


## Teacher Preparation

- If you are not familiar with making orthographic (top and side view) drawings, ask an art or mechanical-drawing teacher for assistance.
- If a chair with casters is not normally available, arrange to have one in the classroom for this day, as well as material to blindfold the students who will ride in the chair and the appropriate safety equipment.
- If you are using the velocimeters, familiarize yourself and the students with how to convert the readings to meters/second. If you are using photogates, show the students how to place the photogate so the center of the ball passes through the gate and how to calculate the ball's speed.
- If tracks are not available for the ball, inclined planes with meter sticks taped on may be used to provide a path.


## Safety

NOTE: Unless stated otherwise, safety goggles should always be worn during lab investigations.

- Students who will be riding in the chair in Part B should wear appropriate safety equipment, including a helmet, and elbow and kneepads. To ensure safe chair behavior, it is best if the teacher pushes the chair for Part B.
- The students should keep careful control over the steel balls used in Part C. The steel balls should not land on the floor where someone may slip on them.


## Materials and Equipment

| Materials and Equipment | Group <br> (4 students) | Class |
| :--- | :--- | :--- |
| Beespi |  | 1 per class |
| Ball, steel sphere, 3/4 in. |  | 1 per class |
| Track (plastic piece for roller coaster) |  | 1 per class |
| Track, wood, base pack <br> (to include hardware) |  | 1 per class |
| Holder, right angle, cast iron |  | 1 per class |
| Rod, aluminum, 3/8 in. $\times 12$ in. <br> (to act as crossarm) |  | 1 per class |
| Ring stand, large |  | 1 per class |
| Meter stick |  | 1 per class |
| Stopwatch |  | 1 per class |
| C-clamp, 3 in. |  | 1 per class |
| Ruler, metric, in./cm |  | 2 per class |
| Battery, alkaline, AAA |  | 1 per class |
| Blindfold* |  | 1 per class |
| Chair (w/ wheels)* |  |  |
| Access to a flat surface* |  |  |

*Additional items needed not supplied

## Time Requirements

- Allow one class period or 45 minutes to do the Investigate and Physics Talk discussion.


## Teacher Preparation

- Most of the planning for Plan A still applies, but only one material setup is required. Prepare one track and velocimeter or photogate setup for the front of the classroom. Several students should be recruited to assist you in taking the measurements and recording them on the board for the rest of the class to record in their journals. If a camera and projection system is available it should be used so the students can see more clearly what is occurring.
- Practice several trials with the track and ball prior to the class to be certain consistent results are obtained. Mark the positions for the ball on the track that you will be using, and make the conversions from the $\mathrm{km} / \mathrm{h}$ recorded by the velocimeter to the $\mathrm{m} / \mathrm{s}$ needed for calculation prior to the start of class.
- Make a Blackline Master of the diagrams in Part A, Step 4 and a transparency of Part C, Step 7 of the Investigate in the Student Edition.
- Summarize the Investigate to familiarize the students with what they will be observing.
- Part B of the Investigate should be done with the teacher pushing the chair and a student riding.


## Safety

NOTE: Unless stated otherwise, safety goggles should always be worn during lab investigations.

- Students who will be riding in the chair in Part B should wear appropriate safety equipment including a helmet, and elbow and kneepads. To ensure safe chair behavior, it is best if the teacher pushes the chair for Part B.


## Meeting the Needs of All Students

## Differentiated Instruction: Augmentation and Accommodations

| Learning Issue | Reference | Augmentation and Accommodations |
| :---: | :---: | :---: |
| Learning and using content vocabulary | Chapter Challenge Physics Corner | Augmentation <br> - A strategy that is very effective to teach new vocabulary to students who struggle to decode words or who have difficulty with memory is to pre-teach vocabulary. Introduce all of the words in this list before the class begins the chapter. It is not necessary to teach all of the word meanings at this point, but allow students to read the list aloud and activate prior knowledge by trying to define the vocabulary in their own words. As the class progresses through the chapter, ask students to check their definitions and decide if they need to add to or delete parts of their predicted definitions. <br> Accommodation <br> - For students who struggle with basic reading and writing tasks, provide a typed word list that students can easily access. This list can be used to practice reading the words with a parent, special education teacher, speech and language therapist, etc. Also, students can reference the list when they are answering questions or working on the Chapter Challenge. |
| Lacking a common experience | What Do You Think? | Augmentation <br> - Assume that at least one student in the class has never seen or ridden a roller coaster. Show video footage of people riding roller coasters and ask students to record their observations. Explicitly tell students to record the reactions of the riders at each part of the roller coaster. Students may need to watch the footage more than once to record meaningful observations. <br> - Students in the class who have been on a roller coaster could also describe how they felt when they rode a roller coaster. |
| Sketching a roller coaster | Investigate <br> Part A, Steps 1-4 <br> Investigate <br> Part D, Step 1 <br> Physics to Go <br> Questions 1, 10.b) | Augmentation <br> - Students who do not see drawing as a personal strength or who have difficulty with fine motor tasks, may take an excessive amount of time to complete these tasks. Provide students with a reasonable time limit for each step. Also, explain that a sketch is a quick drawing with little detail that may be turned into a more detailed drawing at a later time. <br> - Teach students the meaning of roller-coaster vocabulary including "descend," "horizontal," and "vertical," by asking students to explain the definitions in their own words. <br> - Create a class list of the characteristics of the preferred sketches to be used as a reference throughout Chapter 4. <br> Accommodation <br> - Provide a photocopy of Part D, Step 1, for students who have significant difficulties with fine motor skills or vision. This will allow students to focus on labeling the diagram to understand the concept of "pulling $g$ 's" instead of focusing on drawing skills. |
| Maintaining control of one's impulses, especially when caught up in the moment | Investigate <br> Part B, Step 3 | Augmentation <br> - Students who have difficulty with impulse control may know and understand the safety precautions put forth by the teacher, however, when they get caught up in the excitement of the activity, these students may not remember the rules of the activity. Before students begin pushing their classmates in the chairs, establish an alert sign or phrase such as flashing the lights, clapping, or saying the word "stop." This alert signal will allow the teacher to immediately get the attention of all of the students in the room if things are getting out of control or if someone is being unsafe. <br> - Assign groups with a student leader who does not struggle with impulse control. |


| Learning lssue | Reference | Augmentation and Accommodations |
| :---: | :---: | :---: |
| Understanding the concept of a vector <br> Drawing vectors | Investigate <br> Part B, Steps 6-7 | Augmentation <br> - Understanding that acceleration can change because of a change in direction, even though the magnitude remains constant, is a difficult concept for students who are concrete learners because vectors are more abstract concepts. <br> - Explain what a vector represents and the reasons scientists draw vectors. <br> - Review the basic rules for drawing vectors. <br> 1) Vectors are represented with arrows. <br> 2) The direction and length of the arrows are important. <br> - Provide opportunities to practice drawing vectors and receive feedback from the teacher or peers. <br> - This activity could be differentiated by using the Active Physics Plus section to challenge students with more advanced math skills, while the teacher is reviewing basic vector rules with the rest of the class. |
| Differentiating distance and displacement | Physics Talk <br> Checking Up <br> Question 1 | Augmentation <br> - For many students, the difference between distance and displacement is too subtle to seem important and too abstract to be understood conceptually. Help the students create a few concrete diagrams to represent situations for which the distance and displacement are the same and situations for which they are different. <br> - To begin, students could draw diagrams of the situations described in Physics Talk. Then students could draw new situations that compare distance and displacement and share the drawings with their peers. <br> - Remember that conceptually understanding distance and displacement will make it much easier for students to understand the concepts of velocity and speed. <br> Accommodation <br> - Provide diagrams of scenarios and ask students to label the distance and displacement on the diagrams. |
| Using formulas to do calculations | Physics to Go Questions 3, 4, 6, 7 , and 8 | Augmentation <br> - Students often need many opportunities to practice and receive feedback when using new skills. <br> - Model or ask volunteers to model the problem-solving method required in class using the speed, velocity, and acceleration formulas. Providing sample problems for students to refer back to when they are working through problems independently helps increase student accuracy and success. <br> - Practicing a problem-solving method with these more simple formulas will also be helpful later in the chapter when more complicated formulas are introduced. <br> Accommodation <br> - Provide a sheet of blank problem-solving boxes (a graphic organizer) for students who struggle to organize their steps or have had difficulty with problem solving in the past. |

## Strategies for Students with Limited English-Language Proficiency

| Learning Issue | Reference | Augmentation |
| :---: | :---: | :---: |
| Vocabulary comprehension | Investigate Part A: Step 5 | You may need to explain "loading platform." You may also wish to review the term "radius" and explain that it applies not only to circles but also to smooth curves. The terms "vertical" and "horizontal" were reinforced in Physics in Action, Projectile Motion, and now would be a good time to practice fluency in the use of these terms. |
| Comprehension | Investigate <br> Part B: Step 2 | Rating something on a scale of 1 to 5 may not be a familiar practice to some ELL students. They may benefit from an example or two. |
| Vocabulary comprehension | Investigate <br> Part B: Step 3 | Help students understand the word "exhibits" in context. They may be familiar with the use of this term as a noun, for example in a museum exhibit. Work around to the verb form by asking what a museum exhibit does (shows the item on display). So, to exhibit a thing or an emotion is to show it. |
| Comprehension | Investigate <br> Part B: Step 7.b) | Before moving on, make sure students understand that accelerations elicited the strongest responses from the rider. |
| Understanding concepts | Investigate <br> Part C: Step 1.a) | Make sure students identify instruments for measuring distance, direction, and time as the tools necessary for measuring velocity. |
| Vocabulary comprehension | Investigate <br> Part C: Step 2.a) | All students may benefit from a discussion of the terms "distance," "position," and "displacement." Point out that because position can be described by two coordinates on a grid, with no reference to direction, position is a scalar. A change in position (displacement) always has a direction, so it is a vector. The term "distance" gives the magnitude of the change in position, but because it does not specify the direction, it is a scalar. |
| Understanding concepts | Investigate <br> Part C: Step 4 | When you demonstrate the use of a photogate timer, make sure to tell students which kind you are using, double-beam or single-beam. Make sure students understand how it works. Even if you have a double-beam photogate timer, which computes the speed for you, you will need to make sure students understand how the single-beam type works, because they will need to make calculations for scenarios using that type of timer. Before you move on to Step 5, make sure students can answer the question at the end of Step 4.b) [the diameter of the steel ball]. |
| Understanding concepts | Investigate <br> Part D: Step 1.a) | The phrase "pulling $g$ 's" may be confusing for ELL students. The term " $g$ " is used here as a noun, so it can be used in a plural form. Explain that one $g$ would be an acceleration of $9.8 \mathrm{~m} / \mathrm{s}^{\mathrm{s}}$, and two $\mathrm{g}^{\prime} \mathrm{s}$ would be double that, or $19.6 \mathrm{~m} / \mathrm{s}^{\mathrm{s}}$. The phrase "pulling g's" refers to a force that would produce accelerations greater than $g$. If this force is in the same direction as the force of gravity, the rider feels heavy. If this force is in the opposite direction to the force of gravity, the rider feels light. |
| Understanding concepts | Physics Talk | Provide opportunities for ELL students to use the terms "distance" and "displacement" in a class discussion. Have one student read aloud the paragraph that begins, "For a person walking one lap around a city block..." Then ask for a volunteer to explain why the displacement and velocity are zero. To encourage further development of language skills, encourage students to debate whether a person with a velocity of zero has moved. |
| Vocabulary comprehension | Inquiring Further | Make sure students understand "innovations" and "retained" in context. |

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## SECTION I <br> Teacher Suggestions and Sample Answers

## What Do You See?

The What Do You See? illustration is designed to stimulate students' curiosity. Consider using an overhead to highlight certain aspects and trace the zigzag paths that are shown, asking students what these patterns might suggest. Encourage students to ponder each visual and what the details might suggest. As a prompt, you could ask them why the person has been blindfolded or why is the person being pushed around in a chair with wheels. As students begin to warm up to the discussion with answers, ask them to recall these initial impressions as they move further along in the chapter.


## Students' Prior Conceptions

Prior to this study of the concepts developed in Thrills and Chills, teachers should brainstorm with students to assure that they do not confuse energy issues. Students shouldn't confuse or conflate the scientific law of conservation of energy with environmental conservation or with conservation of energy issues widely discussed in current events, the media, and/or in other study areas. This first section enables students to explore their prior conceptions on gravity, particularly the direction in which gravity acts.

1. Students believe that objects are pushed down rather than pulled down by gravity. Given the opportunity to measure and to calculate accelerations and to understand that the velocity changes as roller-coaster rides go up and down hills offer students opportunities to check their nascent ideas on how objects behave in a gravitational field. Calculating decreasing speeds at the top and increasing speeds at the bottom of hills should affirm the pull of gravity on objects in student thinking. Thrills accompany the greater velocity as riders are pulled down the hill of the coaster.

## What Do You Think?

Ask students to use the illustration presented in the What Do You See? to help them answer this question. Students might want to talk of their own experiences on a roller coaster. Encourage them to write down their responses and point out that they will be returning to the question again, and will be given a chance to modify their answers based on their investigations. At this stage, students should be evaluated on the level of their engagement and not for the correctness of their responses. You should emphasize that this question is designed to elicit students' prior understanding.

## What Do You Think?

## A Physicist's Response

Although when screams will occur may seem to be a subjective question, in general, the loudest screams on a roller coaster take place when two criteria are met: The first one is that the rider undergoes a large change in velocity (acceleration). This occurs when the rider is changing speeds quickly, or possibly going around a loop. The change in velocity is also associated with a rapid change in the force that is holding the rider against the seat of the car, affecting their sense of security. The roller-coaster builders strive to achieve this in a manner that is as safe as possible for the riders. The second criterion is that the rider's visual stimulus suggests that something particularly dangerous is about to occur. This is often done by adjusting either the scenery, or putting the riders in a novel situation that also affects their sense of security. And when you are scared, you scream.

## Investigate

## Part A: Sketch of the Roller Coaster

## 1.a)

Before the students draw the roller-coaster ride, you might have the students draw a side view sketch and top view sketch of a simple straight incline. Have the students talk about the relationship between the sketches and the actual incline. This should help the students get started on the roller coaster sketches. One possible sketch might appear like the one below:


## 2.a)

Students who have experience with top and side views may prefer their sketches to those that tried a different approach. Students' reasons for preferring a specific sketch over others should express clarity.

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## 3.a)

Students should realize that the advantage of having both a top and a side-view sketch provides information in three dimensions rather than the two dimensions from a single sketch.

## Teaching Tip

Try drawing a simple roller coaster on the board or overhead projector and ask the students to draw a side and top view for practice. Then show a side and top view.
4.a)

Having students actually sketch the diagrams from the text in their logs is preferable to giving them a copy of the diagram at this time.


## 5.

Ensure that lab partners reverse roles when shifting from the top view to the side view so that each has a chance to move a finger around the roller coaster. Encourage all of the students to participate.

## Part B: Roller-Coaster Fun

## 1.a)

Students should list safety precautions before blindfolding
someone in their group, and write them on the board. Have the student wear a bicycle helmet and hold onto the arms of the chair. Choose a large open area for this Investigate so there is no danger of running into any obstacles. High velocities are not necessary and violent forces leading to extremely rapid changes in direction should not be attempted. If the rider starts to feel ill or nauseous the investigation should
be terminated immediately. The safety rule should include all those previously mentioned. Include any additional suggestions the students have that seem reasonable for safety.

After completing the safety precautions listed above move the chair at a constant speed and then quickly change directions. Play with sudden stops, quick turns, and large increases in speed. Have the other students record the rider's reactions. Maintain the safety of the rider at all times. Your students will find that the rider will smile, laugh, or make sounds during the accelerations.

## 2.

These are instructions for the student rider. You may ask the rider to shout out a number on the $1-5$ scale as the chair is being pushed.

## 3.

Any change in direction or speed will probably produce a reaction, regardless of the direction of the push. Keep the safety of the student rider and watchers paramount at all times during this investigation.
3.a)

Have the students record both the thrill factor and what the motion was that caused that factor's number in their logs.

## 4.a)

The velocity by itself does not produce a large reaction by the rider. It is the changes in the velocity that the rider feels most strongly. These changes could be increases or decreases in the speed or a change in direction of the speed or a combination of the two simultaneously. The highest ratings will probably be for sudden changes in direction and speed simultaneously.

## 5.a)

Using change in velocity as the difference between the beginning and the ending velocities, students calculate the change in velocity to be $1.5 \mathrm{~m} / \mathrm{s}-1.1 \mathrm{~m} / \mathrm{s}=0.4 \mathrm{~m} / \mathrm{s}$.

## 6.a)

Students' drawings should look like the one below:

## 7.a)

Students' diagrams should be similar to the one shown to the right. Direction of the vectors is right. Direction of the vectors is
not important, but they should be at right angles. Students should record a change in speed of $0.2 \mathrm{~m} / \mathrm{s}$ and a direction change of 90 degrees.


Chapter 4 Thrills and Chills

Sa) The recorder should note when the blindfolded team member smiles or laughs or exhibits some emotion as well as the rider's rating of the thrill level.
4. A rider's velocity is a measure of the rider's speed and includes information about the direction in which the rider is traveling. The rider's velocity may have been $1.2 \mathrm{~m} / \mathrm{s}$ north or $1.5 \mathrm{~m} / \mathrm{s}$ toward the door or $1.0 \mathrm{~m} / \mathrm{s}$ toward the window. In each case, there is a magnitude or size ( $1.0 \mathrm{~m} / \mathrm{s}, 1.2 \mathrm{~m} / \mathrm{s}, 1.5 \mathrm{~m} / \mathrm{s}$ ) and a direction (north, toward the door, toward the window).
دa) Was the velocity responsible for the "rider's" reactions? Did the blindfolded rider react more when the chair was moving with a fixed velocity (one with the same speed and the same direction) or when the velocity changed, when there was a change in speed or a change in direction of the chair or change in direction of the chair or
when there was a change in both the speed and in the direction of the chair?
5 . The change in a rider's velocity over time is referred to as acceleration. Suppose a rider was moving at $1.1 \mathrm{~m} / \mathrm{s}$ north and changed velocity to $1.5 \mathrm{~m} / \mathrm{s}$ north. There is an acceleration because there was a change in speed.
Sa) In your Active Physics $\log$, calculate and record the change in velocity,
6. There would also be acceleration if the rider changed velocity from $1.3 \mathrm{~m} / \mathrm{s}$ east to $1.3 \mathrm{~m} / \mathrm{s}$ south. Here the acceleration is due to a change in the direction, with no change in speed.

Sa) Draw vectors for these two velocities and describe the change in velocity in your log.
7. Suppose a rider was moving at $1.5 \mathrm{~m} / \mathrm{s}$ toward the door and someone pushed him or her and made the rider move at $1.3 \mathrm{~m} / \mathrm{s}$ toward the window. There is
acceleration because there was a chang in speed and a change in direction.
a) Draw a vector to represent the two velocities for the rider in the above example. Make the direction toward the window to be at right angles to the original direction toward the door. Record the change in speed and the change in direction in your Active Physics $\log$ for the rider in the example above.
b) Was acceleration responsible for the reactions of the blindfolded rider? Did reactions of the blindfolded rider? Did
8. Acceleration is a change in velocity in a specific time. For example, the change from $1.1 \mathrm{~m} / \mathrm{s}$ north to $1.5 \mathrm{~m} / \mathrm{s}$ north may have taken 1 s .
The change in velocity is $0.4 \mathrm{~m} / \mathrm{s}$ in one second. There are a number of ways in which this can be stated: The change in velocity is

- $0.4 \mathrm{~m} / \mathrm{s}$ in one second
- $0.4 \mathrm{~m} / \mathrm{s}$ every second
- $0.4 \mathrm{~m} / \mathrm{s}$ per second
- $0.4(\mathrm{~m} / \mathrm{s}) / \mathrm{s}$
- $0.4 \mathrm{~m} / \mathrm{s}^{2}$

Part C: Measuring Velocities and Calculating Accelerations

1. The value $1.5 \mathrm{~m} / \mathrm{s}$ north is a velocity. The velocity $1.5 \mathrm{~m} / \mathrm{s}$ tells you that the object can travel 1.5 m in 1 s . The direction of motion is north.
a) If an object were moving across the table, what instruments would you need for measurements to determine if the object were traveling at $1.5 \mathrm{~m} / \mathrm{s}$ ? Describe how you would go about measuring velocity in your classroom.
2. Place a track flat on the top of your table. Place a steel ball in the track and give it a small push to get it moving along the track.

## 7.b)

Students should now be able to point out that the rider reacted to a greater degree when there was an acceleration, either as a change in speed, a change in direction, or both.

## 8.

The various possible units for acceleration are listed for the students. The unit meters per second every second should be
used primarily in the beginning until the students become more comfortable with the concept of acceleration. The unit $\mathrm{m} / \mathrm{s}^{2}$ should not be used until later.

Part C: Measuring Velocities and Calculating Accelerations
1.a)

You would need an instrument to measure distance and an instrument to measure time. Distance measurement
instruments could be rulers, meter sticks, or tape measures.

A shoe (roughly one foot long) could also be a measurement instrument. Time could be measured with a clock, a stopwatch, or your heartbeat.

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## 2.a)

Students should make the measurement and use the format for calculations that include the equation first written in words, then in symbols, substituting values into the equation with units, and finally calculating the result with units. For instance, if the ball has moved 25 cm in 4.0 s , a student would write the calculation as follows:
velocity $=$
displacement/time elapsed
$v=\Delta d / \Delta t$
$v=25 \mathrm{~cm} / 4 \mathrm{~s}=6.3 \mathrm{~cm} / \mathrm{s}$
The students should be prompted to say something about the direction of the velocity. Something simple like "north" or "east" or "toward the door" would be fine.

## 3.a)

Students should repeat the calculation with the ball, moving either more slowly or faster. Insist that students write the equation and show the calculation with the units. The students should again be prompted to say something about the direction of the velocity.


## 4.a)

The velocimeter is an accurate clock. It consists of two light beams (often invisible, infrared beams) a fixed distance apart that are interrupted by an object as it passes through. The time it takes the object to first intercept one beam and then the other is recorded. Since the distance between the beams is known, the velocity is just the distance between the beams divided by the
time taken to travel between the beams. Alternatively, a photogate with just one beam may be used. This device records the time during which the beam is interrupted.

## 4.b)

The length of the object traveling through the beam must be known to calculate the velocity using the length divided by the time.

You should have the students experiment with the velocimeter by interrupting the light beam when passing a small card through the beam and seeing how the reading is related to the motion of the card.

## 5.a)

The speed of the large steel ball is $6 \mathrm{~cm} / 2 \mathrm{~s}=3 \mathrm{~cm} / \mathrm{s}$.

## 6.

Be sure that the steel ball size is compatible with the size of the velocimeter's opening. The velocimeter will calculate the speed. Students could also calculate the speed by writing the equation, substituting the measured values of distance and time into the equation, and then displaying their answer with units.

## 7.a)

The speed can be measured near the top of the ramp and near the bottom of the ramp.

The increase in speed will be visible to the students. If only one velocimeter is available, the velocity at the top when first released can be used as zero, and the velocity at another point measured. Using a stopwatch to determine the time it takes the ball to go from start to the velocimeter or between velocimeters is sufficiently accurate for these purposes.

## 7.b)

The calculation of acceleration requires the students to know the speed at each location and the time between the measurements (i.e., the time for the ball to move down the incline). The students will use the reading on the velocimeter divided by the time of travel from the beginning or the difference between the readings on the velocimeters and the time to travel between velocimeters to determine the acceleration. For example, if the ball starts from rest (zero velocity) and the reading on the velocimeter is $2 \mathrm{~m} / \mathrm{s}$, the change in velocity is $2.0 \mathrm{~m} / \mathrm{s}$. If a stopwatch measures the time of travel from the beginning to the velocimeter to be 0.74 s , the acceleration is
acceleration $=$
change in velocity/change in time $a=\Delta v / \Delta t$
$a=2 \mathrm{~m} / \mathrm{s} \div(0.74 \mathrm{~s})=2.7 \mathrm{~m} / \mathrm{s}^{2}$

## Part D: Acceleration on the Roller Coaster-Pulling g's

## 1.a)

Students will probably know from experience that they will feel light as they go over the top of a hill, heavy at the bottom of a hill, and lighter at the top of a loop than at the bottom. They will feel lighter at B and G, and at the top of the loop between C and D . The will feel heavier at C and H . For a clothoid loop, the students should feel the same, heavier force all around the loop between C and D. They may also realize that they will be heavier going around the back loop and the horizontal loop as the direction changes.


The heavier and lighter feelings are related to their accelerations. The students should be able to recognize where accelerations (changes in speed or changes of direction) are taking place in the depicted roller coaster.

There are changes in speed from A to $B, B$ to $C, C$ to $D$ to $E, G$ to H , and during braking.

There are changes in direction from C to D to $\mathrm{E}, \mathrm{E}$ to F , and
during I. The roller coaster has accelerations due to speeding up from $B$ to $C$ and $G$ to $H$, slowing down from $F$ to $G$ and at $J$.
Between C and D , the students may think they will slow down on the way up the loop and speed up on the way down the loop. This would be true if it were not a clothoid loop. Do not discuss this point yet.


## Physics Talk

This Physics Talk defines important terms needed to understand velocity and acceleration. Students read the difference between distance and displacement, and speed and velocity, before arriving at a definition of acceleration. The distinction between distance and displacement, between speed and velocity and between velocity and acceleration becomes particularly important when students have to make calculations to understand various aspects of the roller-coaster ride. To help students understand the fine distinction between distance and displacement, discuss the definition of each term and ask them to explain the two terms in their logs by giving examples. Students should be able to describe why distance is a scalar quantity and displacement is a vector. Similarly, students should be able to describe the difference between speed and velocity and point out that speed is a scalar quantity while velocity is a vector.

The concept of acceleration also has nuances that might confuse students. For the purpose of clarification, provide practice by having groups of students come up with examples of acceleration. Have each group listen to the example and respond with the correct terminology. Write students' examples of acceleration on the board and emphasize the steps of the Investigate, where students varied the speed and direction of the blindfolded rider and the ball on an inclined track to calculate acceleration.

## Checking Up

## 1.

Distance is a scalar quantity and only represents a certain length that can be measured with a piece of string or a metric tape measure. Displacement is the total distance covered with the direction included. Displacement depends only on the endpoints and not on the detailed path. Displacement is a vector quantity.

## 2.

Your displacement is zero.

## 3.

Speed is the distance covered by the time elapsed. Speed is a scalar quantity. Velocity is the total displacement divided by the time elapsed. Velocity is a vector.

## 4.

You can find the acceleration of an object by measuring its velocity at two different times, then divide this difference by the time interval between the two velocity measurements.

Chapter 4 Thrills and Chills

Physics Words acceleration: the
change in velocity
divided by the time
elapsed; acceleration
is a vector quantity, it and direction.

Checking Up

1. Explain the difference between distance and displacement.
2. You went to school and back home, of 2 km . What is your displacement?
your displacemen
3. What is the difference between
4. How can you find of an object?

This is the method you used to measure the speed of the ball in the investigate. If you also recorded the direction in which the ball was moving, then you have the information needed to describe the ball's velocity.
for a person walking one lap around a city block, the distance is equa to the perimeter of the city block. The speed is equal to this distance divided by the time to complete the walk. The displacement for the entire trip equals zero (since the person ended up where she started) and the velocity equals zero as a result.
You will find that in some cases it is distance that is important and in other cases displacement is important. It will be important to keep the difference between the two ideas in mind. It may seem that defining both distance and displacement as well as speed and velocity complicates things. However, scientists occasionally introduce terms and distinctions that seem to make simple things more complicated because they are then able to make very difficult things much easier to explain and understand.

Acceleration is the change in velocity divided by the time elapsed. An object's acceleration may be $5 \mathrm{~m} / \mathrm{s}$ per second. If the direction stays the same, this means that the object changes its speed by $5 \mathrm{~m} / \mathrm{s}$ every second if it continues with the same acceleration. The speed will increase from $0 \mathrm{~m} / \mathrm{s}$ to $5 \mathrm{~m} / \mathrm{s}$ to $10 \mathrm{~m} / \mathrm{s}$ to $15 \mathrm{~m} / \mathrm{s}$ with each change requiring one second. The acceleration of $5 \mathrm{~m} / \mathrm{s}$ every second is also written as $5 \mathrm{~m} / \mathrm{s}^{2}$ (five meters per second squared).

The equation to calculate acceleration is
acceleration $=$ change in velocity time elapsed
$a=\frac{\Delta v}{\Delta t}$,
where $a$ is the acceleration
$\Delta v$ is the change in velocity, and
$\Delta t$ is the time elapsed
Note that the acceleration (a vector quantity) will be in the direction of the change in velocity.
When you measured the acceleration of the ball rolling down the incline in the Investigate, you measured the velocity of the ball at two different times. The acceleration is then given by the change in velocity divided by the time interval between the two velocity measurements. In Active Physics Plus, you will explore acceleration when the direction of the velocity changes.


## b)

The value of the acceleration is found by using

$$
a_{\text {average }}=\Delta v / \Delta t=1.4 \mathrm{~m} / \mathrm{s}^{2} .
$$

## c)

To find the angle between $\Delta v$ and east use either a protractor or one of the trigonometric functions of sine, cosine or tangent. The angle will be $37^{\circ}$ west of south.
d)


Given:
$v_{\mathrm{i}}=4 \mathrm{~m} / \mathrm{s} ; v_{\mathrm{f}}=-3 \mathrm{~m} / \mathrm{s} ; \Delta t=2 \mathrm{~s}$
$\Delta v=\sqrt{\left(-v_{\mathrm{i}}\right)^{2}+\left(v_{\mathrm{f}}\right)^{2}}=$
$\sqrt{(-4 \mathrm{~m} / \mathrm{s})^{2}+(-3 \mathrm{~m} / \mathrm{s})^{2}}=5 \mathrm{~m} / \mathrm{s}$
$a=\Delta v / \Delta t=(5 \mathrm{~m} / \mathrm{s}) / 2 \mathrm{~s}=2.5 \mathrm{~m} / \mathrm{s}^{2}$
Using a protractor, the angle will be $53^{\circ}$ to the south of west.

## What Do You Think Now?

The What Do You Think? questions are revisited in this section and students have a chance to update their responses. Discuss how their investigations have helped them to develop their understanding of velocity and acceleration and why they should now be able to answer which part

of the roller coaster-ride produces the loudest screams. You might want to provide them with an answer to A Pbysicist's Response. Ask students if the What Do You See? illustration now becomes more relevant. Students will continue to benefit from a review of previously recorded responses.


## Reflecting on the Section and the Challenge

Students should now reflect on the Terminator Express roller coaster design that they have to modify for their Chapter Challenge. Ask them to revisit the main physics concepts presented in this section. Discuss the roller coaster experience that students simulated in the Investigate. Have a student read this section aloud in the student text. Remind students that they have to keep the safety factor in mind while making variations to the Terminator Express.

## Physics Essential Questions

## What does it mean?

Speed is the total distance traveled in a given time. Velocity is the total displacement traveled in a given time. The velocity includes the direction. If the ball were to travel up and down the ramp, the average speed for the entire trip would have a positive value, but the average velocity would be zero, since the net displacement is zero. Acceleration is the change in velocity with respect to time.
How do you know?
Students looked surprised when there was acceleration. This occurred with changes in speed and/or direction.

Why do you believe?
The speedometer could be connected to a GPS, which would take into account the direction of motion as well as the speed.
Why should you care?
When you enter a highway, your car must accelerate to reach the same velocity as the traffic. When purchasing a car, you want to know that it can travel at a speed of $60 \mathrm{mi} / \mathrm{h}$, but you also want to know that it can accelerate to this speed quickly. It's great to travel fast on a roller coaster, but the thrills come from changes in velocity-the acceleration. The rollercoaster design should include places where there are large accelerations.

## Physics to Go

1. 

Student diagrams should resemble the ones below:

2.

The biggest thrill will probably be in the clothoid loop. This is where the riders are experiencing an acceleration due to a change in speed with respect to time and an acceleration due to a change in direction. They are also upside down for a few moments.

## 3.a)

La Paz, Bolivia has the greater speed. Oslo, Norway has moved a much smaller distance in the 24 hours.

## 3.b)

## Given:

$d=40,000 \mathrm{~km} ; t=24 \mathrm{~h}$
The speed is approximately $1700 \mathrm{~km} / \mathrm{h}$ (close to $1000 \mathrm{mi} / \mathrm{h}$ ). speed $=$ distance traveled/time speed $=40,000 \mathrm{~km} / 24 \mathrm{~h}=$ 1667 km/h


## 3.c)

Thrills are produced by changes in velocity. As Earth rotates, the speed of a place on the surface (relative to the center of Earth) does not change significantly.

The direction of the velocity does change (because the location is in circular motion) but the resulting acceleration is very small. This point need not be raised now.


## 4.

Given:
$v_{\mathrm{f}}=16 \mathrm{~m} / \mathrm{s} ; v_{\mathrm{i}}=4 \mathrm{~m} / \mathrm{s} ; \Delta t=3 \mathrm{~s}$

## acceleration $=$

change in velocity/time elapsed $a=\Delta v / \Delta t=(16 \mathrm{~m} / \mathrm{s}-4 \mathrm{~m} / \mathrm{s}) / 3 \mathrm{~s}=$ $(12 \mathrm{~m} / \mathrm{s}) / 3 \mathrm{~s}=4 \mathrm{~m} / \mathrm{s}^{2}$
$\frac{\text { 5.a) }}{\text { Speed—a scalar (no direction) }}$

## 5.b)

Velocity-a vector (speed with a direction)

## 5.c)

Acceleration-a vector (a change in velocity with respect to time)

## 5.d)

Displacement-a vector (has direction)

## 5.e)

Displacement-a vector (has direction)

## 6.

Given:
$d=10 \mathrm{~cm} ; t=2 \mathrm{~s}$
speed $=$
distance traveled/time elapsed $=$ $10 \mathrm{~cm} / 2 \mathrm{~s}=5 \mathrm{~cm} / \mathrm{s}$

## 7.

Going at the same speed, half the distance will take half the time or 1 s .

## 8.

Given:
$\Delta v=25 \mathrm{~m} / \mathrm{s} ; t=10 \mathrm{~s}$
acceleration $=$
change in velocity/time elapsed
$a=\Delta v / \Delta t=$
$(25 \mathrm{~m} / \mathrm{s}-0 \mathrm{~m} / \mathrm{s}) / 10 \mathrm{~s}=2.5 \mathrm{~m} / \mathrm{s}^{2}$
9.

The history of science provides many examples of simple things being explained in a complicated way so that other things will be easier to explain. The Sun appears to move across the sky. To explain this simple observation as the complicated perceived motion of the stationary Sun from a rotating Earth allows us to then explain the solar system. In a student's everyday life, they may recognize that to learn certain moves in sports or dance, that they make a simple move more complex so that they will have good form and be able to be successful with complicated moves.

## Preparing for the Chapter Challenge

## 10.a)

You may want to have smaller heights, gentler curves and smaller changes in acceleration. These changes should be made so that preschool children don't get terrified and enjoy the smaller variations in speed and direction.

## 10.b)

Students' drawings will vary. However, their drawings should show the changes suggested.

## Inquiring Further

This Inquiring Further will be a moving target, since new roller coasters are constantly being built. The most modern (steel roller coasters) are constantly being improved, and new innovations are being tried. Roller coasters where the riders are suspended below the track are becoming more common rather than the more conventional rollercoaster car.

The typical twists, drops and turns of historic roller coasters have been retained, but loops have generally been added that were not available to the older wooden roller coasters.

Steel roller coasters are usually much higher, quieter, smoother and faster than the traditional wooden roller coasters of 50 years ago. The wooden coasters were often deliberately made to creak and shift slightly to add to the thrill, since the velocities were lower.

NOTES

## NOTES

## SECTION 1 QUIZ

## 4-1b Blackline Master

1. The diagram below shows a side view of a section of a roller coaster.


Which of the following views could be a top view of this section?

c) $\qquad$

d)

2. To accelerate, an object must
a) change its speed.
b) change its direction.
c) either change its speed or its direction.
d) change both its speed and direction.
3. A steel ball rolls across a level track a distance of 1.35 meters in a time of 0.45 seconds. What is the velocity of the ball?
a) $0.33 \mathrm{~m} / \mathrm{s}$
b) $1.80 \mathrm{~m} / \mathrm{s}$
c) $3.0 \mathrm{~m} / \mathrm{s}$
d) $0.61 \mathrm{~m} / \mathrm{s}$
4. A student does an experiment rolling a cart down a ramp. The cart starts from rest a distance 0.80 m up the ramp, and 1.5 s later the cart has a velocity of $2.0 \mathrm{~m} / \mathrm{s}$. What is the cart's acceleration?
a) $1.2 \mathrm{~m} / \mathrm{s}^{2}$
b) $1.3 \mathrm{~m} / \mathrm{s}^{2}$
c) $3.0 \mathrm{~m} / \mathrm{s}^{2}$
d) $4.5 \mathrm{~m} / \mathrm{s}^{2}$
5. A cart that is 16 cm in length passes through a velocimeter. The reading on the velocimeter says the cart's velocity was $4.8 \mathrm{~m} / \mathrm{s}$ during the time it took to pass through the meter. How long did it take the cart to pass through the meter?
a) 0.033 s
b) 0.25 s
c) 3.0 s
d) 0.77 s

## SECTION 1 QUIZ ANSWERS

(1) d) Since there is a loop in the track, the two halves of the loop cannot overlap, ruling out choice c). From a top view, only choices d) and c) would be possible for a straight-line run.
(2) Acceleration is defined as the change in velocity with respect to time. Velocity has two components-speed and direction. Changing either one would change the velocity, thus causing an acceleration. It is not necessary to change both factors; changing either one is sufficient to have an acceleration.
(3) Velocity is defined as the change in displacement with respect to time. If the displacement change (in this case the distance since it is in a straight line) is 1.35 m and the change in time is 0.45 s , then $v=\Delta d / t=1.35 \mathrm{~m} / 0.45 \mathrm{~s}=3.0 \mathrm{~m} / \mathrm{s}$.
(4) b) Acceleration is the change in velocity with respect to time. Using the formula, $a=\Delta v / t$ gives $(2.0 \mathrm{~m} / \mathrm{s}) /(1.5 \mathrm{~s})=1.3 \mathrm{~m} / \mathrm{s}^{2}$. As long as the cart starts up the ramp a distance sufficient for it to continue uniformly accelerating, the distance is not relevant in this case.

5 a) Using speed equals distance divided by time, if the cart has an average speed of $4.8 \mathrm{~m} / \mathrm{s}$, and is 0.16 m long yields $v=\Delta d / t$ or $4.8 \mathrm{~m} / \mathrm{s}=(0.16 \mathrm{~m}) / t$. Solving for $t$ gives $(0.16 \mathrm{~m}) /(4.8 \mathrm{~m} / \mathrm{s})=0.033 \mathrm{~s}$.

