

8. From Eq. 38-49, the Lorentz factor is

$$\gamma = 1 + \frac{K}{mc^2} = 1 + \frac{80 \text{ MeV}}{135 \text{ MeV}} = 1.59 .$$

Solving Eq. 38-8 for the speed, we find

$$\gamma = \frac{1}{\sqrt{1 - (v/c)^2}} \implies v = c\sqrt{1 - \frac{1}{\gamma^2}}$$

which yields $v = 0.778c$ or $v = 2.33 \times 10^8 \text{ m/s}$. Now, in the reference frame of the laboratory, the lifetime of the pion is not the given τ value but is “dilated.” Using Eq. 38-9, the time in the lab is

$$t = \gamma\tau = (1.59) (8.3 \times 10^{-17} \text{ s}) = 1.3 \times 10^{-16} \text{ s} .$$

Finally, using Eq. 38-10, we find the distance in the lab to be

$$x = vt = (2.33 \times 10^8 \text{ m/s}) (1.3 \times 10^{-16} \text{ s}) = 3.1 \times 10^{-8} \text{ m} .$$