## SECTION 1

## Static Electricity and Coulomb's Law: Opposites Attract

## Section Overview

Students investigate the behavior of electrically charged objects by bringing two strips of charged tapes near each other and observing the forces of attraction and repulsion between them. They charge the tapes by folding and labeling the ends, then pressing them together and pulling off the top tape. Students also charge a plastic rod or styrene foam with wool and bring it near the charged tapes to observe what happens to the tapes. They also describe how charged objects are neutralized by adding or removing electrons and investigate the force of attraction due to charge redistribution between charged and neutral objects. Subsequently, students read about the principle for conservation of charge, calculate the electrical force using Coulomb's law, and compare Coulomb's law to Newton's law of universal gravitation.

## Background Information

Understanding the electrostatic force between charges is crucial for explaining how atoms are held together. It is also the basis of chemical bonding. There are two types of charges, positive and negative. Like charges repel and unlike charges attract. In the everyday interaction of objects, it is the electrons-the negative charges-that get exchanged between objects. An excess of electrons accounts for a negative charge, while a deficiency of electrons accounts for a positive charge.

There are few conserved quantities in nature. The conservation of electric charge is one of these. The total charge in a closed system remains the same. The charges can be exchanged, but the total charge before an interaction must equal the total charge after the interaction.

In 1784 , Charles Augustus Coulomb experimentally determined the equation for electric forces. Coulomb's law describes the forces between charges. The force is proportional to the charges and inversely proportional to the square of the distance between the charges.
$F=k q_{1} q_{2} / d^{2}$
where $F$ is the force in newtons $(\mathrm{N})$,
$q_{1}$ and $q_{2}$ are charges in coulombs (C),
$d$ is the distance between the centers of the charges in meters, and
$k$ is Coulomb's constant and always equal to $9 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}$.

The similarity between Coulomb's law and Newton's law of gravitation hints at an underlying symmetry of nature. The investigation of symmetries like this (often on a more subtle mathematical level) drives much physics research.

## Crucial Physics

- Atoms are composed of smaller particles that may have an electric charge. The electric charge on the electron is defined as being negative, while the charge on the proton is said to be positive.
- The magnitude of the charge on electrons and protons is equal.
- Static electric charge comes in two forms. An object gains a negative charge by having an excess of electrons and gains a positive charge from a deficiency of electrons.
- Charges that have the same sign (positive or negative) repel one another, while charges of opposite signs attract.
- Coulomb's law describes the force between charged particles. The force between two charged objects $(F)$ depends upon the product of the charges ( $q_{1}$ and $q_{2}$ ), and is inversely proportional to the square of the distance between the charges $(d)$. This is expressed mathematically as $F=k q_{1} q_{2} / d^{2}$. Coulomb's law for the force between two charges is very similar to the law of universal gravitation, which describes the gravitational force between two masses; however, gravitation is only attractive.
- When charge is passed from one object to another, the total amount of charge on the two bodies is conserved.
- Objects may be charged either by passing charge from one object to another, or by inducing charge redistribution on another body when a charged object is brought near by (induction).

| Learning Outcomes | Location in the Section | Evidence of Understanding |
| :--- | :--- | :--- |
| Produce electrically charged <br> objects. | Investigate <br> Steps 1 and 4 | Students press two strips of invisible tape together, and <br> then separate them to create oppositely charged objects. <br> They also rub a rod or a piece of styrene foam with wool to <br> produce a net charge on each object. |
| Describe the behavior of like <br> charges, and the behavior of <br> unlike charges. | Investigate <br> Steps 2-8 <br> Physics Talk | Students bring the electrically charged objects near each <br> other and describe the charges as like or unlike, depending <br> on whether they attract or repel each other. <br> Students read how charged objects behave and solve <br> problems that explain how like and unlike charges behave <br> when brought near each other. |
| Discover the factors that <br> determine the force between <br> two charged objects. | Physics to Go <br> Questions 1-20 | Steps 2-8 <br> Physics Talk |
| Calculate the electrical forces <br> using Coulomb's law. | Physics Talk <br> Physics to Go <br> Questions 5, 6, 11, and 12 | Students compare and contrast forces of attraction <br> and repulsion between charged objects and how the <br> magnitude of charges and the distance between them <br> affects the strength of those forces. |
| Implement the organizing Physics Talk <br> principle of conservation  <br> of charge.  | Physics to Go <br> Questions 1-4, and 18-19 | Students calculate electrical force by solving problems <br> using Coulomb's law. |
| Recognize the similarities <br> and differences between <br> Coulomb's law and Newton's <br> law of gravitation. | Physics Talk | Student read how charge is conserved between two <br> electrically charged spheres that are brought in contact <br> and then separated using the overall net charge before <br> and after contact as a constant. |
| Explain how Coulomb was able <br> to measure the electrostatic <br> constant using a torsion balance. | Physics Talk | Students recognize that electrical forces can be attractive <br> or repulsive since charges are either positive or negative. <br> Gravitational forces are only attractive since mass only <br> comes in one variety. The constants that determine the <br> magnitude of the forces is much larger for electrical forces <br> than gravity. |

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## Section 1 Materials, Preparation, and Safety

## Materials and Equipment

| PLAN A and PLAN B |  |  |
| :---: | :---: | :---: |
| Materials and Equipment | Group (4 students) | Class |
| Rod, friction, plastic | 1 per group |  |
| Pad, wool | 1 per group |  |
| Tape, transparent, adhesive | 1 per group |  |
| Paper, single sheet* | 1 per group |  |

*Additional items needed not supplied

## Time Requirements

- Allow one class period or 45 minutes for the Investigate.


## Teacher Preparation

- If not already available, obtain one roll of "transparent" cellophane tape for each lab group.
- One pack of styrene-foam plates (available from a supermarket) should be sufficient for all the groups, and can be reused for other classes.
- Test the cloth you are using to charge the styrenefoam plates to ensure that it is able to develop a charge. If an electroscope is available, it would serve as a charge detector. If other charging apparatus is to be used, try it out first with the tapes to ensure that it functions in the desired manner.
- Search the Internet to find a Web site that has an animation of electrostatics and charged objects that can be shown to the students.


## Safety Requirements

- A careful examination of the voltages developed in even small static experiments would indicate that high voltages are being generated. In this experiment, however, the voltages are both small, and the total energy available is so low that it does not present a hazard of students receiving an electric shock.


# Meeting the Needs of All Students Differentiated Instruction: Augmentation and Accommodations 

| Learning Issue | Reference | Augmentation and Accommodations |
| :---: | :---: | :---: |
| Following written directions | Investigate <br> Step 1 <br> Investigate <br> Steps 3, 4, 6, and 8 | Augmentation <br> - Students who struggle with reading, visual processing, and/or maintaining attention to a task often have a difficult time following written directions, especially those written in paragraph form. An alternate way to present these directions in written form is to provide a numbered list. This allows students to complete one simple step at a time and to check off steps as they proceed. <br> - When preparing the strips of tape, it may also be helpful to ask a student to read the directions aloud while the teacher models the process once for the whole group. Students have a difficult time understanding how to make a tab and label the tape. They often press the entire piece of tape onto the table and find it difficult to remove it. Having a visual model paired with auditory directions helps many students. <br> Accommodation <br> - For students who struggle to follow a set of directions and may take a long time to set up the tape, provide ready-made sets of tape for them to pull off of the table. This will allow students to focus on the investigation and the concepts instead of wasting a lot of time playing with tape. |
| Understanding vocabulary | Investigate <br> Steps 2.c) and 5 | Augmentation <br> - Some students will not know the meanings of the words "attractive" and "repulsive." There are a number of ways to help students understand these two words. Ask them to find the words in their science text or a dictionary. Show them two objects that are attracted or repelled and ask them to describe the action of the objects. <br> - Ask students to show their hands repelling and attracting. Pairing auditory, visual, and kinesthetic cues helps all students remember these words. |
| Estimating distances | Investigate <br> Step 3.b) | Augmentation <br> - Students who struggle with visual/spatial tasks have a difficult time estimating measurements. Ask students to find common objects that they could measure and use to help them estimate. For example, a paper clip may be three centimeters long or a penny may be two centimeters wide. Students can also create their own cardboard squares for a few different measurements and use those tabs to help with estimation. <br> - It may also help these students to actually use a ruler and measure the distance, knowing that the measurements may not be extremely accurate but more accurate than a poor estimation. <br> - Pair students strategically to help students who struggle with estimation. <br> Accommodation <br> - Seeing this part of the investigation as a demonstration in a smaller group may help some students focus on the distances as opposed to focusing on maneuvering the tape. |


| Learning Issue | Reference | Augmentation and Accommodations |
| :---: | :---: | :---: |
| Understanding the transfer of electrons | Investigate Steps 6, 8, and 9 <br> Physics Talk <br> Physics to Go <br> Questions 1, 2, <br> 18 , and 19 | Augmentation <br> - Because students are unable to see electrons, they may not have an idea how the negative charges are transferred. Some students may need to see a visual representation of an atom to be able to make sense of charge transfer. Though the structure of an atom will be discussed further in later sections, it is important that deductive learners have the big picture in their mind. <br> - Ask students to draw pictures to represent the transfer of negative charges from the wool to the foam. This visual representation will make clear some misconceptions students may have about the transfer of charges. <br> Accommodation <br> - Provide drawings of the transfer of charges to make an object positively or negatively charged. As students show increased understanding of this concept, require increased independence in making charge transfer drawings and describing the process of transferring charges. |
| Solving problems to find electric force | Physics Talk <br> Active Physics Plus <br> Physics to Go Questions 5 and 6. | Augmentation <br> - Students who struggle with mathematical calculation have a difficult time with the formula for electric force because it contains a constant with a challenging SI unit, distance is squared, multiplication and division are required, and scientific notation is used. One strategy that is used to help students practice a new skill is to show them how to do one problem from start to finish. Next, ask them to guide the teacher through doing a second problem and clarify any misunderstandings. Then require that all students complete a third problem independently. <br> - Students may need to learn or review scientific notation. They may also need to learn how to do calculations with exponents on their calculators. Taking the time to review these skills will build confidence and allow more students to successfully solve for electric force. <br> Accommodation <br> - There are students who may be unable to solve problems for electric force. For example, if a student is still struggling to multiply and divide, these problems will be very challenging. For these students, focus on the conceptual ideas of attractive and repulsive forces and how they are affected by charge and distance. |
| Conceptually understanding Coulomb's law | Physics Talk <br> Physics to Go Questions 9, 10, 14,15 , and 17 | Augmentation <br> - Students who struggle with mathematical relationships and number sense will need help understanding the direct relationship between electrical force and charge and the inverse square relationship between electrical force and distance. One method to help students understand these concepts is to use a kinesthetic model. Two or three students hold signs with a positive or negative number to represent their relative charges and use meter sticks to represent the distances between them. Then a small group or the whole class decides which direction the charges will move based on the effects of charge and distance. It is helpful if the students who are struggling to understand the concept are the students who represent the charges. <br> - Help students see the direct and inverse mathematical relationships by using small whole numbers to represent the charges and the distance and solve for electrical force in terms of $k$. This allows students to make more sense of what will happen if charge is doubled or what will happen if distance is doubled. |

## Strategies for Students with Limited English-Language Proficiency

| Learning Issue | Reference | Augmentation |
| :---: | :---: | :---: |
| Vocabulary comprehension | Investigate Step 1 | Learning to use context to figure out the meaning of unfamiliar words and phrases is an important skill for all readers, including ELL students. Notice how students deal with the phrase "smooth out the creases." Other words in the sentence, "rubbing your finger over the strips a few times," should be sufficient to help students determine the meaning of both "smooth out" and "creases." |
| Comprehension | Investigate <br> Step 2.b) | Students may benefit from a quick review of Newton's second law. Discuss what it means to be "in agreement" with a law. Make it clear that the agreement is between the observations and the interactions predicted by Newton's second law, rather than the more familiar context of an agreement between two people. |
| Identifying parts of speech | Investigate <br> Step 2.c) | Students have previously encountered the terms "attract" and "repel," most recently when dealing with magnets. Here, check that they understand the adjectival forms "attractive" and "repulsive." |
| Understanding concepts <br> Vocabulary comprehension | Investigate <br> Step 5.a) | Making inferences is a higher-level reading skill. When learning a new language, ELL students may not pick up on subtleties that indicate a connection between two bits of information. Be sure students understand that "this law of electrostatics" refers to "opposite charges attract and like charges repel." Students may be familiar with the term "static," but most likely have not seen it used as a word root in a term like "electrostatics." Help students deconstruct the meaning of this term. |
| Vocabulary comprehension <br> Identifying parts of speech | Investigate <br> Step 9.b) | Students will likely recognize the word "sink" but may not have encountered the meaning found here. Tell students that in English, many words have more than one meaning. Students may have heard of a "heat sink," which is used, for example, to draw heat away from electronic components. <br> The terms "ground," "grounding," and "grounded" may have syntax that seems odd for students. Students may be puzzled about the active voice in a phrase like "when the ground removes electrons." Most people do not think of the ground as a noun that initiates action. The verb form can also be confusing. You can ground an object by just touching it or by touching it to a ground. Also, an object can "be grounded." Because so many different variations occur with this verb, the meaning may need to be discussed at length. |
| Understanding concepts | Physics Talk Static Charges and Forces | Hold a class discussion about "visible and measurable effects." Be sure students understand that scientists frequently use such effects to prove the existence of and explain the behavior of various unseen phenomena. Remind students that they have already learned about two such phenomena in their studies this year: gravity and magnetism. |
| Vocabulary comprehension | Physics Talk Conservation of Charge | Work through the idea of conservation of charge with the class. To help students understand the concept, you may wish to review the law of conservation of energy. But unlike energy, which can change form, charge does not change form. The total amount of negative charge remains constant, and the total amount of positive charge remains constant. Also, be sure students do not think that matter with a neutral charge has no charge. Neutral matter can be loaded with charge, but as long as the amount of positive charge equals the amount of negative charge, matter has a neutral charge. Finally, challenge students to use context to determine the meanings of "excess" and "deficiency." |

## SECTION 1

Teaching Suggestions and Sample Answers

## What Do You See?

The images in this illustration are likely to elicit an immediate reaction from students. The bolts of lightning outside and the obvious effects of the electric discharge detected by the person holding the microphone provides interesting points of discussion. You might want to prompt students to notice that the lightning streaks are toward the ground, rather than from cloud to cloud. Encourage them to relate their impressions of what the artist is trying to convey and suggest that they return to the What Do You Think? question once they have advanced further in this section. Use an overhead of this illustration to highlight different aspects of the visual.


## Students' Prior Conceptions

This section reviews what students think they understand about the nature of matter and how charges are created or transferred among various objects. You should look for students to seek consistent explanations dealing with the production of electrically charged objects and how the forces between two objects make them behave. Attending to the following prior conceptions sets the stage for eradicating misconceptions in other sections of this chapter.

1. Friction is necessary to create static electricity. This belief is erroneous because static charges appear whenever two dissimilar insulating objects touch each other. Chemical bonds form between the two surfaces and if atoms in one of the objects hold electrons more tightly than the second object then the first object takes charged particles from the second object upon immediately touching each other. You can emphasize this phenomenon between dissimilar objects,
such as sticky tape and table tops. You may also emphasize that merely standing on a rug in stocking feet is sufficient for the existence of an imbalance in charge between the stockings and the rug. Students need not slide across a rug to touch a metal doorknob and receive a "static shock."
2. Neutral objects have no charge. It is essential for you to review the structure of atoms to reinforce that all atoms contain both positive and negative charges. Atoms are electrically neutral because these charges are balanced-the number of electrons in the atomic orbits equals the number of protons in the nucleus.
3. Protons are mobile like electrons. As you focus on the structure of the atom, emphasize that the electrons are the mobile constituents of atoms; only under extreme nuclear reactions are protons involved in reactions that transfer charge.

Consider reading the title aloud and asking students to make connections between the title and the stormy scenes depicted in the visual.

## What Do You Think?

The introductory paragraph of this section has several questions that prompt students to think about what caused them to feel a shock. The questions provide you an opportunity to start a discussion that should help students to respond with confidence. Emphasize that at this stage it doesn't matter whether an answer is accurate, the purpose of What Do You Think? is to set the stage for the Investigate that follows after they have recorded their answers in their logs. Given the freedom to express their ideas without being concerned about a grade reveals the prior conceptions students might have and will help you address these conceptions at appropriate times during the lesson. Encourage students to connect the What Do You Think? question to why people sometimes feel a shock when they touch something.

## Teaching Tip

If students' hands are oily, cleaning them with a few drops of commercial alcohol-based hand sanitizer will allow for better results with the tapes.

## Investigate

## 1.

Students cut the two $12-\mathrm{cm}$ long strips of invisible tape, fold the ends, label them, and press them together. They peel off the top strip by pulling up its tab.

## What Do You Think?

## A Physicist's Response

The lightning outside caused the shock by transferring a large charge from cloud to the ground. Flashes of lightning and small shocks one gets from shuffling across a carpet differ only in scale. Students probably received electric shocks from carpets when they were indoors-more likely in the winter when the air was dry. Rubbing shoes against a dry carpet often builds up a charge on the walker, who may then touch a doorknob, a light switch, or another person.
4. A positively charged object gains protons. The key idea for you to emphasize is that only the electrons are mobile during ordinary chemical interactions and reactions. It is the loss and gain of electrons that makes an object carry a positive charge or a negative charge.
5. Static electricity is the build-up of electrons. This prior conception is false because it is the imbalance of charge between two objects that leads to a static build-up and the discharge of an electric "jolt," such as the discharge depicted in the picture in the Physics Talk. The central concept for teachers to emphasize is the imbalance of charge.
6. Students fail to recognize that charge is conserved. When students are explaining what happens with the strips of tape, and what happens when charge is shared between objects that are able to conduct electricity, be sure that students are considering the total charge on an isolated system.

The distribution of charge may change but the total charge is conserved.
7. As students compare Newton's law of gravitation with Coulomb's law, they might believe that the electrical force is the same as the gravitational force. A corollary to this misconception is that the gravitational force is stronger than the electrical force. Have students observe the reaction between small bits of paper and one of the charged strips of tape. The paper bits will "jump up" to the charged tape, demonstrating that the force of gravity is the weaker force. Emphasize that the Coulomb force is both an attractive and a repulsive force whereas the force of gravity is only an attractive force. You should also emphasize that the value for the gravitational constant, $G$, is a small number, whereas the value for Coulomb's constant, $k$, is a large number.

## 2.a)

The two strips will attract each other.

## 2.b)

The two strips did not hang straight down but accelerated toward each other. The fact that they accelerated toward each other at first and then were stationary once equilibrium of forces was attained is in agreement with Newton's second law.

## 2.c)

The force was attractive.

## 3.

Students should set up an experiment to see what occurs when two top strips, two bottom strips, and combinations of top and bottom strips are brought near one another. $\mathrm{T}_{1}$ should be brought near $\mathrm{B}_{1}, \mathrm{~B}_{2}$, and $\mathrm{T}_{2}$. Then $\mathrm{B}_{1}$ brought near $\mathrm{T}_{1}, \mathrm{~B}_{2}$, and $\mathrm{T}_{2}$ and so forth until all combinations have been tried.

## 3.a)

Students should record their observations in a table. The table may look like the one shown below:


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## 3.b)

Distance affects the magnitude of the force. The closer the strips, the more they will attract or repel. Estimates of distance measurements will vary with the students doing the investigation, the weather conditions, the tape used, etc.

## 4.a)

Students record their observations. The styrene foam will also attract the top tapes and repel the bottom tapes.

> Teaching Tip
> Many materials will reliably develop static charges for testing. PVC pipe rubbed with wool is a long lasting and inexpensive alternative to the styrene-foam plates, as well as things such as the golf tubes that are inside golf bags, and the plastic covers that fit over fluorescent lights. For additional material that develops both positive and negative charges, consult the triboelectric series, a list that ranks various materials according to their tendency to gain or lose electrons. This can be found on the Web.

## 4.b)

To compare the forces, students will have to ensure that the distances between a charged tape and the styrene foam or plastic rod are the same as the previous distances between tapes. The forces between the styrene foam or plastic and the tape should be greater than the force between tapes due to the larger charge on the styrene foam or plastic rod.

## 4.c)

The magnitude of the charge on the plate compared to the tape will also affect the size of the force.

## 5.a)

Using the concept that opposite charges attract and like charges repel, students should conclude that when pairs of strips ( $\mathrm{T}_{1}$ and $\mathrm{B}_{1}$ ) attract, they must have opposite charges. When top or bottom pairs of strips are brought together ( $\mathrm{T}_{1}$ and $\mathrm{T}_{2}$ or $\mathrm{B}_{1}$ and $\mathrm{B}_{2}$ ), they repel. This implies they have like charges.

## 5.b)

Students should conclude that the styrene foam has the same charge as the bottom tapes, since it repels them.

## 6.a)

The positives on the T tapes came from transferring electrons to the B tapes.

## 6.b)

Because the B tapes gained electrons, they must have a net negative charge.

## 6.c)

One possible test is to use the wool, which transferred electrons to the styrene foam, leaving it with a net positive charge. When the wool is brought near the bottom tape, it should attract the tape with negative charge.

## 7.a)

The force of attraction between the styrene foam and the pieces of paper must be stronger than the force of gravity between the paper and Earth.

## 8.a)

Students should find that their finger attracts both tapes by induction.

Chapter 8 Atoms on Display
5. You have probably heard the phrase "opposites attract." Opposite charges attract and like charges repel.

دa) Using this law of electrostatics, explain the results of your inquiry investigation when pairs of strips (for example, T1 and B1) were placed near each other.
What did your investigation tell you about the relative charges on the different tapes?
Db) Using this law of electrostatics, explain the results of your inquiry investigation when the styrene foam or plastic rod was used.
6. Rubbing the foam transfers negative charges (electrons) from the wool to the foam, giving it an overall negative charge and leaving the wool with a shortage of electrons (a positive charge).

دa) Where did the positives on the T tapes come from?

Db) How would that affect the charge on the B tapes? Explain how your observations confirm your idea.
Dc) Think of another test to determine that B tapes are negative. Try the test and record your observations.
7. Use the charged styrene foam or plastic rod to pick up a tiny piece of paper.
دa) Compare the force of electrical attraction between the styrene foam and the piece of paper with the gravitational force of attraction between Earth and the paper.
8. Recharge the original two strips of tape as in Step 1. Place them back on the table edge. Bring your finger close to each tape.

دa) Describe your observations.
$\Delta$ b) Like charges repel, and unlike charges attract. How would you explain the interaction between the charged pieces of tape and your finger? (Hint: The electrons in your finger are able to move about so that some are able to move closer to or further away from each charged tape.)

Use a diagram to help you explain your observations. Remember, when some electrons leave an area it becomes more positively charged.
9. Investigate if it is possible to remove the charge from the charged styrene foam or plastic rod tube by touching it.
دa) If the charged object had an excess of negative charges, describe how they could have gone from the tube to your finger and then through your body to the ground. (You may have to move your hand around to different places while touching the object.)

Db) Adding or removing electrons to restore a charged object to neutral is called grounding. By taking the negative charges from the plastic rod, you grounded it. Describe what happens when a positively charged object is grounded.
8.b)

Because a finger attracts both the top (positive) tape and the bottom (negative) tape, the finger must have the charge opposite to each tape. Electrons in the finger are able to move, so when the finger is brought near the top tape, the electrons are drawn toward the positive charges in the tape. This makes the fingertip negative, leaving the back of the hand positive. Because the negative
fingertip is closer than the positive back of the hand there is a net attractive force, which attracts the positive tape. The electrons in the fingertip are drawn from further back in the finger, leaving that part positive. The first diagram on the next page shows what the charges would look like.


finger tip

When the finger is brought near a negative (bottom) tape, the opposite process occurs, as shown in the diagram below:


## 9.a)

For the negatively charged styrene foam, the electrons would repel each other, and pass through the hand and arm down to the ground (which is able to store large numbers of electrons), leaving the styrene foam with almost no charge. Because styrene is an insulator, students will probably have to rub the foam with their hand to get all the charge to move from the styrene to their hand.

## 9.b)

When a positively charged object is grounded, the positive charges draw electrons up from the ground through your arm, to neutralize the positive object.

## Physics Talk

Students understand the presence of invisible forces on different objects. They correlate their findings in the Investigate with the evidence of visible and measurable effects. They read how electrons were discovered. The Physics Talk also explains the process of grounding and how charge is conserved. Students further relate the behavior of charged objects to Coulomb's law and compare Coulomb's law to Newton's law of universal gravitation.

The idea of invisible forces may present prior conceptions that you could address during this Physics Talk. Ask students to summarize Benjamin Franklin's discovery of opposite charges and explain how he decided which kind of charge would be called positive and which kind of charge would be negative.

Using the example of the investigations with tapes, determine if students know that the tapes were electrically neutral before they pulled the top tape off the bottom tape. Consider asking students why their finger removed the excess electrons from the charged object and have them describe the process of grounding. Encourage them to draw diagrams while explaining the transfer of charges.

While discussing the conservation of charge, check to see if students understand how charge is distributed after spheres of different charges touch and then separate. You might want to ask student volunteers to come up to the board and explain how charges becomes identical after the two spheres of different charges come in contact with each other. Point out that the charges are only equally distributed when the spheres are identical. Ask students to write a brief description of the law of conservation of charge.

As students are introduced to Coulomb's law, have them describe how Charles Augustin de Coulomb was able to verify that the attractive or repulsive force between charged objects decreases as the distance between them increases, and that the strength of the force is directly proportional to the magnitude of the charges. Ask students to explore how enormous amounts of electric charge are transferred to person inside his or her house when a bolt of lightning hits the ground nearby. Have them compare the results of Cavendish's experiment

to Coulomb's experiment. Discuss the similarities between the equations describing the gravitational and electric forces and how both depend upon the inverse square of the distance between the objects.


The conservation of charge between identical metal spheres that touch and then separate can be summarized as follows:

1. The total charge of the two spheres before touching is equal to the total charge after touching.
2. The charges on the identical spheres must be identical after they touch.
3. In solving problems like this, find the total charge before contact. Distribute that total charge of the two spheres equally to both spheres after contact.

## Coulomb's Law

You have seen that in physics, scientists often search for an equation that can provide a clearer, more precise description of what they observe. In your experiments, you found that the force between two charged objects could be attractive or repulsive, and the force decreased when the objects moved farther apart. You also found that larger amounts of charge exerted a greater force between the objects. In 1784, Charles Augustin de Coulomb experimentally determined Coulomb experimentally determine
and used precise measurements to and used precise measurements to
show that the force of attraction show that the force of attraction
between two charges is directly between two charges is directly
proportional to the product of the proportional to the product of the
charges and inversely proportional charges and inversely proport to the square of the distance
between them. This is called Coulomb's law.


This law can be written using an equation:

$$
F=k \frac{q, q_{2}}{d^{2}}
$$

where $F$ is the force in newtons ( N ,
$q_{1}$ and $q_{2}$ are charges in coulombs (C),
$d$ is the distance between the centers of the charges
in meters ( m ), and
$k$ is Coulomb's constant, always equal to $9 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}$
In every problem you solve, $k$ will be $9 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}$. That is why it is called a constant. Note that the unit of charge was named a coulomb, in honor of Charles de Coulomb.
Sample Problem
Two small charged spheres are placed 0.2 m apart. The first sphere has a charge of $+3.0 \times 10^{-6} \mathrm{C}$ and the second sphere has a charge of
$-4.0 \times 10^{-6} \mathrm{C}$. Calculate the force between them.
Strategy: You can use the equation for electric forces to calculate the force between the spheres.
Given:

$$
\begin{aligned}
q_{1} & =+3.0 \times 10^{-6} \mathrm{C} \\
q_{2} & =-4.0 \times 10^{-6} \mathrm{C} \\
d & =0.2 \mathrm{~m}
\end{aligned}
$$

Solution:

$$
F=k \frac{q_{1} q_{2}}{d^{2}}
$$

$$
F=\frac{\left(9 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}\right)\left(+3.0 \times 10^{-6} \mathrm{C}\right)\left(-4.0 \times 10^{-6} \mathrm{C}\right)}{(0.2 \mathrm{~m})^{2}}=-2.7 \mathrm{~N}
$$

The negative sign indicates that the force is attractive.
One coulomb of charge is an enormous amount of charge. A lightning bolt may transfer a coulomb of charge. That is why, in solving problems that have to do with realistic charges, you must use numbers and units like $1 \times 10^{-6} \mathrm{C}$. Many calculators allow calculations with exponents to be completed with ease.


How does a negatively charged rod pick up a neutral piece of paper? The rod is negatively charged. In the diagram to the right, there are more negatives than positives in the rod. The piece of paper is neutral. There are an equal number of positives and negatives. When the rod is brought close to the paper, the excess negatives on the rod repel

the negatives of the paper. The excess negatives of the rod are attracted to the positives in the paper and repelled by the negatives in the paper. Because the positives are closer, the force of attraction is larger. Coulomb's law informs you that the force gets weaker as the distance gets larger. With a stronger force of attraction on the positive charges gets larger. With a stronger force of attraction on the positive charges
and the weaker force of repulsion on the negative charges, the rod can and the weaker for
pick up the paper.
Comparing Coulomb's Law
and Newton's Law of Universal Gravitation
You found you could actually calculate the force of attraction or repulsion of charges by using Coulomb's law:

$$
F=k \frac{q_{1} q_{2}}{d^{2}}
$$

Coulomb's law for electrostatic attraction and repulsion is very similar to Newton's law of universal gravitation. Newton's law gives the relationship among gravitational force, masses, and the distance between the masses. This relationship can be summarized by the following equation:

$$
F=G \frac{m_{1} m_{2}}{d^{2}}
$$

Physics Words
Physics Words Newton's law of
universal gravitation: universal gravitation
the relationship mong gravitation among gravitational
force, masses, and the distance between the masses.

Where $F$ is the force in newtons ( N ),
$m_{1}$ and $m_{2}$ are masses in kilograms (kg),
$d$ is the distance between the centers of the masses in meters ( m ), and $G$ is the gravitational constant, always equal to $6.67 \times 10^{-11} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{kg}^{2}$. Look at the similarities:

- Both laws show forces that decrease in strength with the square of the distance between two objects.
- Both laws show forces that depend on the product of the masses or charges.


## Checking Up

## 1.

Removing electrons from a neutral object leaves the object with a net positive charge. Because a neutral material has an equal number of positive and negative charges, taking away some of the negatives leaves some of the positives unbalanced, and thus the net positive charge.

## 2.

As the distance between two charged objects increases, the force of attraction between the objects decreases. According to Coulomb's law, the force between charged objects varies according to the equation $F=k q_{1} q_{2} / d^{2}$ so that if the distance between the objects is doubled, the force between them will decrease by a factor of four.

## 3.

When two charged conducting objects touch each other and are then separated, the charges between the objects will be shared. (Note: The objects will achieve the same potential-i.e., voltage-not necessarily equal charges.) The total net charge before contact will be the same after contact due to conservation of charge. If the two objects are conducting spheres of equal size, each object will have the same net charge.

- Both laws have constants that set the scale of their intrinsic strength. Look at the differences:
- Electric forces are attractive and repulsive; gravitational forces are only attractive.
- Charges come in two varieties, + and -. Mass comes in one variety, +.
- The electric force constant $k$ is quite large, while the gravitational force constant $G$ is quite small.
If you look at the gravitational and electrical forces between two electrons, the gravitational force is much smaller. The force is so small that you don't need to take it into account when describing the electric forces between the charges.
The experimental techniques to find the value of $k$ and $G$ are quite similar. In Coulomb's experiment, two spheres were attached to the ends of a rod and the rod was suspended by a wire. These spheres were charged, and similarly charged spheres were brought near the ends of the rods. The repulsive force caused the wire to twist. The twist was a measure of the force, and Coulomb was able to verify his law.

The constant for the strength of the gravitational force was determined in an experiment by Henry Cavendish. Cavendish's setup was similar to Coulomb's, but the
Checking Up

1. If eectrons are
removed from a
neutral object,
what kind of
charge will the object have? Explain
2. What happens
to the force of
attraction between
two charged
distance between
distance between
them increases?
Explain using
Coulomb's law.
When two charged
When two charged objects are made
to touch each other and then other and then
separated, what will be true about the net charge of the two objects after separation? Explain your attraction between the pairs of spheres was due to their gravitational attraction. This tiny force was measured by the twist in the wire. The symmetry of what appears to be two unrelated forces provides a glimpse into the beauty of the world. Physicists remark on this beauty, which drives them to find out if there understandings of the two forces because of that symmetry. This that symmetry. This exploring when you hear about their work on unified theories.



Active Physics


## Active Physics Plus

Students use Coulomb's law to determine that the force among charges depends upon the magnitude and vector nature of the forces. They then use this principle in different situations to explain the direction in which the charges will accelerate under the influence of attractive or repulsive forces.

## 1.a)

45 units to the right where each unit $F=k q_{1} q_{2} / d^{2}$.

## 1.b)

20 units to the left
1.c)

8 units to the left
1.d)

120/9 units to the left

## 1.e)

0 units in any direction

Chapter 8 Atoms on Display

For what charge of C would the net force on B be zero? Since C is twice as far from $B$, the charge would have to be four times as large to exert an equal force. That is because the force decreases by the square of the distance. Double the distance, and the force is $(1 / 2)^{2}$ or $1 / 4$ the strength; triple the distance, and the force is $(1 / 3)^{2}$ or $1 / 9$ the strength).

1. Find the direction of the net force on B in the following situations without any calculations.
a) Assume that you have three charged objects equally spaced along a line.

b) Assume that you have three charged objects equally spaced along a line.

c) Assume that you have three charged objects, where C is three times as far from $B$ as $A$ is from $B$.

d) Assume that you have three charged objects, where C is three times as far from B as A is from B.
e) Assume that you have three charged objects, where C is three times as far from B as A is from B. to positions along a line. If the charges are located in fixed positions on a plane, you can also determine the force by adding the forces. However, in this case, the vector addition of forces is a bit more complex than addition of forces along a line.
Situation 5: Assume that you have three charged objects equally spaced as shown in the diagram.

The force on B can be determined to be down and to the left. Object A will attract $B$ to the left. Object $C$ will attract $B$ to the bottom of the page. Both forces will be equal since the charges and distances will be equal.

2.

Let each unit of force be $F=k q_{1} q_{2} / d^{2}$ with the coordinate system being the standard cardinal directions.

Case 1
$F_{\text {A on } \mathrm{B}}=0.0563 \mathrm{~N}$
$F_{\text {Con B }}=0.0563 \mathrm{~N}$
$\left|F_{\mathrm{B}}\right|=\sqrt{\left(F_{\mathrm{A} \text { on B }}\right)^{2}+\left(F_{\mathrm{ConB}}\right)^{2}}=$
$\sqrt{(0.0563 \mathrm{~N})^{2}+(0.0563 \mathrm{~N})^{2}}=$
0.0796 N at $45^{\circ}$ North of East

Case 2
$F_{\mathrm{A} \text { on } \mathrm{B}}=0.0563 \mathrm{~N}$
$F_{\text {Con } B}=-0.0563 \mathrm{~N}$
$\left|F_{\mathrm{B}}\right|=\sqrt{\left(F_{\mathrm{A} \text { on } \mathrm{B}}\right)^{2}+\left(F_{\mathrm{ConB}}\right)^{2}}=$ $\sqrt{(0.0563 \mathrm{~N})^{2}+(-0.0563 \mathrm{~N})^{2}}=$ 0.0796 N at $45^{\circ}$ South of East

Case 3
$F_{\text {A on B }}=0.0563 \mathrm{~N}$
$F_{\text {Con } \mathrm{B}}=-0.1125 \mathrm{~N}$
$\left|F_{\mathrm{B}}\right|=\sqrt{\left(F_{\mathrm{A} \text { on } \mathrm{B}}\right)^{2}+\left(F_{\mathrm{ConB}}\right)^{2}}=$
$\sqrt{(0.0563 \mathrm{~N})^{2}+(-0.1125 \mathrm{~N})^{2}}=$
0.1258 N at $63^{\circ}$ South of East

Case 4
$F_{\mathrm{A} \text { on } \mathrm{B}}=0.0563 \mathrm{~N}$
$F_{\text {Con }}=0.0563 \mathrm{~N}$
$\left|F_{\mathrm{B}}\right|=\sqrt{\left(F_{\mathrm{A} \text { on } \mathrm{B}}\right)^{2}+\left(F_{\mathrm{ConB}}\right)^{2}}=$
$\sqrt{(0.0563 \mathrm{~N})^{2}+(0.0563 \mathrm{~N})^{2}}=$ 0.0796 N at $45^{\circ}$ North of East

Case 5
$F_{\mathrm{A} \text { on } \mathrm{B}}=0.0563 \mathrm{~N}$
$F_{\text {Con } B}=-0.1688 \mathrm{~N}$
$\left|F_{\mathrm{B}}\right|=\sqrt{\left(F_{\mathrm{A} \text { on } \mathrm{B}}\right)^{2}+\left(F_{\mathrm{ConB}}\right)^{2}}=$ $\sqrt{(0.0563 \mathrm{~N})^{2}+(-0.1688 \mathrm{~N})^{2}}=$ 0.1779 N at $71^{\circ}$ South of East

## What Do You Think Now?

Students should know how the transfer of charges leaves an object with a net positive or negative charge, and should be able to answer why they felt a shock on touching something. Share A Physicist's Response with them and ask them to include the law of conservation of charge in their responses. Point out that they now have the opportunity to update their previous answers and also realize how their understanding of charges has evolved gradually and prior conceptions modified or changed to accommodate knew concepts.

Encourage them to revisit What Do You See? and explain how the lightning strike might have transferred an electric charge of 1 C .

## Reflecting on the Section and the Challenge

Students should reflect on what they have learned from this section and how they can connect the interaction between charges to their Chapter Challenge. Encourage them to begin planning their museum display based on what evidence they have on the particles comprising an atom. Ask students to reflect attractive and repulsive forces between like and unlike charges and how an electrostatic force is similar to and different from a gravitational force.


Chapter 8 Atoms on Display

## Physics <br> Essential Questions

What does it mean?
How does Coulomb's law increase your understanding of unlike charges attracting and like charges repelling?
How do you know?
What experiments have you made yourself that show "something" is going on in the world that Coulomb's law attempts to describe? What kinds of measurements did you perform that show both attraction and repulsion?
Why do you believe?

| Connects with Other Physics Content | Fits with Big Ideas in Science | Meets Physics Requirements |
| :--- | :--- | :--- |
| * forces and motion | Models | Good, clear, explanation, <br> no more complex than necessary |

* The electrical force between charged objects is invisible. You can't see the charged particles and you can't see the force. In physics, scientists adopt models that can explain what they observe within nature. They try to derive equations that can accurately explain what they observe and can predict what they will observe in different situations. Forces and motion is one of physics' big ideas. Finding similarities (symmetries) between forces is one of the challenges of modern physics. Compare and contrast the electrostatic force with the gravitational force. A comparison between Coulomb's law for electrostatics and Newton's law of gravitational attraction would be helpful.
Why should you care?
You have seen that charged objects can attract or repel one another. These attractive and repulsive forces will help you create a model for how the atom is constructed and held together. Since your museum exhibit must include distinct features of the atom, you may decide to include something you learned about charges and forces from this section. Describe the aspects of electrical forces you might include in your exhibit and how you will make it engaging.

Reflecting on the Section and the Challenge
You are starting to provide evidence that atoms are composed of electrons and other particles. These particles have electric charge. You will need to provide a description of the interaction between the charges when you provide a description of the atom for your museum display. You may find a way to include in your exhibit the larger concepts of conservation of charge or the ability to actually calculate these forces of attraction and repulsion.

## Physics Essential Questions

## What does it mean?

Coulomb's law provides an equation by which you can calculate the strength of the force. The force is proportional to the quantity of charge and inversely proportional to the square of the distance between charges.

How do you know?
Strips of tape were able to attract while other strips of tape repelled each other.

Why do you believe?
Both the gravitational force and the electrostatic force are "inverse square" laws. The force gets weaker by the square of the distance between masses or charges. The forces are also similar because the gravitational force depends on mass and the electrical force depends on charge. The gravitational force is always attractive (i.e., there is only one type of mass) and the electrostatic force can be attractive or repulsive (i.e., there are both positive and negative charges). Electrostatic force is expressed in the following equation:

$$
F=k q_{1} q_{2} / d^{2}
$$

| Section 1 Static Electricty and Coulomb's Law: Opposites Attract |
| :--- |
| 1. Electrons are transferred from a rod to a piece of cloth. |
| a) Which object will become negatively charged? |
| b) Which object will become positively charged? |
| 2. A rubber rod is negatively charged after being rubbed by wool. Explain how |
| this happens. |
| 3. Two identical spheres are mounted on insulated stands. The first sphere has a |
| charge of -1 . The second sphere has a charge of -3 . After the spheres touch, |
| what will the charge on each be? |
| 4. One of two identical metal spheres has a charge of +1 and the other sphere |
| has a charge of -5 . Compare the total charge on the spheres before and after |
| contact. |
| 5. Charge A is $+2.0 \times 10^{-6} \mathrm{C}$ and charge B is $+3 \times 10^{-6} \mathrm{C}$. The charges are 3 m |
| apart. What is the force between them? Is it attractive or repulsive? |
| 6. Charge A is $-4.0 \times 10^{-6} \mathrm{C}$ and charge B is $+2 \times 10^{-6} \mathrm{C}$. The charges are 5 m |
| apart. What is the force between them? Is it attractive or repulsive? |
| 7. When the air is dry and you walk on a wool carpet with your shoes, you may |
| experience a shock when you touch a doorknob. Explain what is happening |
| in terms of electric charge. (Hint: Your shoes are similar to the rubber rod.) |
| 8. Compare and contrast Coulomb's law and Newton's law of gravitational |
| attraction. Provide at least one similarity and one difference. |
| 9. Coulomb's law states that the electric force between two charged objects |
| decreases with the square of the distance. Suppose the original force between |
| two objects is 60 N , and the distance between them is tripled, the new force |
| would be $\left(\frac{1}{3}\right)^{2}$, or nine times weaker. This new force would be $60 \mathrm{~N} \times \frac{1}{9}=6.7 \mathrm{~N}$ |
| or 7 N . Find the new forces if the original distance was |
| a) doubled. |
| b) quadrupled. |
| c) halved. |
| d) quartered. |
| 10. Sketch a graph that shows how the electrostatic force defined by Coulomb's |
| law varies with the distance. |

Gravitational force is expressed in the following equation:

$$
F_{\mathrm{G}}=G m_{1} m_{2} / r^{2}
$$

Why should you care?
You can include the attractive and repulsive forces. You can let people try the experiment with pieces of tape. You can have two pieces of tape repelling each other to capture people's attention.

## Physics to Go

## 1.a)

the cloth

## 1.b)

the rod
2.

Electrons were stripped off the wool and attached to the rubber rod.
3.
-2 on each
4.
-2 on each
5.
$6 \times 10^{-3} \mathrm{~N}$, repulsive
6.
$2.9 \times 10^{-3} \mathrm{~N}$, attractive

## 7.

The rubber soles of your shoes pick up electrons from the wool carpet. This makes your shoes negative. Since you are a good conductor of electric charge, this excess negative charge spreads throughout your body (you are at a higher voltage). When you touch the doorknob, you are grounded (you have touched a point of zero voltage) and the charge leaves your body at once, producing a shock (electric current is driven by a voltage difference).

## 8.

They are similar because: They both decrease with the square of the distance between the objects. They both have constants.
They are different because: The Coulomb constant is much greater than the gravitational constant. Electrical forces are attractive
and repulsive while gravitational forces are only attractive. Masses come in one variety (+) while charges come in two varieties (+/-).

## 9.a)

If distance is doubled, the force is decreased by a factor of four.

## 9.b)

If distance is quadrupled, the force is $1 / 16$ its magnitude.

## 9.c)

If the distance is halved, the force is four times as large.

## 9.d)

If the distance is quartered, the force is 16 times as large.
10.

The student's graph should look similar to the one shown below.

distance

## 11.a)

Let $N=$ number of electrons sought. Then
$1 \mathrm{C}=N \times 1.6 \times 10^{-19} \mathrm{C}$.
Therefore
$N=1 /\left(1.6 \times 10^{-19}\right)=6.25 \times 10^{18}$.
11.b)

Because current = charge/time, we have charge $=$ current $\times$ time $=$ $(5 \mathrm{amps}) \times(1 \mathrm{~min})=(5 \mathrm{C} / \mathrm{s})(60 \mathrm{~s})=$ 300 C. Because each Coulomb

## Chapter 8 Atoms on Display

11. A single electron has a charge of $1.6 \times 10^{-19} \mathrm{C}$.
a) Show why it takes $6.25 \times 10^{13}$ electrons to equal 1 C .
b) If you studied currents in Electricity for Everyone, solve this problem: Calculate how many electrons go by when 5 A of current exists for one minute.
12. Compare the gravitational force between two electrons to the electric force between them. Which force is stronger, and by how much? The mass of an electron is $9.1 \times 10^{-31} \mathrm{~kg}$.
13. How could you depict the invisible electrostatic force in a museum exhibit?

For Questions 14 to 19 choose the best answer from those given.
14. If the distance between two charged objects is halved, the force between them will
a) double.
b) be half as much.
c) quadruple.
d) stay the same.
15. Two charged identical spheres attract each other. If the charge on one is doubled, the force between them will
a) double.
b) be half as much.
c) quadruple.
d) stay the same.
16. The force between two charged objects $A$ and $B$ is determined to be -47 N . Which of the following options is possible?
I. The charge on $A$ is positive and $B$ is positive.
II. The charge on $A$ is negative and $B$ is negative.
III. The charge on A is positive and B is negative.
IV. The charge on $A$ is negative and $B$ is positive.
a) III and IV
b) I and II
c) III only
d) II only
equals $6.25 \times 10^{18}$ electrons,
12. the total number of electrons is $(300 \mathrm{C})\left(6.25 \times 10^{18}\right.$ electrons $\left./ \mathrm{C}\right)=$ $1.875 \times 10^{21}$ electrons.
$F_{\text {graviry }} / F_{\text {electric }}=$
$\frac{G m^{2} / r^{2}}{k e^{2} / r^{2}}=\quad\left(\right.$ the $r^{\prime}$ s cancel $)$
$\left[\begin{array}{l}\left.\left(6.67 \times 10^{-11} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{kg}^{2}\right) \times\right] \\ \left(9.11 \times 10^{-31} \mathrm{~kg}\right)^{2}\end{array}\right]$
$\left[\begin{array}{l}\left.\left(9 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}\right) \times\right] \\ \left(1.6 \times 10^{-19} \mathrm{C}\right)^{2}\end{array}\right]$
$2.4 \times 10^{-43}=$
0.000000000000000000000
00000000000000000000024.


Therefore, gravity is negligible compared to the electric force between two electrons.

## 13.

Magnetism is also an invisible force, so substituting magnetism for electricity might be a possibility. Alternatively, magicians' tricks using mirrors to make things seem to be invisible might be used to hide one object exerting a force.

## 14.c)

quadruple. If the distance between two charged objects is doubled, the force between them will be one quarter the original.

## 15.a)

double. If the charge on one is doubled, the force between them will double.

## 16.a)

III and IV. A negative force means a force of attraction, so the charges must be of opposite signs.

## 17.a)

increase. Since the force is inverse square with distance, decreasing the distance increases the force.

## 18.d)

take away negatives. Electrons are the mobile charges, and removing some from neutral objects which have equal numbers of positive and negative charges makes neutral objects positive.

## 19.c)

neutral. A neutral object will attract both a positive and a negative object by induction.

## 20.

## Preparing for the

 Chapter ChallengeStudent answers will vary, but should make some mention of the electric force associated with charges such as electrons.

## SECTION 1 QUIZ

## 8-1a Blackline Master

1. To charge an object positively, a student should
a) add positive charges.
b) add negative charges.
c) remove positive charges.
d) remove negative charges.
2. Two identical conducting spheres on insulating stands are charged as shown at right. The two spheres touch and then are separated. After the spheres are separated the charge on each sphere will be
a) +4 .
b) +2 .
c) +16 .
d) -4 .

3. For Question 2, when the spheres touch, the total charge on the two spheres will
a) decrease by 6 .
b) increase by 6 .
c) decrease by 4 .
d) remain the same.
4. Two small charges are a distance of 10 meters apart. Charge A is $4.0 \times 10^{-5} \mathrm{C}$ and charge B is $2.0 \times 10^{-6} \mathrm{C}$. What is the size of the force between the charges?
a) $8.0 \times 10^{-30} \mathrm{~N}$
b) $8.0 \times 10^{-11} \mathrm{~N}$
c) $7.2 \times 10^{-3} \mathrm{~N}$
d) $7.2 \times 10^{-17} \mathrm{~N}$
5. Which graph below correctly represents how the force between two charged objects varies with distance?
a)

b)

c)

d)


## SECTION 1 QUIZ ANSWERS

(1) d) remove negative charges. Electrons are the mobile parts of the atom. The positively charged protons are firmly held in the nucleus and are difficult to remove. To affect the balance of the charge, it is easier to remove the negatively charged electrons, leaving a net positive charge. Adding positive charges to the nucleus would be extremely difficult, and not doable under ordinary circumstances.

2 b) By conservation of charge, the total charge on the two spheres before contact the sum of +10 and -6 , or +4 . That is, there are 6 extra electrons on one sphere, while the other is 10 electrons short. When the spheres touch, the 6 electrons will migrate to the sphere that is missing the 10 electrons. In addition, the remaining positive charge of +4 will then attract an additional 2 electrons from the now neutral sphere to leave a charge of +2 on each. Thus the charge is equally distributed between the two identical spheres giving each one a charge of +2 for a total of +4 .
(3) By conservation of charge, the total charge must remain the same.
(4) c) Using the Coulomb's law formula $F=k q_{1} q_{2} / d^{2}$ gives
$F=\left(9 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}\right)\left(4 \times 10^{-5} \mathrm{C}\right)\left(2 \times 10^{-6} \mathrm{C}\right) /(10 \mathrm{~m})^{2}=7.2 \times 10^{-3} \mathrm{~N}$.
(5) d) The force falls off as the inverse square of the distance and only graph d shows this type of relationship.

