

41. (a) We use the relativistic relationship between speed and momentum:

$$p = \gamma mv = \frac{mv}{\sqrt{1 - (v/c)^2}},$$

which we solve for the speed  $v$ :

$$\frac{v}{c} = \sqrt{1 - \frac{1}{\left(\frac{pc}{mc^2}\right)^2 + 1}}.$$

For an antiproton  $mc^2 = 938.3 \text{ MeV}$  and  $pc = 1.19 \text{ GeV} = 1190 \text{ MeV}$ , so

$$v = c \sqrt{1 - \frac{1}{(1190 \text{ MeV}/938.3 \text{ MeV})^2 + 1}} = 0.785c.$$

For the negative pion  $mc^2 = 139.6 \text{ MeV}$ , and  $pc$  is the same. Therefore,

$$v = c \sqrt{1 - \frac{1}{(1190 \text{ MeV}/139.6 \text{ MeV})^2 + 1}} = 0.993c.$$

(b) See part (a).

(c) Since the speed of the antiprotons is about  $0.78c$  but not over  $0.79c$ , an antiproton will trigger C1.

(d) Since the speed of the negative pions exceeds  $0.79c$ , a negative pion will trigger C2.

(e) and (f) We use  $\Delta t = d/v$ , where  $d = 12 \text{ m}$ . For an antiproton

$$\Delta t = \frac{12 \text{ m}}{0.785(2.998 \times 10^8 \text{ m/s})} = 5.1 \times 10^{-8} \text{ s} = 51 \text{ ns},$$

and for a negative pion

$$\Delta t = \frac{12 \text{ m}}{0.993(2.998 \times 10^8 \text{ m/s})} = 4.0 \times 10^{-8} \text{ s} = 40 \text{ ns}.$$