

P
$\boldsymbol{U Z L G R}$

You can estimate the distance to an approaching storm by listening carefully to the sound of the thunder. How is this done? Why is the sound that follows a lightning strike sometimes a short, sharp thunderclap and other times a longlasting rumble? (Richard Kaylin/Tony Stone Images)

## Sound Waves



## Chapteroutline

17.1 Speed of Sound Waves
17.2 Periodic Sound Waves
17.3 Intensity of Periodic Sound Waves
17.4 Spherical and Plane Waves
17.5 The Doppler Effect


Figure 17.1 Motion of a longitudinal pulse through a compressible gas. The compression (darker region) is produced by the moving piston.

Sound waves are the most important example of longitudinal waves. They can travel through any material medium with a speed that depends on the properties of the medium. As the waves travel, the particles in the medium vibrate to produce changes in density and pressure along the direction of motion of the wave. These changes result in a series of high-pressure and low-pressure regions. If the source of the sound waves vibrates sinusoidally, the pressure variations are also sinusoidal. We shall find that the mathematical description of sinusoidal sound waves is identical to that of sinusoidal string waves, which was discussed in the previous chapter.

Sound waves are divided into three categories that cover different frequency ranges. (1) Audible waves are waves that lie within the range of sensitivity of the human ear. They can be generated in a variety of ways, such as by musical instruments, human vocal cords, and loudspeakers. (2) Infrasonic waves are waves having frequencies below the audible range. Elephants can use infrasonic waves to communicate with each other, even when separated by many kilometers. (3) Ultrasonic waves are waves having frequencies above the audible range. You may have used a "silent" whistle to retrieve your dog. The ultrasonic sound it emits is easily heard by dogs, although humans cannot detect it at all. Ultrasonic waves are also used in medical imaging.

We begin this chapter by discussing the speed of sound waves and then wave intensity, which is a function of wave amplitude. We then provide an alternative description of the intensity of sound waves that compresses the wide range of intensities to which the ear is sensitive to a smaller range. Finally, we treat effects of the motion of sources and/or listeners.

### 17.1 SPEED OF SOUND WAVES

Let us describe pictorially the motion of a one-dimensional longitudinal pulse moving through a long tube containing a compressible gas (Fig. 17.1). A piston at the left end can be moved to the right to compress the gas and create the pulse. Before the piston is moved, the gas is undisturbed and of uniform density, as represented by the uniformly shaded region in Figure 17.1a. When the piston is suddenly pushed to the right (Fig. 17.1b), the gas just in front of it is compressed (as represented by the more heavily shaded region); the pressure and density in this region are now higher than they were before the piston moved. When the piston comes to rest (Fig. 17.1c), the compressed region of the gas continues to move to the right, corresponding to a longitudinal pulse traveling through the tube with


An ultrasound image of a human fetus in the womb after 20 weeks of development, showing the head, body, arms, and legs in profile.
speed $v$. Note that the piston speed does not equal $v$. Furthermore, the compressed region does not "stay with" the piston as the piston moves, because the speed of the wave may be greater than the speed of the piston.

The speed of sound waves depends on the compressibility and inertia of the medium. If the medium has a bulk modulus $B$ (see Section 12.4) and density $\rho$, the speed of sound waves in that medium is

$$
v=\sqrt{\frac{B}{\rho}}
$$

(17.1)

It is interesting to compare this expression with Equation 16.4 for the speed of transverse waves on a string, $v=\sqrt{T / \mu}$. In both cases, the wave speed depends on an elastic property of the medium - bulk modulus $B$ or string tension $T$-and on an inertial property of the medium - $\rho$ or $\mu$. In fact, the speed of all mechanical waves follows an expression of the general form

$$
v=\sqrt{\frac{\text { elastic property }}{\text { inertial property }}}
$$

The speed of sound also depends on the temperature of the medium. For sound traveling through air, the relationship between wave speed and medium temperature is

$$
v=(331 \mathrm{~m} / \mathrm{s}) \sqrt{1+\frac{T_{\mathrm{C}}}{273^{\circ} \mathrm{C}}}
$$

where $331 \mathrm{~m} / \mathrm{s}$ is the speed of sound in air at $0^{\circ} \mathrm{C}$, and $T_{\mathrm{C}}$ is the temperature in degrees Celsius. Using this equation, one finds that at $20^{\circ} \mathrm{C}$ the speed of sound in air is approximately $343 \mathrm{~m} / \mathrm{s}$.

This information provides a convenient way to estimate the distance to a thunderstorm, as demonstrated in the QuickLab. During a lightning flash, the temperature of a long channel of air rises rapidly as the bolt passes through it. This temperature increase causes the air in the channel to expand rapidly, and this expansion creates a sound wave. The channel produces sound throughout its entire length at essentially the same instant. If the orientation of the channel is such that all of its parts are approximately the same distance from you, sounds from the different parts reach you at the same time, and you hear a short, intense thunderclap. However, if the distances between your ear and different portions of the channel vary, sounds from different portions arrive at your ears at different times. If the channel were a straight line, the resulting sound would be a steady roar, but the zigzag shape of the path produces variations in loudness.

## Quick Puiz 17.1

The speed of sound in air is a function of (a) wavelength, (b) frequency, (c) temperature, (d) amplitude.

## Quick Quiz 17.2

As a result of a distant explosion, an observer first senses a ground tremor and then hears the explosion later. Explain.

## QuickLab

The next time a thunderstorm approaches, count the seconds between a flash of lightning (which reaches you almost instantaneously) and the following thunderclap. Divide this time by 3 to determine the approximate number of kilometers (or by 5 to estimate the miles) to the storm.

To learn more about lightning, read E. Williams, "The Electrification of Thunderstorms" Sci. Am. 259(5):88-89, 1988.

## EXAMPLE 17.1 Speed of Sound in a Solid

If a solid bar is struck at one end with a hammer, a longitudinal pulse propagates down the bar with a speed $v=\sqrt{Y / \rho}$, where $Y$ is the Young's modulus for the material (see Section 12.4). Find the speed of sound in an aluminum bar.

Solution From Table 12.1 we obtain $Y=7.0 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$ for aluminum, and from Table 1.5 we obtain $\rho=$ $2.70 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}$. Therefore,

$$
v_{\mathrm{Al}}=\sqrt{\frac{Y}{\rho}}=\sqrt{\frac{7.0 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}}{2.70 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}}} \approx 5.1 \mathrm{~km} / \mathrm{s}
$$

This typical value for the speed of sound in solids is much greater than the speed of sound in gases, as Table 17.1 shows. This difference in speeds makes sense because the molecules of a solid are bound together into a much more rigid structure than those in a gas and hence respond more rapidly to a disturbance.

## EXAMPLE 17.2 Speed of Sound in a Liquid

(a) Find the speed of sound in water, which has a bulk modulus of $2.1 \times 10^{9} \mathrm{~N} / \mathrm{m}^{2}$ and a density of $1.00 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}$.

Solution Using Equation 17.1, we find that

$$
v_{\text {water }}=\sqrt{\frac{B}{\rho}}=\sqrt{\frac{2.1 \times 10^{9} \mathrm{~N} / \mathrm{m}^{2}}{1.00 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}}}=1.4 \mathrm{~km} / \mathrm{s}
$$

In general, sound waves travel more slowly in liquids than in solids because liquids are more compressible than solids.
(b) Dolphins use sound waves to locate food. Experiments have shown that a dolphin can detect a $7.5-\mathrm{cm}$ target 110 m away, even in murky water. For a bit of "dinner" at that distance, how much time passes between the moment the dolphin emits a sound pulse and the moment the dolphin hears its reflection and thereby detects the distant target?

Solution The total distance covered by the sound wave as it travels from dolphin to target and back is $2 \times 110 \mathrm{~m}=$ 220 m. From Equation 2.2, we have

$$
\Delta t=\frac{\Delta x}{v_{x}}=\frac{220 \mathrm{~m}}{1400 \mathrm{~m} / \mathrm{s}}=0.16 \mathrm{~s}
$$



Bottle-nosed dolphin. (Stuart Westmoreland/Tony Stone Images)

### 17.2 PERIODIC SOUND WAVES

This section will help you better comprehend the nature of sound waves. You will learn that pressure variations control what we hear-an important fact for understanding how our ears work.

One can produce a one-dimensional periodic sound wave in a long, narrow tube containing a gas by means of an oscillating piston at one end, as shown in Figure 17.2. The darker parts of the colored areas in this figure represent re-
gions where the gas is compressed and thus the density and pressure are above their equilibrium values. A compressed region is formed whenever the piston is pushed into the tube. This compressed region, called a condensation, moves through the tube as a pulse, continuously compressing the region just in front of itself. When the piston is pulled back, the gas in front of it expands, and the pressure and density in this region fall below their equilibrium values (represented by the lighter parts of the colored areas in Fig. 17.2). These low-pressure regions, called rarefactions, also propagate along the tube, following the condensations. Both regions move with a speed equal to the speed of sound in the medium.

As the piston oscillates sinusoidally, regions of condensation and rarefaction are continuously set up. The distance between two successive condensations (or two successive rarefactions) equals the wavelength $\lambda$. As these regions travel through the tube, any small volume of the medium moves with simple harmonic motion parallel to the direction of the wave. If $s(x, t)$ is the displacement of a small volume element from its equilibrium position, we can express this harmonic displacement function as

$$
\begin{equation*}
s(x, t)=s_{\max } \cos (k x-\omega t) \tag{17.2}
\end{equation*}
$$

where $\boldsymbol{s}_{\text {max }}$ is the maximum displacement of the medium from equilibrium (in other words, the displacement amplitude of the wave), $k$ is the angular wavenumber, and $\omega$ is the angular frequency of the piston. Note that the displacement of the medium is along $x$, in the direction of motion of the sound wave, which means we are describing a longitudinal wave.

As we shall demonstrate shortly, the variation in the gas pressure $\Delta P$, measured from the equilibrium value, is also periodic and for the displacement function in Equation 17.2 is given by

$$
\begin{equation*}
\Delta P=\Delta P_{\max } \sin (k x-\omega t) \tag{17.3}
\end{equation*}
$$

where the pressure amplitude $\boldsymbol{\Delta} \boldsymbol{P}_{\text {max }}$ — which is the maximum change in pres-

Figure 17.2 A sinusoidal longitudinal wave propagating through a gas-filled tube. The source of the wave is a sinusoidally oscillating piston at the left. The high-pressure and low-pressure regions are colored darkly and lightly, respectively.


| TABLE 17.1 |  |
| :--- | ---: |
| Speeds of Sound in Various |  |
| Media |  |
| Medium | $\boldsymbol{v}(\mathbf{m} / \mathbf{s})$ |
| Gases |  |
| Hydrogen $\left(0^{\circ} \mathrm{C}\right)$ | 1286 |
| Helium $\left(0^{\circ} \mathrm{C}\right)$ | 972 |
| Air $\left(20^{\circ} \mathrm{C}\right)$ | 343 |
| Air $\left(0^{\circ} \mathrm{C}\right)$ | 331 |
| Oxygen $\left(0^{\circ} \mathrm{C}\right)$ | 317 |
| Liquids at $\mathbf{2 5}^{\circ} \mathbf{C}$ |  |
| Glycerol | 1904 |
| Sea water | 1533 |
| Water | 1493 |
| Mercury | 1450 |
| Kerosene | 1324 |
| Methyl alcohol | 1143 |
| Carbon tetrachloride | 926 |
| Solids |  |
| Diamond | 12000 |
| Pyrex glass | 5640 |
| Iron | 5130 |
| Aluminum | 5100 |
| Brass | 4700 |
| Copper | 3560 |
| Gold | 3240 |
| Lucite | 2680 |
| Lead | 1322 |
| Rubber | 1600 |
|  |  |

Pressure amplitude


Figure 17.3 (a) Displacement amplitude versus position and (b) pressure amplitude versus position for a sinusoidal longitudinal wave. The displacement wave is $90^{\circ}$ out of phase with the pressure wave.
sure from the equilibrium value - is given by

$$
\begin{equation*}
\Delta P_{\max }=\rho v \omega \mathrm{~s}_{\max } \tag{17.4}
\end{equation*}
$$

Thus, we see that a sound wave may be considered as either a displacement wave or a pressure wave. A comparison of Equations 17.2 and 17.3 shows that the pressure wave is $90^{\circ}$ out of phase with the displacement wave. Graphs of these functions are shown in Figure 17.3. Note that the pressure variation is a maximum when the displacement is zero, and the displacement is a maximum when the pressure variation is zero.

## Ouick Quiz 17.3

If you blow across the top of an empty soft-drink bottle, a pulse of air travels down the bottle. At the moment the pulse reaches the bottom of the bottle, compare the displacement of air molecules with the pressure variation.

## Derivation of Equation 17.3

From the definition of bulk modulus (see Eq. 12.8), the pressure variation in the gas is

$$
\Delta P=-B \frac{\Delta V}{V_{i}}
$$

The volume of gas that has a thickness $\Delta x$ in the horizontal direction and a crosssectional area $A$ is $V_{i}=A \Delta x$. The change in volume $\Delta V$ accompanying the pressure change is equal to $A \Delta s$, where $\Delta s$ is the difference between the value of $s$ at $x+\Delta x$ and the value of $s$ at $x$. Hence, we can express $\Delta P$ as

$$
\Delta P=-B \frac{\Delta V}{V_{i}}=-B \frac{A \Delta s}{A \Delta x}=-B \frac{\Delta s}{\Delta x}
$$

As $\Delta x$ approaches zero, the ratio $\Delta s / \Delta x$ becomes $\partial s / \partial x$. (The partial derivative indicates that we are interested in the variation of $s$ with position at a fixed time.) Therefore,

$$
\Delta P=-B \frac{\partial s}{\partial x}
$$

If the displacement is the simple sinusoidal function given by Equation 17.2, we find that

$$
\Delta P=-B \frac{\partial}{\partial x}\left[s_{\max } \cos (k x-\omega t)\right]=B k s_{\max } \sin (k x-\omega t)
$$

Because the bulk modulus is given by $B=\rho v^{2}$ (see Eq. 17.1), the pressure variation reduces to

$$
\Delta P=\rho v^{2} k s_{\max } \sin (k x-\omega t)
$$

From Equation 16.13 , we can write $k=\omega / v$; hence, $\Delta P$ can be expressed as

$$
\Delta P=\rho v \omega s_{\max } \sin (k x-\omega t)
$$

Because the sine function has a maximum value of 1 , we see that the maximum value of the pressure variation is $\Delta P_{\max }=\rho v \omega s_{\max }$ (see Eq. 17.4), and we arrive at Equation 17.3:

$$
\Delta P=\Delta P_{\max } \sin (k x-\omega t)
$$

### 17.3 INTENSITY OF PERIODIC SOUND WAVES

In the previous chapter, we showed that a wave traveling on a taut string transports energy. The same concept applies to sound waves. Consider a volume of air of mass $\Delta m$ and width $\Delta x$ in front of a piston oscillating with a frequency $\omega$, as shown in Figure 17.4. The piston transmits energy to this volume of air in the tube, and the energy is propagated away from the piston by the sound wave. ${ }^{1}$ To evaluate the rate of energy transfer for the sound wave, we shall evaluate the kinetic energy of this volume of air, which is undergoing simple harmonic motion. We shall follow a procedure similar to that in Section 16.8, in which we evaluated the rate of energy transfer for a wave on a string.

As the sound wave propagates away from the piston, the displacement of any volume of air in front of the piston is given by Equation 17.2. To evaluate the kinetic energy of this volume of air, we need to know its speed. We find the speed by taking the time derivative of Equation 17.2:

$$
v(x, t)=\frac{\partial}{\partial t} s(x, t)=\frac{\partial}{\partial t}\left[s_{\max } \cos (k x-\omega t)\right]=\omega s_{\max } \sin (k x-\omega t)
$$

Imagine that we take a "snapshot" of the wave at $t=0$. The kinetic energy of a given volume of air at this time is

$$
\begin{aligned}
\Delta K & =\frac{1}{2} \Delta m v^{2}=\frac{1}{2} \Delta m\left(\omega s_{\max } \sin k x\right)^{2}=\frac{1}{2} \rho A \Delta x\left(\omega s_{\max } \sin k x\right)^{2} \\
& =\frac{1}{2} \rho A \Delta x\left(\omega s_{\max }\right)^{2} \sin ^{2} k x
\end{aligned}
$$

where $A$ is the cross-sectional area of the moving air and $A \Delta x$ is its volume. Now, as in Section 16.8, we integrate this expression over a full wavelength to find the total kinetic energy in one wavelength. Letting the volume of air shrink to infinitesimal thickness, so that $\Delta x \rightarrow d x$, we have

$$
\begin{gathered}
K_{\lambda}=\int d K=\int_{0}^{\lambda} \frac{1}{2} \rho A\left(\omega s_{\max }\right)^{2} \sin ^{2} k x d x=\frac{1}{2} \rho A\left(\omega s_{\max }\right)^{2} \int_{0}^{\lambda} \sin ^{2} k x d x \\
=\frac{1}{2} \rho A\left(\omega s_{\max }\right)^{2}\left(\frac{1}{2} \lambda\right)=\frac{1}{4} \rho A\left(\omega s_{\max }\right)^{2} \lambda
\end{gathered}
$$

As in the case of the string wave in Section 16.8, the total potential energy for one wavelength has the same value as the total kinetic energy; thus, the total mechani-


Figure 17.4 An oscillating piston transfers energy to the air in the tube, initially causing the volume of air of width $\Delta x$ and mass $\Delta m$ to oscillate with an amplitude $s_{\text {max }}$.

[^0]cal energy is
$$
E_{\lambda}=K_{\lambda}+U_{\lambda}=\frac{1}{2} \rho A\left(\omega s_{\max }\right)^{2} \lambda
$$

As the sound wave moves through the air, this amount of energy passes by a given point during one period of oscillation. Hence, the rate of energy transfer is

$$
\mathscr{P}=\frac{E_{\lambda}}{\Delta t}=\frac{\frac{1}{2} \rho A\left(\omega s_{\max }\right)^{2} \lambda}{T}=\frac{1}{2} \rho A\left(\omega s_{\max }\right)^{2}\left(\frac{\lambda}{T}\right)=\frac{1}{2} \rho A v\left(\omega s_{\max }\right)^{2}
$$

where $v$ is the speed of sound in air.
We define the intensity $\boldsymbol{I}$ of a wave, or the power per unit area, to be the rate at which the energy being transported by the wave flows through a unit area $A$ perpendicular to the direction of travel of the wave.

In the present case, therefore, the intensity is

$$
\begin{equation*}
I=\frac{\mathscr{P}}{A}=\frac{1}{2} \rho v\left(\omega s_{\max }\right)^{2} \tag{17.5}
\end{equation*}
$$

Thus, we see that the intensity of a periodic sound wave is proportional to the square of the displacement amplitude and to the square of the angular frequency (as in the case of a periodic string wave). This can also be written in terms of the pressure amplitude $\Delta P_{\text {max }}$; in this case, we use Equation 17.4 to obtain

$$
\begin{equation*}
I=\frac{\Delta P_{\max }^{2}}{2 \rho v} \tag{17.6}
\end{equation*}
$$

## EXAMPLE 17.3 Hearing Limits

The faintest sounds the human ear can detect at a frequency of 1000 Hz correspond to an intensity of about $1.00 \times$ $10^{-12} \mathrm{~W} / \mathrm{m}^{2}$ - the so-called threshold of hearing. The loudest sounds the ear can tolerate at this frequency correspond to an intensity of about $1.00 \mathrm{~W} / \mathrm{m}^{2}$ - the threshold of pain. Determine the pressure amplitude and displacement amplitude associated with these two limits.

Solution First, consider the faintest sounds. Using Equation 17.6 and taking $v=343 \mathrm{~m} / \mathrm{s}$ as the speed of sound waves in air and $\rho=1.20 \mathrm{~kg} / \mathrm{m}^{3}$ as the density of air, we obtain

$$
\begin{aligned}
\Delta P_{\max } & =\sqrt{2 \rho v I} \\
& =\sqrt{2\left(1.20 \mathrm{~kg} / \mathrm{m}^{3}\right)(343 \mathrm{~m} / \mathrm{s})\left(1.00 \times 10^{-12} \mathrm{~W} / \mathrm{m}^{2}\right)} \\
& =2.87 \times 10^{-5} \mathrm{~N} / \mathrm{m}^{2}
\end{aligned}
$$

Because atmospheric pressure is about $10^{5} \mathrm{~N} / \mathrm{m}^{2}$, this result
tells us that the ear can discern pressure fluctuations as small as 3 parts in $10^{10}$ !

We can calculate the corresponding displacement amplitude by using Equation 17.4, recalling that $\omega=2 \pi f$ (see Eqs. 16.10 and 16.12):

$$
\begin{aligned}
s_{\max } & =\frac{\Delta P_{\max }}{\rho v \omega}=\frac{2.87 \times 10^{-5} \mathrm{~N} / \mathrm{m}^{2}}{\left(1.20 \mathrm{~kg} / \mathrm{m}^{3}\right)(343 \mathrm{~m} / \mathrm{s})(2 \pi \times 1000 \mathrm{~Hz})} \\
& =1.11 \times 10^{-11} \mathrm{~m}
\end{aligned}
$$

This is a remarkably small number! If we compare this result for $s_{\text {max }}$ with the diameter of a molecule (about $10^{-10} \mathrm{~m}$ ), we see that the ear is an extremely sensitive detector of sound waves.

In a similar manner, one finds that the loudest sounds the human ear can tolerate correspond to a pressure amplitude of $28.7 \mathrm{~N} / \mathrm{m}^{2}$ and a displacement amplitude equal to $1.11 \times 10^{-5} \mathrm{~m}$.

## Sound Level in Decibels

The example we just worked illustrates the wide range of intensities the human ear can detect. Because this range is so wide, it is convenient to use a logarithmic scale, where the sound level $\beta$ (Greek letter beta) is defined by the equation

$$
\begin{equation*}
\beta=10 \log \left(\frac{I}{I_{0}}\right) \tag{17.7}
\end{equation*}
$$

The constant $I_{0}$ is the reference intensity, taken to be at the threshold of hearing ( $I_{0}=1.00 \times 10^{-12} \mathrm{~W} / \mathrm{m}^{2}$ ), and $I$ is the intensity, in watts per square meter, at the sound level $\beta$, where $\beta$ is measured in decibels $(\mathrm{dB}) .{ }^{2}$ On this scale, the threshold of pain $\left(I=1.00 \mathrm{~W} / \mathrm{m}^{2}\right)$ corresponds to a sound level of $\beta=$ $10 \log \left[\left(1 \mathrm{~W} / \mathrm{m}^{2}\right) /\left(10^{-12} \mathrm{~W} / \mathrm{m}^{2}\right)\right]=10 \log \left(10^{12}\right)=120 \mathrm{~dB}$, and the threshold of hearing corresponds to $\beta=10 \log \left[\left(10^{-12} \mathrm{~W} / \mathrm{m}^{2}\right) /\left(10^{-12} \mathrm{~W} / \mathrm{m}^{2}\right)\right]=0 \mathrm{~dB}$.

Prolonged exposure to high sound levels may seriously damage the ear. Ear plugs are recommended whenever sound levels exceed 90 dB . Recent evidence suggests that "noise pollution" may be a contributing factor to high blood pressure, anxiety, and nervousness. Table 17.2 gives some typical sound-level values.

| TABLE 17.2 |  |
| :--- | :---: |
| Sound Levels |  |
| Source of Sound | $\boldsymbol{\beta}(\mathbf{d B})$ |
| Nearby jet airplane | 150 |
| Jackhammer; |  |
| $\quad$ machine gun | 130 |
| Siren; rock concert <br> Subway; power <br> mower <br> Busy traffic | 120 |
| Vacuum cleaner | 100 |
| Normal conver- | 70 |
| sation | 50 |
| Mosquito buzzing | 40 |
| Whisper | 30 |
| Rustling leaves | 10 |
| Threshold of |  |
| $\quad$ hearing | 0 |

## EXAMPLE 17.4 Sound Levels

Two identical machines are positioned the same distance from a worker. The intensity of sound delivered by each machine at the location of the worker is $2.0 \times 10^{-7} \mathrm{~W} / \mathrm{m}^{2}$. Find the sound level heard by the worker (a) when one machine is operating and (b) when both machines are operating.

Solution (a) The sound level at the location of the worker with one machine operating is calculated from Equation 17.7:

$$
\begin{aligned}
\beta_{1} & =10 \log \left(\frac{2.0 \times 10^{-7} \mathrm{~W} / \mathrm{m}^{2}}{1.00 \times 10^{-12} \mathrm{~W} / \mathrm{m}^{2}}\right)=10 \log \left(2.0 \times 10^{5}\right) \\
& =53 \mathrm{~dB}
\end{aligned}
$$

(b) When both machines are operating, the intensity is doubled to $4.0 \times 10^{-7} \mathrm{~W} / \mathrm{m}^{2}$; therefore, the sound level now is

$$
\begin{aligned}
\beta_{2} & =10 \log \left(\frac{4.0 \times 10^{-7} \mathrm{~W} / \mathrm{m}^{2}}{1.00 \times 10^{-12} \mathrm{~W} / \mathrm{m}^{2}}\right)=10 \log \left(4.0 \times 10^{5}\right) \\
& =56 \mathrm{~dB}
\end{aligned}
$$

From these results, we see that when the intensity is doubled, the sound level increases by only 3 dB .

## Ouick Quiz 17.4

A violin plays a melody line and is then joined by nine other violins, all playing at the same intensity as the first violin, in a repeat of the same melody. (a) When all of the violins are playing together, by how many decibels does the sound level increase? (b) If ten more violins join in, how much has the sound level increased over that for the single violin?

[^1]
### 17.4 SPHERICAL AND PLANE WAVES

If a spherical body oscillates so that its radius varies sinusoidally with time, a spherical sound wave is produced (Fig. 17.5). The wave moves outward from the source at a constant speed if the medium is uniform.

Because of this uniformity, we conclude that the energy in a spherical wave propagates equally in all directions. That is, no one direction is preferred over any other. If $\mathscr{P}_{\mathrm{av}}$ is the average power emitted by the source, then this power at any distance $r$ from the source must be distributed over a spherical surface of area $4 \pi r^{2}$. Hence, the wave intensity at a distance $r$ from the source is

$$
\begin{equation*}
I=\frac{\mathscr{P}_{\mathrm{av}}}{A}=\frac{\mathscr{P}_{\mathrm{av}}}{4 \pi r^{2}} \tag{17.8}
\end{equation*}
$$

Because $\mathscr{P}_{\text {av }}$ is the same for any spherical surface centered at the source, we see that the intensities at distances $r_{1}$ and $r_{2}$ are

$$
I_{1}=\frac{\mathscr{P}_{\mathrm{av}}}{4 \pi r_{1}{ }^{2}} \quad \text { and } \quad I_{2}=\frac{\mathscr{P}_{\mathrm{av}}}{4 \pi r_{2}{ }^{2}}
$$

Therefore, the ratio of intensities on these two spherical surfaces is

$$
\frac{I_{1}}{I_{2}}=\frac{r_{2}{ }^{2}}{r_{1}{ }^{2}}
$$

This inverse-square law states that the intensity decreases in proportion to the square of the distance from the source. Equation 17.5 tells us that the intensity is proportional to $s_{\max }^{2}$. Setting the right side of Equation 17.5 equal to the right side


Figure 17.5 A spherical sound wave propagating radially outward from an oscillating spherical body. The intensity of the spherical wave varies as $1 / r^{2}$.


Figure 17.6 Spherical waves emitted by a point source. The circular arcs represent the spherical wave fronts that are concentric with the source. The rays are radial lines pointing outward from the source, perpendicular to the wave fronts.


Figure 17.7 Far away from a point source, the wave fronts are nearly parallel planes, and the rays are nearly parallel lines perpendicular to the planes. Hence, a small segment of a spherical wave front is approximately a plane wave.
of Equation 17.8, we conclude that the displacement amplitude $s_{\max }$ of a spherical wave must vary as $1 / r$. Therefore, we can write the wave function $\psi$ (Greek letter psi) for an outgoing spherical wave in the form

$$
\begin{equation*}
\psi(r, t)=\frac{s_{0}}{r} \sin (k r-\omega t) \tag{17.9}
\end{equation*}
$$

where $s_{0}$, the displacement amplitude at unit distance from the source, is a constant parameter characterizing the whole wave.

It is useful to represent spherical waves with a series of circular arcs concentric with the source, as shown in Figure 17.6. Each arc represents a surface over which the phase of the wave is constant. We call such a surface of constant phase a wave front. The distance between adjacent wave fronts equals the wavelength $\lambda$. The radial lines pointing outward from the source are called rays.

Now consider a small portion of a wave front far from the source, as shown in Figure 17.7. In this case, the rays passing through the wave front are nearly parallel to one another, and the wave front is very close to being planar. Therefore, at distances from the source that are great compared with the wavelength, we can approximate a wave front with a plane. Any small portion of a spherical wave far from its source can be considered a plane wave.

Figure 17.8 illustrates a plane wave propagating along the $x$ axis, which means that the wave fronts are parallel to the $y z$ plane. In this case, the wave function depends only on $x$ and $t$ and has the form

$$
\begin{equation*}
\psi(x, t)=A \sin (k x-\omega t) \tag{17.10}
\end{equation*}
$$



Figure 17.8 A representation of a plane wave moving in the positive $x$ direction with a speed $v$. The wave fronts are planes parallel to the $y z$ plane.

Representation of a plane wave

That is, the wave function for a plane wave is identical in form to that for a onedimensional traveling wave.

The intensity is the same at all points on a given wave front of a plane wave.

## EXAMPLE 17.5 Intensity Variations of a Point Source

A point source emits sound waves with an average power output of 80.0 W . (a) Find the intensity 3.00 m from the source.

Solution A point source emits energy in the form of spherical waves (see Fig. 17.5). At a distance $r$ from the source, the power is distributed over the surface area of a sphere, $4 \pi r^{2}$. Therefore, the intensity at the distance $r$ is given by Equation 17.8:

$$
I=\frac{\mathscr{P}_{\mathrm{av}}}{4 \pi r^{2}}=\frac{80.0 \mathrm{~W}}{4 \pi(3.00 \mathrm{~m})^{2}}=0.707 \mathrm{~W} / \mathrm{m}^{2}
$$

an intensity that is close to the threshold of pain.
(b) Find the distance at which the sound level is 40 dB .

Solution We can find the intensity at the $40-\mathrm{dB}$ sound level by using Equation 17.7 with $I_{0}=1.00 \times 10^{-12} \mathrm{~W} / \mathrm{m}^{2}$ :

$$
\begin{aligned}
10 \log \left(\frac{I}{I_{0}}\right) & =40 \mathrm{~dB} \\
\log I-\log I_{0} & =\frac{40}{10}=4 \\
\log I & =4+\log 10^{-12} \\
\log I & =-8 \\
I & =1.00 \times 10^{-8} \mathrm{~W} / \mathrm{m}^{2}
\end{aligned}
$$

Using this value for $I$ in Equation 17.8 and solving for $r$, we obtain

$$
\begin{aligned}
r & =\sqrt{\frac{\mathscr{P} \text { av }}{4 \pi I}}=\sqrt{\frac{80.0 \mathrm{~W}}{4 \pi \times 1.00 \times 10^{-8} \mathrm{~W} / \mathrm{m}^{2}}} \\
& =2.52 \times 10^{4} \mathrm{~m}
\end{aligned}
$$

which equals about 16 miles!

## QuickLab

(Before attempting to do this QuickLab, you should check to see whether it is legal to sound a horn in your area.) Sound your car horn while driving toward and away from a friend in a campus parking lot or on a country road. Try this at different speeds while driving toward and past the friend (not at the friend). Do the frequencies of the sounds your friend hears agree with what is described in the text?

### 17.5 THE DOPPLER EFFECT

Perhaps you have noticed how the sound of a vehicle's horn changes as the vehicle moves past you. The frequency of the sound you hear as the vehicle approaches you is higher than the frequency you hear as it moves away from you (see QuickLab). This is one example of the Doppler effect. ${ }^{3}$

To see what causes this apparent frequency change, imagine you are in a boat that is lying at anchor on a gentle sea where the waves have a period of $T=3.0 \mathrm{~s}$. This means that every 3.0 s a crest hits your boat. Figure 17.9 a shows this situation, with the water waves moving toward the left. If you set your watch to $t=0$ just as one crest hits, the watch reads 3.0 s when the next crest hits, 6.0 s when the third crest hits, and so on. From these observations you conclude that the wave frequency is $f=1 / T=(1 / 3.0) \mathrm{Hz}$. Now suppose you start your motor and head directly into the oncoming waves, as shown in Figure 17.9b. Again you set your watch to $t=0$ as a crest hits the front of your boat. Now, however, because you are moving toward the next wave crest as it moves toward you, it hits you less than 3.0 s after the first hit. In other words, the period you observe is shorter than the $3.0-\mathrm{s}$ period you observed when you were stationary. Because $f=1 / T$, you observe a higher wave frequency than when you were at rest.

If you turn around and move in the same direction as the waves (see Fig. 17.9c), you observe the opposite effect. You set your watch to $t=0$ as a crest hits the back of the boat. Because you are now moving away from the next crest, more than 3.0 s has elapsed on your watch by the time that crest catches you. Thus, you observe a lower frequency than when you were at rest.

These effects occur because the relative speed between your boat and the waves depends on the direction of travel and on the speed of your boat. When you are moving toward the right in Figure 17.9b, this relative speed is higher than that of the wave speed, which leads to the observation of an increased frequency. When you turn around and move to the left, the relative speed is lower, as is the observed frequency of the water waves.

Let us now examine an analogous situation with sound waves, in which the water waves become sound waves, the water becomes the air, and the person on the boat becomes an observer listening to the sound. In this case, an observer $O$ is moving and a sound source $S$ is stationary. For simplicity, we assume that the air is also stationary and that the observer moves directly toward the source. The observer moves with a speed $v_{O}$ toward a stationary point source $\left(v_{S}=0\right)$ (Fig. 17.10). In general, at rest means at rest with respect to the medium, air.

[^2]

Figure 17.9 (a) Waves moving toward a stationary boat. The waves travel to the left, and their source is far to the right of the boat, out of the frame of the drawing. (b) The boat moving toward the wave source. (c) The boat moving away from the wave source.

We take the frequency of the source to be $f$, the wavelength to be $\lambda$, and the speed of sound to be $v$. If the observer were also stationary, he or she would detect $f$ wave fronts per second. (That is, when $v_{O}=0$ and $v_{S}=0$, the observed frequency equals the source frequency.) When the observer moves toward the source,


Figure 17.10 An observer O (the cyclist) moves with a speed $v_{O}$ toward a stationary point source S, the horn of a parked car. The observer hears a frequency $f^{\prime}$ that is greater than the source frequency.

Frequency heard with an observer in motion
the speed of the waves relative to the observer is $v^{\prime}=v+v_{O}$, as in the case of the boat, but the wavelength $\lambda$ is unchanged. Hence, using Equation 16.14, $v=\lambda f$, we can say that the frequency heard by the observer is increased and is given by

$$
f^{\prime}=\frac{v^{\prime}}{\lambda}=\frac{v+v_{O}}{\lambda}
$$

Because $\lambda=v / f$, we can express $f^{\prime}$ as

$$
\begin{equation*}
f^{\prime}=\left(1+\frac{v_{O}}{v}\right) f \quad \text { (observer moving toward source) } \tag{17.11}
\end{equation*}
$$

If the observer is moving away from the source, the speed of the wave relative to the observer is $v^{\prime}=v-v_{O}$. The frequency heard by the observer in this case is decreased and is given by

$$
\begin{equation*}
f^{\prime}=\left(1-\frac{v_{O}}{v}\right) f \quad \text { (observer moving away from source) } \tag{17.12}
\end{equation*}
$$

In general, whenever an observer moves with a speed $v_{O}$ relative to a stationary source, the frequency heard by the observer is

$$
\begin{equation*}
f^{\prime}=\left(1 \pm \frac{v_{O}}{v}\right) f \tag{17.13}
\end{equation*}
$$

where the positive sign is used when the observer moves toward the source and the negative sign is used when the observer moves away from the source.

Now consider the situation in which the source is in motion and the observer is at rest. If the source moves directly toward observer A in Figure 17.11a, the wave fronts heard by the observer are closer together than they would be if the source were not moving. As a result, the wavelength $\lambda^{\prime}$ measured by observer A is shorter than the wavelength $\lambda$ of the source. During each vibration, which lasts for a time $T$ (the period), the source moves a distance $v_{S} T=v_{S} / f$ and the wavelength is

(a)

Figure 17.11 (a) A source S moving with a speed $v_{S}$ toward a stationary observer A and away from a stationary observer B. Observer A hears an increased frequency, and observer B hears a decreased frequency. (b) The Doppler effect in water, observed in a ripple tank. A point source is moving to the right with speed $v_{S}$.
(b)

shortened by this amount. Therefore, the observed wavelength $\lambda^{\prime}$ is

$$
\lambda^{\prime}=\lambda-\Delta \lambda=\lambda-\frac{v_{S}}{f}
$$

Because $\lambda=v / f$, the frequency heard by observer A is

$$
\begin{align*}
& f^{\prime}=\frac{v}{\lambda^{\prime}}=\frac{v}{\lambda-\frac{v_{S}}{f}}=\frac{v}{\frac{v}{f}-\frac{v_{S}}{f}} \\
& f^{\prime}=\left(\frac{1}{1-\frac{v_{S}}{v}}\right) f \tag{17.14}
\end{align*}
$$

That is, the observed frequency is increased whenever the source is moving toward the observer.

When the source moves away from a stationary observer, as is the case for observer B in Figure 17.11a, the observer measures a wavelength $\lambda^{\prime}$ that is greater than $\lambda$ and hears a decreased frequency:

$$
\begin{equation*}
f^{\prime}=\left(\frac{1}{1+\frac{v_{S}}{v}}\right) f \tag{17.15}
\end{equation*}
$$

Combining Equations 17.14 and 17.15, we can express the general relationship for the observed frequency when a source is moving and an observer is at rest as

$$
\begin{equation*}
f^{\prime}=\left(\frac{1}{1 \mp \frac{v_{S}}{v}}\right) f \tag{17.16}
\end{equation*}
$$

Finally, if both source and observer are in motion, we find the following general relationship for the observed frequency:

$$
\begin{equation*}
f^{\prime}=\left(\frac{v \pm v_{O}}{v \mp v_{S}}\right) f \tag{17.17}
\end{equation*}
$$

In this expression, the upper signs $\left(+v_{O}\right.$ and $\left.-v_{S}\right)$ refer to motion of one toward the other, and the lower signs $\left(-v_{O}\right.$ and $\left.+v_{S}\right)$ refer to motion of one away from the other.

A convenient rule concerning signs for you to remember when working with all Doppler-effect problems is as follows:

The word toward is associated with an increase in observed frequency. The words away from are associated with a decrease in observed frequency.

Although the Doppler effect is most typically experienced with sound waves, it is a phenomenon that is common to all waves. For example, the relative motion of source and observer produces a frequency shift in light waves. The Doppler effect is used in police radar systems to measure the speeds of motor vehicles. Likewise, astronomers use the effect to determine the speeds of stars, galaxies, and other celestial objects relative to the Earth.

"I love hearing that lonesome wail of the train whistle as the magnitude of the frequency of the wave changes due to the Doppler effect."

Frequency heard with source in motion

Frequency heard with observer and source in motion

## EXAMPLE 17.6 The Noisy Siren

As an ambulance travels east down a highway at a speed of $33.5 \mathrm{~m} / \mathrm{s}(75 \mathrm{mi} / \mathrm{h})$, its siren emits sound at a frequency of 400 Hz . What frequency is heard by a person in a car traveling west at $24.6 \mathrm{~m} / \mathrm{s}(55 \mathrm{mi} / \mathrm{h})$ (a) as the car approaches the ambulance and (b) as the car moves away from the ambulance?

Solution (a) We can use Equation 17.17 in both cases, taking the speed of sound in air to be $v=343 \mathrm{~m} / \mathrm{s}$. As the ambulance and car approach each other, the person in the car hears the frequency

$$
\begin{aligned}
f^{\prime} & =\left(\frac{v+v_{O}}{v-v_{S}}\right) f=\left(\frac{343 \mathrm{~m} / \mathrm{s}+24.6 \mathrm{~m} / \mathrm{s}}{343 \mathrm{~m} / \mathrm{s}-33.5 \mathrm{~m} / \mathrm{s}}\right)(400 \mathrm{~Hz}) \\
& =475 \mathrm{~Hz}
\end{aligned}
$$

(b) As the vehicles recede from each other, the person hears the frequency

$$
\begin{aligned}
f^{\prime} & =\left(\frac{v-v_{O}}{v+v_{S}}\right) f=\left(\frac{343 \mathrm{~m} / \mathrm{s}-24.6 \mathrm{~m} / \mathrm{s}}{343 \mathrm{~m} / \mathrm{s}+33.5 \mathrm{~m} / \mathrm{s}}\right)(400 \mathrm{~Hz}) \\
& =338 \mathrm{~Hz}
\end{aligned}
$$

The change in frequency detected by the person in the car is $475-338=137 \mathrm{~Hz}$, which is more than $30 \%$ of the true frequency.

Exercise Suppose the car is parked on the side of the highway as the ambulance speeds by. What frequency does the person in the car hear as the ambulance (a) approaches and (b) recedes?

Answer (a) 443 Hz . (b) 364 Hz .

## Shock Waves

Now let us consider what happens when the speed $v_{S}$ of a source exceeds the wave speed $v$. This situation is depicted graphically in Figure 17.12a. The circles represent spherical wave fronts emitted by the source at various times during its motion. At $t=0$, the source is at $S_{0}$, and at a later time $t$, the source is at $S_{n}$. In the time $t$,



Figure 17.13 The V-shaped bow wave of a boat is formed because the boat speed is greater than the speed of the water waves. A bow wave is analogous to a shock wave formed by an airplane traveling faster than sound.
the wave front centered at $S_{0}$ reaches a radius of $v t$. In this same amount of time, the source travels a distance $v_{S} t$ to $S_{n}$. At the instant the source is at $S_{n}$, waves are just beginning to be generated at this location, and hence the wave front has zero radius at this point. The tangent line drawn from $S_{n}$ to the wave front centered on $S_{0}$ is tangent to all other wave fronts generated at intermediate times. Thus, we see that the envelope of these wave fronts is a cone whose apex half-angle $\theta$ is given by

$$
\sin \theta=\frac{v t}{v_{S} t}=\frac{v}{v_{S}}
$$

The ratio $v_{S} / v$ is referred to as the Mach number, and the conical wave front produced when $v_{S}>v$ (supersonic speeds) is known as a shock wave. An interesting analogy to shock waves is the V -shaped wave fronts produced by a boat (the bow wave) when the boat's speed exceeds the speed of the surface-water waves (Fig. 17.13).

Jet airplanes traveling at supersonic speeds produce shock waves, which are responsible for the loud "sonic boom" one hears. The shock wave carries a great deal of energy concentrated on the surface of the cone, with correspondingly great pressure variations. Such shock waves are unpleasant to hear and can cause damage to buildings when aircraft fly supersonically at low altitudes. In fact, an airplane flying at supersonic speeds produces a double boom because two shock fronts are formed, one from the nose of the plane and one from the tail (Fig. 17.14). People near the path of the space shuttle as it glides toward its landing point often report hearing what sounds like two very closely spaced cracks of thunder.

## Quick Quiz 17.5

An airplane flying with a constant velocity moves from a cold air mass into a warm air mass. Does the Mach number increase, decrease, or stay the same?

## Quick Quiz 17.6

Suppose that an observer and a source of sound are both at rest and that a strong wind blows from the source toward the observer. Describe the effect of the wind (if any) on


Figure 17.14 The two shock waves produced by the nose and tail of a jet airplane traveling at supersonic speeds.
(a) the observed frequency of the sound waves, (b) the observed wave speed, and (c) the observed wavelength.

## SUMMARY

Sound waves are longitudinal and travel through a compressible medium with a speed that depends on the compressibility and inertia of that medium. The speed of sound in a medium having a bulk modulus $B$ and density $\rho$ is

$$
\begin{equation*}
v=\sqrt{\frac{B}{\rho}} \tag{17.1}
\end{equation*}
$$

With this formula you can determine the speed of a sound wave in many different materials.

For sinusoidal sound waves, the variation in the displacement is given by

$$
\begin{equation*}
s(x, t)=s_{\max } \cos (k x-\omega t) \tag{17.2}
\end{equation*}
$$

and the variation in pressure from the equilibrium value is

$$
\begin{equation*}
\Delta P=\Delta P_{\max } \sin (k x-\omega t) \tag{17.3}
\end{equation*}
$$

where $\Delta P_{\text {max }}$ is the pressure amplitude. The pressure wave is $90^{\circ}$ out of phase with the displacement wave. The relationship between $s_{\max }$ and $\Delta P_{\max }$ is given by

$$
\begin{equation*}
\Delta P_{\max }=\rho v \omega s_{\max } \tag{17.4}
\end{equation*}
$$

The intensity of a periodic sound wave, which is the power per unit area, is

$$
\begin{equation*}
I=\frac{1}{2} \rho v\left(\omega s_{\max }\right)^{2}=\frac{\Delta P_{\max }^{2}}{2 \rho v} \tag{17.5,17.6}
\end{equation*}
$$

The sound level of a sound wave, in decibels, is given by

$$
\begin{equation*}
\beta=10 \log \left(\frac{I}{I_{0}}\right) \tag{17.7}
\end{equation*}
$$

The constant $I_{0}$ is a reference intensity, usually taken to be at the threshold of hearing $\left(1.00 \times 10^{-12} \mathrm{~W} / \mathrm{m}^{2}\right)$, and $I$ is the intensity of the sound wave in watts per square meter.

The intensity of a spherical wave produced by a point source is proportional to the average power emitted and inversely proportional to the square of the distance from the source:

$$
\begin{equation*}
I=\frac{\mathscr{P}_{\mathrm{av}}}{4 \pi r^{2}} \tag{17.8}
\end{equation*}
$$

The change in frequency heard by an observer whenever there is relative motion between a source of sound waves and the observer is called the Doppler effect. The observed frequency is

$$
\begin{equation*}
f^{\prime}=\left(\frac{v \pm v_{O}}{v \mp v_{S}}\right) f \tag{17.17}
\end{equation*}
$$

The upper signs $\left(+v_{O}\right.$ and $\left.-v_{S}\right)$ are used with motion of one toward the other, and the lower signs $\left(-v_{O}\right.$ and $\left.+v_{S}\right)$ are used with motion of one away from the other. You can also use this formula when $v_{O}$ or $v_{S}$ is zero.

## Questions

1. Why are sound waves characterized as longitudinal?
2. If an alarm clock is placed in a good vacuum and then activated, no sound is heard. Explain.
3. A sonic ranger is a device that determines the position of an object by sending out an ultrasonic sound pulse and measuring how long it takes for the sound wave to return after it reflects from the object. Typically, these devices cannot reliably detect an object that is less than half a meter from the sensor. Why is that?
4. In Example 17.5, we found that a point source with a power output of 80 W reduces to a sound level of 40 dB at a distance of about 16 miles. Why do you suppose you cannot normally hear a rock concert that is going on 16 miles away? (See Table 17.2.)
5. If the distance from a point source is tripled, by what factor does the intensity decrease?
6. Explain how the Doppler effect is used with microwaves to determine the speed of an automobile.
7. Explain what happens to the frequency of your echo as you move in a vehicle toward a canyon wall. What happens to the frequency as you move away from the wall?
8. Of the following sounds, which is most likely to have a sound level of 60 dB - a rock concert, the turning of a page in this text, normal conversation, or a cheering crowd at a football game?
9. Estimate the decibel level of each of the sounds in the previous question.
10. A binary star system consists of two stars revolving about their common center of mass. If we observe the light reaching us from one of these stars as it makes one complete revolution, what does the Doppler effect predict will happen to this light?
11. How can an object move with respect to an observer so that the sound from it is not shifted in frequency?
12. Why is it not possible to use sonar (sound waves) to determine the speed of an object traveling faster than the speed of sound in a given medium?
13. Why is it so quiet after a snowfall?
14. Why is the intensity of an echo less than that of the original sound?
15. If the wavelength of a sound source is reduced by a factor of 2 , what happens to its frequency? Its speed?
16. In a recent discovery, a nearby star was found to have a large planet orbiting about it, although the planet could not be seen. In terms of the concept of a system rotating about its center of mass and the Doppler shift for light (which is in many ways similar to that for sound), explain how an astronomer could determine the presence of the invisible planet.
17. A friend sitting in her car far down the road waves to you and beeps her horn at the same time. How far away must her car be for you to measure the speed of sound to two significant figures by measuring the time it takes for the sound to reach you?

## Problems

1, 2, 3 = straightforward, intermediate, challenging $\quad \square$ = full solution available in the Student Solutions Manual and Study Guide W\&B = solution posted at http://www.saunderscollege.com/physics/ $\square=$ Computer useful in solving problem $Z=$ Interactive Physics $\square$ = paired numerical/symbolic problems

## Section 17.1 Speed of Sound Waves

1. Suppose that you hear a clap of thunder 16.2 s after seeing the associated lightning stroke. The speed of sound waves in air is $343 \mathrm{~m} / \mathrm{s}$, and the speed of light in air is $3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}$. How far are you from the lightning stroke?
2. Find the speed of sound in mercury, which has a bulk modulus of approximately $2.80 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$ and a density of $13600 \mathrm{~kg} / \mathrm{m}^{3}$.
3. A flower pot is knocked off a balcony 20.0 m above the sidewalk and falls toward an unsuspecting $1.75-\mathrm{m}$-tall man who is standing below. How close to the sidewalk can the flower pot fall before it is too late for a shouted warning from the balcony to reach the man in time? Assume that the man below requires 0.300 s to respond to the warning.
4. You are watching a pier being constructed on the far shore of a saltwater inlet when some blasting occurs.

You hear the sound in the water 4.50 s before it reaches you through the air. How wide is the inlet? (Hint: See Table 17.1. Assume that the air temperature is $20^{\circ} \mathrm{C}$.)
5. Another approximation of the temperature dependence of the speed of sound in air (in meters per second) is given by the expression

$$
v=331.5+0.607 T_{\mathrm{C}}
$$

where $T_{\mathrm{C}}$ is the Celsius temperature. In dry air the temperature decreases about $1^{\circ} \mathrm{C}$ for every $150-\mathrm{m}$ rise in altitude. (a) Assuming that this change is constant up to an altitude of 9000 m , how long will it take the sound from an airplane flying at 9000 m to reach the ground on a day when the ground temperature is $30^{\circ} \mathrm{C}$ ?
(b) Compare this to the time it would take if the air were at $30^{\circ} \mathrm{C}$ at all altitudes. Which interval is longer?
6. A bat can detect very small objects, such as an insect whose length is approximately equal to one wavelength
of the sound the bat makes. If bats emit a chirp at a frequency of 60.0 kHz , and if the speed of sound in air is $340 \mathrm{~m} / \mathrm{s}$, what is the smallest insect a bat can detect?
7. An airplane flies horizontally at a constant speed, piloted by rescuers who are searching for a disabled boat. When the plane is directly above the boat, the boat's crew blows a loud horn. By the time the plane's sound detector receives the horn's sound, the plane has traveled a distance equal to one-half its altitude above the ocean. If it takes the sound 2.00 s to reach the plane, determine (a) the speed of the plane and (b) its altitude. Take the speed of sound to be $343 \mathrm{~m} / \mathrm{s}$.

## Section 17.2 Periodic Sound Waves

Note: In this section, use the following values as needed, unless otherwise specified. The equilibrium density of air is $\rho=$ $1.20 \mathrm{~kg} / \mathrm{m}^{3}$; the speed of sound in air is $v=343 \mathrm{~m} / \mathrm{s}$. Pressure variations $\Delta P$ are measured relative to atmospheric pressure, $1.013 \times 10^{5} \mathrm{~Pa}$.
8. A sound wave in air has a pressure amplitude equal to $4.00 \times 10^{-3} \mathrm{~Pa}$. Calculate the displacement amplitude of the wave at a frequency of 10.0 kHz .
9. A sinusoidal sound wave is described by the displacement

$$
s(x, t)=(2.00 \mu \mathrm{~m}) \cos \left[\left(15.7 \mathrm{~m}^{-1}\right) x-\left(858 \mathrm{~s}^{-1}\right) t\right]
$$

(a) Find the amplitude, wavelength, and speed of this wave. (b) Determine the instantaneous displacement of the molecules at the position $x=0.0500 \mathrm{~m}$ at $t=3.00 \mathrm{~ms}$. (c) Determine the maximum speed of a molecule's oscillatory motion.
10. As a sound wave travels through the air, it produces pressure variations (above and below atmospheric pressure) that are given by $\Delta P=1.27 \sin (\pi x-340 \pi t)$ in SI units. Find (a) the amplitude of the pressure variations, (b) the frequency of the sound wave, (c) its wavelength in air, and (d) its speed.
11. Write an expression that describes the pressure variation as a function of position and time for a sinusoidal sound wave in air, if $\lambda=0.100 \mathrm{~m}$ and $\Delta P_{\text {max }}=$ 0.200 Pa .
12. Write the function that describes the displacement wave corresponding to the pressure wave in Problem 11.
13. The tensile stress in a thick copper bar is $99.5 \%$ of its elastic breaking point of $13.0 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$. A $500-\mathrm{Hz}$ sound wave is transmitted through the material.
(a) What displacement amplitude will cause the bar to break? (b) What is the maximum speed of the particles at this moment?
14. Calculate the pressure amplitude of a $2.00-\mathrm{kHz}$ sound wave in air if the displacement amplitude is equal to $2.00 \times 10^{-8} \mathrm{~m}$.
$\mathbf{w \& s}$ 15. An experimenter wishes to generate in air a sound wave that has a displacement amplitude of $5.50 \times 10^{-6} \mathrm{~m}$. The pressure amplitude is to be limited to $8.40 \times 10^{-1} \mathrm{~Pa}$. What is the minimum wavelength the sound wave can have?
16. A sound wave in air has a pressure amplitude of 4.00 Pa and a frequency of 5.00 kHz . Take $\Delta P=0$ at the point $x=0$ when $t=0$. (a) What is $\Delta P$ at $x=0$ when $t=$ $2.00 \times 10^{-4} \mathrm{~s}$ ? (b) What is $\Delta P$ at $x=0.0200 \mathrm{~m}$ when $t=0$ ?

## Section 17.3 Intensity of Periodic Sound Waves

17. Calculate the sound level, in decibels, of a sound wave that has an intensity of $4.00 \mu \mathrm{~W} / \mathrm{m}^{2}$.
18. A vacuum cleaner has a measured sound level of 70.0 dB . (a) What is the intensity of this sound in watts per square meter? (b) What is the pressure amplitude of the sound?
19. The intensity of a sound wave at a fixed distance from a speaker vibrating at 1.00 kHz is $0.600 \mathrm{~W} / \mathrm{m}^{2}$. (a) Determine the intensity if the frequency is increased to 2.50 kHz while a constant displacement amplitude is maintained. (b) Calculate the intensity if the frequency is reduced to 0.500 kHz and the displacement amplitude is doubled.
20. The intensity of a sound wave at a fixed distance from a speaker vibrating at a frequency $f$ is $I$. (a) Determine the intensity if the frequency is increased to $f^{\prime}$ while a constant displacement amplitude is maintained.
(b) Calculate the intensity if the frequency is reduced to $f / 2$ and the displacement amplitude is doubled.
21. A family ice show is held in an enclosed arena. The skaters perform to music with a sound level of 80.0 dB . This is too loud for your baby, who consequently yells at a level of 75.0 dB . (a) What total sound intensity engulfs you? (b) What is the combined sound level?

## Section 17.4 Spherical and Plane Waves

22. For sound radiating from a point source, show that the difference in sound levels, $\beta_{1}$ and $\beta_{2}$, at two receivers is related to the ratio of the distances $r_{1}$ and $r_{2}$ from the source to the receivers by the expression

$$
\beta_{2}-\beta_{1}=20 \log \left(\frac{r_{1}}{r_{2}}\right)
$$

23. A fireworks charge is detonated many meters above the ground. At a distance of 400 m from the explosion, the acoustic pressure reaches a maximum of $10.0 \mathrm{~N} / \mathrm{m}^{2}$. Assume that the speed of sound is constant at $343 \mathrm{~m} / \mathrm{s}$ throughout the atmosphere over the region considered, that the ground absorbs all the sound falling on it, and that the air absorbs sound energy as described by the rate $7.00 \mathrm{~dB} / \mathrm{km}$. What is the sound level (in decibels) at 4.00 km from the explosion?
24. A loudspeaker is placed between two observers who are 110 m apart, along the line connecting them. If one observer records a sound level of 60.0 dB and the other records a sound level of 80.0 dB , how far is the speaker from each observer?
25. Two small speakers emit spherical sound waves of different frequencies. Speaker $A$ has an output of 1.00 mW , and speaker $B$ has an output of 1.50 mW . Determine the sound level (in decibels) at point $C$ (Fig. P17.25) if (a) only speaker $A$ emits sound, (b) only speaker $B$ emits sound, (c) both speakers emit sound.


Figure P17.25
26. An experiment requires a sound intensity of $1.20 \mathrm{~W} / \mathrm{m}^{2}$ at a distance of 4.00 m from a speaker. What power output is required? Assume that the speaker radiates sound equally in all directions.
27. A source of sound ( 1000 Hz ) emits uniformly in all directions. An observer 3.00 m from the source measures a sound level of 40.0 dB . Calculate the average power output of the source.
28. A jackhammer, operated continuously at a construction site, behaves as a point source of spherical sound waves. A construction supervisor stands 50.0 m due north of this sound source and begins to walk due west. How far does she have to walk in order for the amplitude of the wave function to drop by a factor of 2.00 ?
29. The sound level at a distance of 3.00 m from a source is 120 dB . At what distances is the sound level (a) 100 dB and (b) 10.0 dB ?
30. A fireworks rocket explodes 100 m above the ground. An observer directly under the explosion experiences an average sound intensity of $7.00 \times 10^{-2} \mathrm{~W} / \mathrm{m}^{2}$ for 0.200 s .
(a) What is the total sound energy of the explosion? (b) What sound level, in decibels, is heard by the observer?
31. As the people in a church sing on a summer morning, the sound level everywhere inside the church is 101 dB . The massive walls are opaque to sound, but all the windows and doors are open. Their total area is $22.0 \mathrm{~m}^{2}$.
(a) How much sound energy is radiated in 20.0 min ?
(b) Suppose the ground is a good reflector and sound
radiates uniformly in all horizontal and upward directions. Find the sound level 1.00 km away.
32. A spherical wave is radiating from a point source and is described by the wave function

$$
\Delta P(r, t)=\left[\frac{25.0}{r}\right] \sin (1.25 r-1870 t)
$$

where $\Delta P$ is in pascals, $r$ in meters, and $t$ in seconds. (a) What is the pressure amplitude 4.00 m from the source? (b) Determine the speed of the wave and hence the material the wave might be traveling through.
(c) Find the sound level of the wave, in decibels, 4.00 m from the source. (d) Find the instantaneous pressure 5.00 m from the source at 0.0800 s .

## Section 17.5 The Doppler Effect

33. A commuter train passes a passenger platform at a constant speed of $40.0 \mathrm{~m} / \mathrm{s}$. The train horn is sounded at its characteristic frequency of 320 Hz . (a) What change in frequency is detected by a person on the platform as the train passes? (b) What wavelength is detected by a person on the platform as the train approaches?
34. A driver travels northbound on a highway at a speed of $25.0 \mathrm{~m} / \mathrm{s}$. A police car, traveling southbound at a speed of $40.0 \mathrm{~m} / \mathrm{s}$, approaches with its siren sounding at a frequency of 2500 Hz . (a) What frequency does the driver observe as the police car approaches? (b) What frequency does the driver detect after the police car passes him? (c) Repeat parts (a) and (b) for the case in which the police car is northbound.
Wยв 35. Standing at a crosswalk, you hear a frequency of 560 Hz from the siren of an approaching police car. After the police car passes, the observed frequency of the siren is 480 Hz . Determine the car's speed from these observations.
35. Expectant parents are thrilled to hear their unborn baby's heartbeat, revealed by an ultrasonic motion detector. Suppose the fetus's ventricular wall moves in simple harmonic motion with an amplitude of 1.80 mm and a frequency of 115 per minute. (a) Find the maximum linear speed of the heart wall. Suppose the motion detector in contact with the mother's abdomen produces sound at 2000000.0 Hz , which travels through tissue at $1.50 \mathrm{~km} / \mathrm{s}$. (b) Find the maximum frequency at which sound arrives at the wall of the baby's heart. (c) Find the maximum frequency at which reflected sound is received by the motion detector. (By electronically "listening" for echoes at a frequency different from the broadcast frequency, the motion detector can produce beeps of audible sound in synchronization with the fetal heartbeat.)
36. A tuning fork vibrating at 512 Hz falls from rest and accelerates at $9.80 \mathrm{~m} / \mathrm{s}^{2}$. How far below the point of release is the tuning fork when waves with a frequency of 485 Hz reach the release point? Take the speed of sound in air to be $340 \mathrm{~m} / \mathrm{s}$.
37. A block with a speaker bolted to it is connected to a spring having spring constant $k=20.0 \mathrm{~N} / \mathrm{m}$, as shown in Figure P17.38. The total mass of the block and speaker is 5.00 kg , and the amplitude of this unit's motion is 0.500 m . (a) If the speaker emits sound waves of frequency 440 Hz , determine the highest and lowest frequencies heard by the person to the right of the speaker. (b) If the maximum sound level heard by the person is 60.0 dB when he is closest to the speaker, 1.00 m away, what is the minimum sound level heard by the observer? Assume that the speed of sound is $343 \mathrm{~m} / \mathrm{s}$.


Figure P17.38
39. A train is moving parallel to a highway with a constant speed of $20.0 \mathrm{~m} / \mathrm{s}$. A car is traveling in the same direction as the train with a speed of $40.0 \mathrm{~m} / \mathrm{s}$. The car horn sounds at a frequency of 510 Hz , and the train whistle sounds at a frequency of 320 Hz . (a) When the car is behind the train, what frequency does an occupant of the car observe for the train whistle? (b) When the car is in front of the train, what frequency does a train passenger observe for the car horn just after the car passes?
40. At the Winter Olympics, an athlete rides her luge down the track while a bell just above the wall of the chute rings continuously. When her sled passes the bell, she hears the frequency of the bell fall by the musical interval called a minor third. That is, the frequency she hears drops to five sixths of its original value. (a) Find the speed of sound in air at the ambient temperature $-10.0^{\circ} \mathrm{C}$. (b) Find the speed of the athlete.
41. A jet fighter plane travels in horizontal flight at Mach 1.20 (that is, 1.20 times the speed of sound in air). At the instant an observer on the ground hears the shock wave, what is the angle her line of sight makes with the horizontal as she looks at the plane?
42. When high-energy charged particles move through a transparent medium with a speed greater than the speed of light in that medium, a shock wave, or bow wave, of light is produced. This phenomenon is called the Cerenkov effect and can be observed in the vicinity of the core of a swimming-pool nuclear reactor due to
high-speed electrons moving through the water. In a particular case, the Cerenkov radiation produces a wave front with an apex half-angle of $53.0^{\circ}$. Calculate the speed of the electrons in the water. (The speed of light in water is $2.25 \times 10^{8} \mathrm{~m} / \mathrm{s}$.)
wes 43. A supersonic jet traveling at Mach 3.00 at an altitude of 20000 m is directly over a person at time $t=0$, as in Figure P17.43. (a) How long will it be before the person encounters the shock wave? (b) Where will the plane be when it is finally heard? (Assume that the speed of sound in air is $335 \mathrm{~m} / \mathrm{s}$.)


Figure P17.43
44. The tip of a circus ringmaster's whip travels at Mach 1.38 (that is, $v_{S} / v=1.38$ ). What angle does the shock front make with the direction of the whip's motion?

## ADDITIONAL PROBLEMS

45. A stone is dropped into a deep canyon and is heard to strike the bottom 10.2 s after release. The speed of sound waves in air is $343 \mathrm{~m} / \mathrm{s}$. How deep is the canyon? What would be the percentage error in the calculated depth if the time required for the sound to reach the canyon rim were ignored?
46. Unoccupied by spectators, a large set of football bleachers has solid seats and risers. You stand on the field in front of it and fire a starter's pistol or sharply clap two wooden boards together once. The sound pulse you produce has no frequency and no wavelength. You hear back from the bleachers a sound with definite pitch, which may remind you of a short toot on a trumpet, or of a buzzer or a kazoo. Account for this sound. Compute order-of-magnitude estimates for its frequency, wavelength, and duration on the basis of data that you specify.
47. Many artists sing very high notes in ornaments and cadenzas. The highest note written for a singer in a published score was F-sharp above high C, 1.480 kHz , sung
by Zerbinetta in the original version of Richard Strauss's opera Ariadne auf Naxos. (a) Find the wavelength of this sound in air. (b) Suppose that the people in the fourth row of seats hear this note with a level of 81.0 dB . Find the displacement amplitude of the sound. (c) In response to complaints, Strauss later transposed the note down to F above high C, 1.397 kHz . By what increment did the wavelength change?
48. A sound wave in a cylinder is described by Equations 17.2 through 17.4. Show that $\Delta P= \pm \rho v \omega \sqrt{s_{\text {max }}^{2}-s^{2}}$.
49. On a Saturday morning, pickup trucks carrying garbage to the town dump form a nearly steady procession on a country road, all traveling at $19.7 \mathrm{~m} / \mathrm{s}$. From this direction, two trucks arrive at the dump every three minutes. A bicyclist also is traveling toward the dump at $4.47 \mathrm{~m} / \mathrm{s}$. (a) With what frequency do the trucks pass him? (b) A hill does not slow the trucks but makes the out-of-shape cyclist's speed drop to $1.56 \mathrm{~m} / \mathrm{s}$. How often do the noisy trucks whiz past him now?
50. The ocean floor is underlain by a layer of basalt that constitutes the crust, or uppermost layer, of the Earth in that region. Below the crust is found denser peridotite rock, which forms the Earth's mantle. The boundary between these two layers is called the Mohorovicic discontinuity ("Moho" for short). If an explosive charge is set off at the surface of the basalt, it generates a seismic wave that is reflected back out at the Moho. If the speed of the wave in basalt is $6.50 \mathrm{~km} / \mathrm{s}$ and the two-way travel time is 1.85 s , what is the thickness of this oceanic crust?
51. A worker strikes a steel pipeline with a hammer, generating both longitudinal and transverse waves. Reflected waves return 2.40 s apart. How far away is the reflection point? (For steel, $v_{\text {long }}=6.20 \mathrm{~km} / \mathrm{s}$ and $v_{\text {trans }}=$ $3.20 \mathrm{~km} / \mathrm{s}$.)
52. For a certain type of steel, stress is proportional to strain with Young's modulus as given in Table 12.1. The steel has the density listed for iron in Table 15.1. It bends permanently if subjected to compressive stress greater than its elastic limit, $\sigma=400 \mathrm{MPa}$, also called its yield strength. A rod 80.0 cm long, made of this steel, is projected at $12.0 \mathrm{~m} / \mathrm{s}$ straight at a hard wall. (a) Find the speed of compressional waves moving along the rod. (b) After the front end of the rod hits the wall and stops, the back end of the rod keeps moving, as described by Newton's first law, until it is stopped by the excess pressure in a sound wave moving back through the rod. How much time elapses before the back end of the rod gets the message? (c) How far has the back end of the rod moved in this time? (d) Find the strain in the rod and (e) the stress. (f) If it is not to fail, show that the maximum impact speed a rod can have is given by the expression $\sigma / \sqrt{\rho Y}$.
53. To determine her own speed, a sky diver carries a buzzer that emits a steady tone at 1800 Hz . A friend at the landing site on the ground directly below the sky diver listens to the amplified sound he receives from the buzzer. Assume that the air is calm and that the speed
of sound is $343 \mathrm{~m} / \mathrm{s}$, independent of altitude. While the sky diver is falling at terminal speed, her friend on the ground receives waves with a frequency of 2150 Hz . (a) What is the sky diver's speed of descent? (b) Suppose the sky diver is also carrying sound-receiving equipment that is sensitive enough to detect waves reflected from the ground. What frequency does she receive?
54. A train whistle ( $f=400 \mathrm{~Hz}$ ) sounds higher or lower in pitch depending on whether it is approaching or receding. (a) Prove that the difference in frequency between the approaching and receding train whistle is

$$
\Delta f=\frac{2(u / v)}{1-\left(u^{2} / v^{2}\right)} f
$$

where $u$ is the speed of the train and $v$ is the speed of sound. (b) Calculate this difference for a train moving at a speed of $130 \mathrm{~km} / \mathrm{h}$. Take the speed of sound in air to be $340 \mathrm{~m} / \mathrm{s}$.
55. A bat, moving at $5.00 \mathrm{~m} / \mathrm{s}$, is chasing a flying insect. If the bat emits a $40.0-\mathrm{kHz}$ chirp and receives back an echo at 40.4 kHz , at what relative speed is the bat moving toward or away from the insect? (Take the speed of sound in air to be $v=340 \mathrm{~m} / \mathrm{s}$.)


Figure P17.55
56. A supersonic aircraft is flying parallel to the ground. When the aircraft is directly overhead, an observer on the ground sees a rocket fired from the aircraft. Ten seconds later the observer hears the sonic boom, which is followed 2.80 s later by the sound of the rocket engine. What is the Mach number of the aircraft?
57. A police car is traveling east at $40.0 \mathrm{~m} / \mathrm{s}$ along a straight road, overtaking a car that is moving east at $30.0 \mathrm{~m} / \mathrm{s}$. The police car has a malfunctioning siren that is stuck at 1000 Hz . (a) Sketch the appearance of the wave fronts of the sound produced by the siren. Show the
wave fronts both to the east and to the west of the police car. (b) What would be the wavelength in air of the siren sound if the police car were at rest? (c) What is the wavelength in front of the car? (d) What is the wavelength behind the police car? (e) What frequency is heard by the driver being chased?
58. A copper bar is given a sharp compressional blow at one end. The sound of the blow, traveling through air at $0^{\circ} \mathrm{C}$, reaches the opposite end of the bar 6.40 ms later than the sound transmitted through the metal of the bar. What is the length of the bar? (Refer to Table 17.1.)
59. The power output of a certain public address speaker is 6.00 W. Suppose it broadcasts equally in all directions. (a) Within what distance from the speaker would the sound be painful to the ear? (b) At what distance from the speaker would the sound be barely audible?
60. A jet flies toward higher altitude at a constant speed of $1963 \mathrm{~m} / \mathrm{s}$ in a direction that makes an angle $\theta$ with the horizontal (Fig. P17.60). An observer on the ground hears the jet for the first time when it is directly overhead. Determine the value of $\theta$ if the speed of sound in air is $340 \mathrm{~m} / \mathrm{s}$.


Figure P17.60

Two ships are moving along a line due east. The trailing vessel has a speed of $64.0 \mathrm{~km} / \mathrm{h}$ relative to a land-based observation point, and the leading ship has a speed of $45.0 \mathrm{~km} / \mathrm{h}$ relative to that point. The two ships are in a region of the ocean where the current is moving uniformly due west at $10.0 \mathrm{~km} / \mathrm{h}$. The trailing ship transmits a sonar signal at a frequency of 1200.0 Hz . What frequency is monitored by the leading ship? (Use $1520 \mathrm{~m} / \mathrm{s}$ as the speed of sound in ocean water.)
62. A microwave oven generates a sound with intensity level 40.0 dB everywhere just outside it, when consuming 1.00 kW of power. Find the fraction of this power that is converted into the energy of sound waves. Assume the dimensions of the oven are $40.0 \mathrm{~cm} \times 40.0 \mathrm{~cm} \times$ 50.0 cm .
63. A meteoroid the size of a truck enters the Earth's atmosphere at a speed of $20.0 \mathrm{~km} / \mathrm{s}$ and is not significantly slowed before entering the ocean. (a) What is the Mach angle of the shock wave from the meteoroid in the atmosphere? (Use $331 \mathrm{~m} / \mathrm{s}$ as the sound speed.) (b) Assuming that the meteoroid survives the impact with the ocean surface, what is the (initial) Mach angle of the shock wave that the meteoroid produces in the water? (Use the wave speed for sea water given in Table 17.1.)
64. Consider a longitudinal (compressional) wave of wavelength $\lambda$ traveling with speed $v$ along the $x$ direction through a medium of density $\rho$. The displacement of the molecules of the medium from their equilibrium position is

$$
s=s_{\max } \sin (k x-\omega t)
$$

Show that the pressure variation in the medium is given by

$$
\Delta P=-\left(\frac{2 \pi \rho v^{2}}{\lambda} s_{\max }\right) \cos (k x-\omega t)
$$

wes 65. By proper excitation, it is possible to produce both longitudinal and transverse waves in a long metal rod. A particular metal rod is 150 cm long and has a radius of 0.200 cm and a mass of 50.9 g . Young's modulus for the material is $6.80 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$. What must the tension in the rod be if the ratio of the speed of longitudinal waves to the speed of transverse waves is 8.00 ?
66. An interstate highway has been built through a neighborhood in a city. In the afternoon, the sound level in a rented room is 80.0 dB as 100 cars per minute pass outside the window. Late at night, the traffic flow on the freeway is only five cars per minute. What is the average late-night sound level in the room?
67. A siren creates a sound level of 60.0 dB at a location 500 m from the speaker. The siren is powered by a battery that delivers a total energy of 1.00 kJ . Assuming that the efficiency of the siren is $30.0 \%$ (that is, $30.0 \%$ of the supplied energy is transformed into sound energy), determine the total time the siren can sound.
68. A siren creates a sound level $\beta$ at a distance $d$ from the speaker. The siren is powered by a battery that delivers a total energy $E$. Assuming that the efficiency of the siren is $e$ (that is, $e$ is equal to the output sound energy divided by the supplied energy), determine the total time the siren can sound.
69. The Doppler equation presented in the text is valid when the motion between the observer and the source occurs on a straight line, so that the source and observer are moving either directly toward or directly away from each other. If this restriction is relaxed, one must use the more general Doppler equation

$$
f^{\prime}=\left(\frac{v+v_{O} \cos \theta_{O}}{v-v_{S} \cos \theta_{S}}\right) f
$$



Figure P17.69
where $\theta_{O}$ and $\theta_{S}$ are defined in Figure P17.69a. (a) Show that if the observer and source are moving away from each other, the preceding equation reduces to Equation 17.17 with lower signs. (b) Use the preceding equation to solve the following problem. A train moves at a constant speed of $25.0 \mathrm{~m} / \mathrm{s}$ toward the intersection shown in Figure P17.69b. A car is stopped near the intersection, 30.0 m from the tracks. If the train's horn emits a frequency of 500 Hz , what frequency is heard by the passengers in the car when the train is 40.0 m from the intersection? Take the speed of sound to be $343 \mathrm{~m} / \mathrm{s}$.
70. Figure 17.5 illustrates that at distance $r$ from a point source with power $\mathscr{P}_{\text {av }}$, the wave intensity is $I=$ $\mathscr{P}_{\text {av }} / 4 \pi r^{2}$. Study Figure 17.11a and prove that at distance $r$ straight in front of a point source with power $\mathscr{P}_{\text {av }}$, moving with constant speed $v_{S}$, the wave intensity is

$$
I=\frac{\mathscr{P}_{\mathrm{av}}}{4 \pi r^{2}}\left(\frac{v-v_{S}}{v}\right)
$$

71. Three metal rods are located relative to each other as shown in Figure P17.71, where $L_{1}+L_{2}=L_{3}$. The den-
sity values and Young's moduli for the three materials are $\rho_{1}=2.70 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}, Y_{1}=7.00 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$; $\rho_{2}=11.3 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}, Y_{2}=1.60 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$; $\rho_{3}=8.80 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}, Y_{3}=11.0 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$.
(a) If $L_{3}=1.50 \mathrm{~m}$, what must the ratio $L_{1} / L_{2}$ be if a sound wave is to travel the combined length of rods 1 and 2 in the same time it takes to travel the length of $\operatorname{rod} 3$ ? (b) If the frequency of the source is 4.00 kHz , determine the phase difference between the wave traveling along rods 1 and 2 and the one traveling along $\operatorname{rod} 3$.


Figure P17.71
72. The volume knob on a radio has what is known as a "logarithmic taper." The electrical device connected to the knob (called a potentiometer) has a resistance $R$ whose logarithm is proportional to the angular position of the knob: that is, $\log R \propto \theta$. If the intensity of the sound $I$ (in watts per square meter) produced by the speaker is proportional to the resistance $R$, show that the sound level $\beta$ (in decibels) is a linear function of $\theta$.
73. The smallest wavelength possible for a sound wave in air is on the order of the separation distance between air molecules. Find the order of magnitude of the highestfrequency sound wave possible in air, assuming a wave speed of $343 \mathrm{~m} / \mathrm{s}$, a density of $1.20 \mathrm{~kg} / \mathrm{m}^{3}$, and an average molecular mass of $4.82 \times 10^{-26} \mathrm{~kg}$.

## Answers to Quick Quizzes

17.1 The only correct answer is (c). Although the speed of a wave is given by the product of its wavelength and frequency, it is not affected by changes in either one. For example, if the sound from a musical instrument increases in frequency, the wavelength decreases, and thus $v=\lambda f$ remains constant. The amplitude of a sound wave determines the size of the oscillations of air molecules but does not affect the speed of the wave through the air.
17.2 The ground tremor represents a sound wave moving through the Earth. Sound waves move faster through the Earth than through air because rock and other ground materials are much stiffer against compression. Therefore - the vibration through the ground and the sound in the air having started together-the vibration through the ground reaches the observer first.
17.3 Because the bottom of the bottle does not allow molecular motion, the displacement in this region is at its minimum value. Because the pressure variation is a maximum when the displacement is a minimum, the pressure variation at the bottom is a maximum.
17.4 (a) 10 dB . If we call the intensity of each violin $I$, the total intensity when all the violins are playing is $I+9 I=10 I$. Therefore, the addition of the nine violins increases the intensity of the sound over that of one violin by a factor of 10 . From Equation 17.7 we see that an increase in intensity by a factor of 10 increases the sound level by 10 dB . (b) 13 dB . The intensity is now increased by a factor of 20 over that of a single violin.
17.5 The Mach number is the ratio of the plane's speed (which does not change) to the speed of sound, which is greater in the warm air than in the cold, as we learned
in Section 17.1 (see Quick Quiz 17.1). The denominator of this fraction increases while the numerator stays constant. Therefore, the fraction as a whole - the Mach number-decreases.
17.6 (a) In the reference frame of the air, the observer is moving toward the source at the wind speed through stationary air, and the source is moving away from the observer with the same speed. In Equation 17.17, therefore, a plus sign is needed in both the numerator and
the denominator:

$$
f^{\prime}=\left(\frac{v_{\text {sound }}+v_{\text {wind }}}{v_{\text {sound }}+v_{\text {wind }}}\right) f
$$

meaning the observed frequency is the same as if no wind were blowing. (b) The observer "sees" the sound waves coming toward him at a higher speed
$\left(v_{\text {sound }}+v_{\text {wind }}\right)$. (c) At this higher speed, he attributes a greater wavelength $\lambda^{\prime}=\left(v_{\text {sound }}+v_{\text {wind }}\right) / f$ to the wave.


[^0]:    ${ }^{1}$ Although it is not proved here, the work done by the piston equals the energy carried away by the wave. For a detailed mathematical treatment of this concept, see Chapter 4 in Frank S. Crawford, Jr., Waves, Berkeley Physics Course, vol. 3, New York, McGraw-Hill Book Company, 1968.

[^1]:    ${ }^{2}$ The unit bel is named after the inventor of the telephone, Alexander Graham Bell (1847-1922). The prefix deci-is the SI prefix that stands for $10^{-1}$.

[^2]:    ${ }^{3}$ Named after the Austrian physicist Christian Johann Doppler (1803-1853), who discovered the effect for light waves.

